

# *Effective model for the description of pions, eta and vector mesons in nuclear matter*

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Progress Report on “Properties of Hadrons in Nuclear Matter  
and Dilepton Emission in Relativistic Heavy-Ion Collisions”



**Măgurele, December 11th, 2008**

# OVERVIEW

- **Introduction and Motivation**
- **Model for pion-nucleon-resonance interaction**
  - Effective interaction
  - Three-level model
  - In-medium pion spectral functions
- **Model for vector mesons in vacuum**
  - Rho meson
  - Omega meson
  - Corrections to vacuum spectral functions
- **Model for eta-nucleon-resonance interaction**
- **Summary and Outlook**

# Introduction: the model so far

determine **self energies** of vector mesons in-medium

1) **Nucleonic Resonances Contributions**: forward Compton scattering

resonances:  $N^*(1440)$ ,  $N^*(1520)$ ,  $N^*(1535)$ ,  $N^*(1650)$ ,  $N^*(1680)$   
 $\Delta^*(1232)$ ,  $\Delta^*(1620)$ ,  $\Delta^*(1700)$ ,  $\Delta^*(1905)$

2) **Nonresonant scattering** of vector mesons off nucleons:

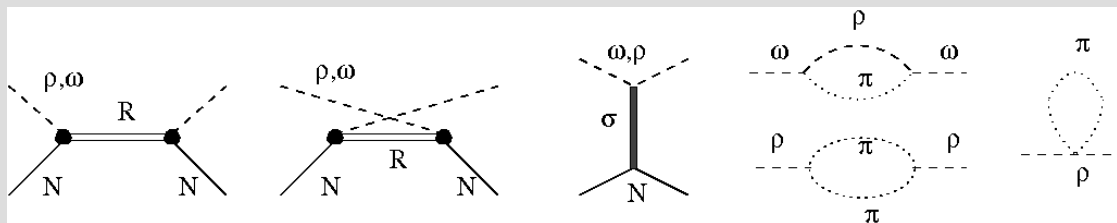
$\rho$ NN and  $\omega$ NN: Bonn nucleon-nucleon potential model

3) **Sigma meson exchanges**:

$g_{\rho\rho\sigma}$ : from the decay  $\rho^0 \rightarrow \rho^0 \sigma \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

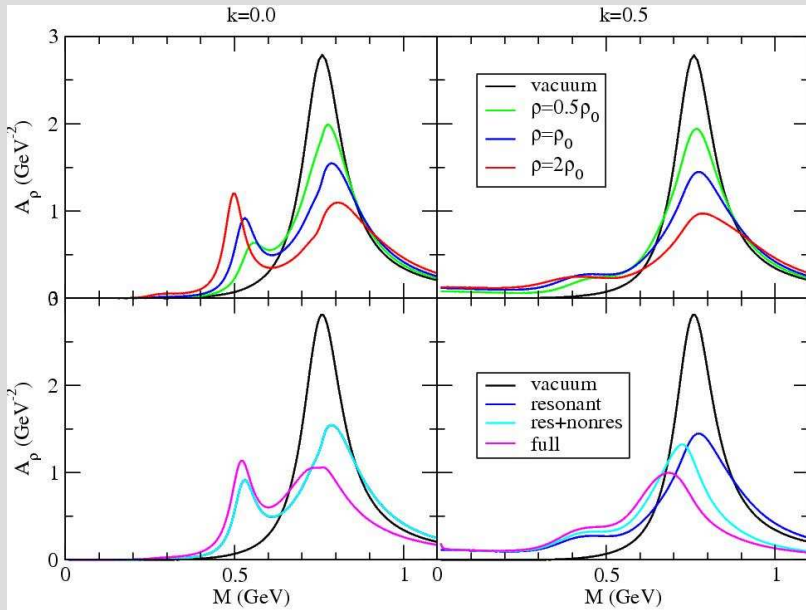
$$g_{\omega\omega\sigma} = 3g_{\rho\rho\sigma}$$

4) **Vacuum self-energies** parametrize results of  $\rho\pi\pi$  interaction for  $\rho$  and of the effective Gell-Mann-Sharp-Wagener for the  $\omega$

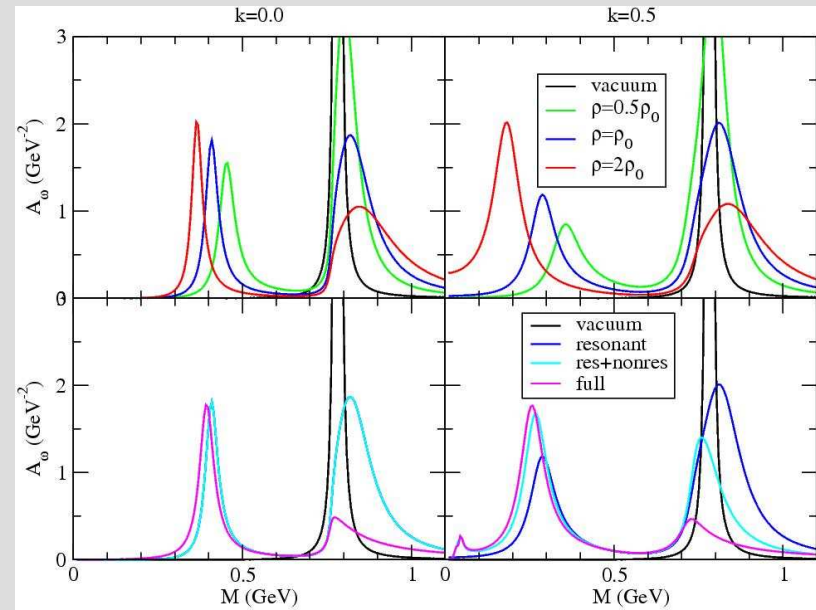


# In-medium spectral functions

$$A^{L,T}(p^2) = -\frac{1}{\pi} \frac{-\text{Im} \Sigma^{L,T}(p) + \sqrt{p^2} \Gamma^{vac}(p)}{[p^2 - m_0^2 - \text{Re} \Sigma^{L,T}(p)]^2 + [-\text{Im} \Sigma^{L,T}(p) + \sqrt{p^2} \Gamma^{vac}(p)]^2}$$



$N^*(1520)$ ,  $N^*(1535)$ ,  $\Delta(1620)$



$N^*(1535)$ ,  $N^*(1520)$

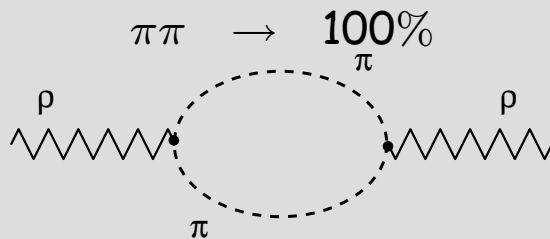
# What does PDG tell us about $\rho/\omega$ ?

## Rho (770)

Mass:  $769.3 \pm 0.8$  MeV

Width:  $150.2 \pm 0.8$  MeV

Decay modes:



## Omega (782)

Mass:  $782.57 \pm 0.12$  MeV

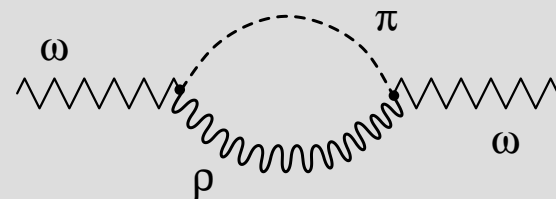
Width:  $8.44 \pm 0.09$  MeV

Decay modes:

$$\pi^+ \pi^- \pi^0 \rightarrow 88.8\%$$

$$\pi^0 \gamma \rightarrow 8.5\%$$

$$\pi^+ \pi^- \rightarrow 2.2\%$$



# Mesons In Nuclear Matter

**Objective:** extend the present model to properly (and consistently) consider all contributions at first order in an expansion in density

**At present:** - eVMD:  $RN\rho$  and  $RN\omega$

- nonresonant contributions:  $NN\rho$ ,  $NN\omega$
- t channel  $\rho$ -N and  $\omega$ -N scattering with  $\sigma$  exchange

**Missing:**

- proper treatment of the pion cloud (vacuum self-energies) in-medium
- at present only a parametrisation of the vacuum widths is considered

**Why should they be considered?**

- 1) consistency and 2) strong  $RN\pi$  interaction
- hints that they are important: [Urban et al., NPA 641, 433 \(1998\)](#)

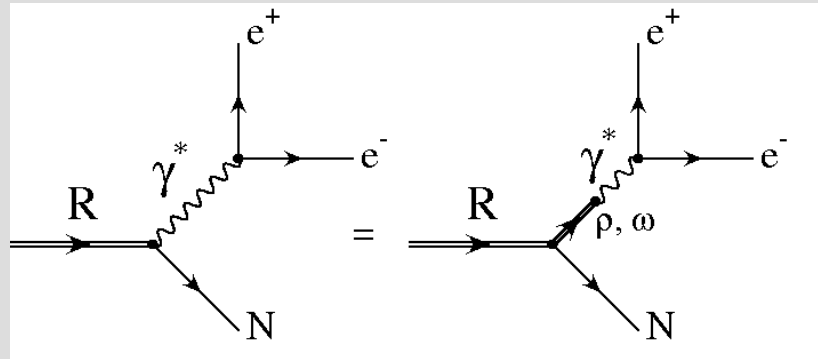
**Strategy:**

- model for pions in nuclear matter
- model for pion-rho meson interaction
- model for omega-rho-pion-photon interaction

# Extended VMD model

consider nucleon resonances  $R = \Delta^*, N^*$  with mass below 2 GeV and spin  $J \leq \frac{7}{2}$

unified description of resonance dilepton decays, resonance meson decays, resonance photo-production and meson dilepton decays



## Vector Meson Dominance (VMD):

$$J_\mu(p_R, \lambda_R, p, \lambda) = e \bar{u}_{\beta_1 \dots \beta_2}(p_R, \lambda_R) \Gamma_{\beta_1 \dots \beta_2 \mu}^{(\pm)} u(p, \lambda),$$

$$\Gamma_{\beta_1 \dots \beta_l \mu}^{(\pm)} = q_{\beta_1} \cdots q_{\beta_{l-1}} \sum_k \Gamma_{\beta_l \mu}^{(\pm) k} F_k^{(\pm)}$$

$$F_k^{(\pm)}(q^2) = \sum_V \frac{f_{VNR,k}^{(\pm)}}{g_V} \frac{1}{1 - q^2/m_V^2}.$$

Decay modes:  $\Delta^* \rightarrow N\rho$        $N^* \rightarrow N\rho/\omega$

M. Krivoruchenko, B. Martemyanov *Ann. Phys.* 296, 299 (2002)

# $RN\pi$ interactions

consider all resonances of spin 1/2 and spin 3/2

$S_{11}$  and  $S_{31}$  resonances

$$\mathcal{L} = -g\bar{\psi}_R \vec{\tau} \psi \vec{\pi} + h.c.$$

$P_{11}$  and  $P_{31}$  resonances

$$\mathcal{L} = -g\bar{\psi}_R \gamma_5 \gamma_\mu \vec{\tau} \psi \partial^\mu \vec{\pi} + h.c.$$

spin 3/2: gauge invariant couplings ([Pascalutsa nucl-th/9905065](https://arxiv.org/abs/nucl-th/9905065))

$P_{13}$  and  $P_{33}$  resonances

$$\begin{aligned}\mathcal{L} &= -g\bar{\psi} \gamma_5 \gamma_\mu \vec{\tau} \tilde{G}^{\mu\nu} \partial_\nu \vec{\pi} + h.c. \\ \tilde{G}^{\mu\nu} &= \frac{1}{2} \varepsilon^{\mu\nu\rho\sigma} G_{\rho\sigma}; \quad G^{\mu\nu} = \partial^\mu \psi^\nu - \partial^\nu \psi^\mu\end{aligned}$$

$D_{13}$  and  $D_{33}$  resonances

$$\mathcal{L} = -g\bar{\psi} \gamma_5 \gamma_\mu \gamma_n u \vec{\tau} G^{\mu\rho} \partial_\rho \partial^\nu \vec{\pi} + h.c.$$

$NN\pi$ : customary pseudo-vector coupling



# Three-level model

simplification of the model allowing analytical calculations (Urban, NPA 643, 433)

## Approximations:

- allow only for  $\Delta(1232)$  and non-resonant scattering
- perform a non-relativistic reduction
- assume momentum of the hole ( $\vec{p}$ ) small compared with pion momentum ( $\vec{k}$ )

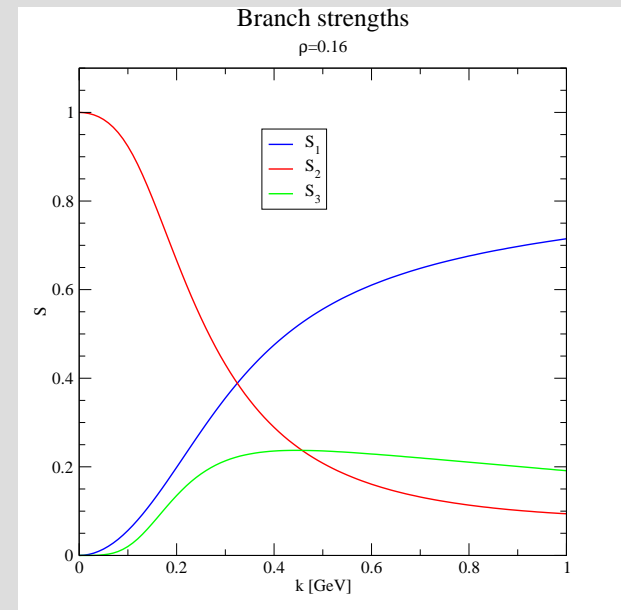
**Simplifications:** - self-energies expressions

$$\Sigma_{\pi N}(k) = \frac{\alpha_N(\vec{k})}{k_0^2 - \Omega_N^2(\vec{k}) + i\varepsilon}$$

$$\Sigma_{\pi \Delta}(k) = \frac{\alpha_\Delta(\vec{k})}{k_0^2 - \Omega_\Delta^2(\vec{k}) + i\varepsilon}$$

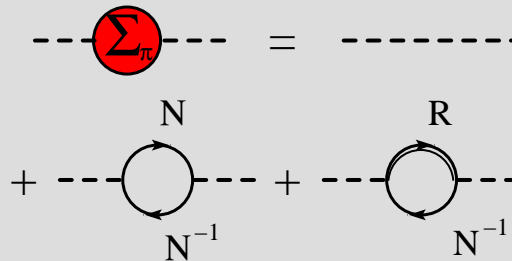
## Pion propagator:

$$\begin{aligned} \Delta_\pi(k) &= \frac{1}{k^2 - m_\pi^2 + \Sigma_{\pi N} + \Sigma_{\pi \Delta}} \\ &= \frac{S_1(\vec{k})}{k_0^2 - \omega_1^2(\vec{k})} + \frac{S_2(\vec{k})}{k_0^2 - \omega_2^2(\vec{k})} + \frac{S_3(\vec{k})}{k_0^2 - \omega_3^2(\vec{k})} \end{aligned}$$

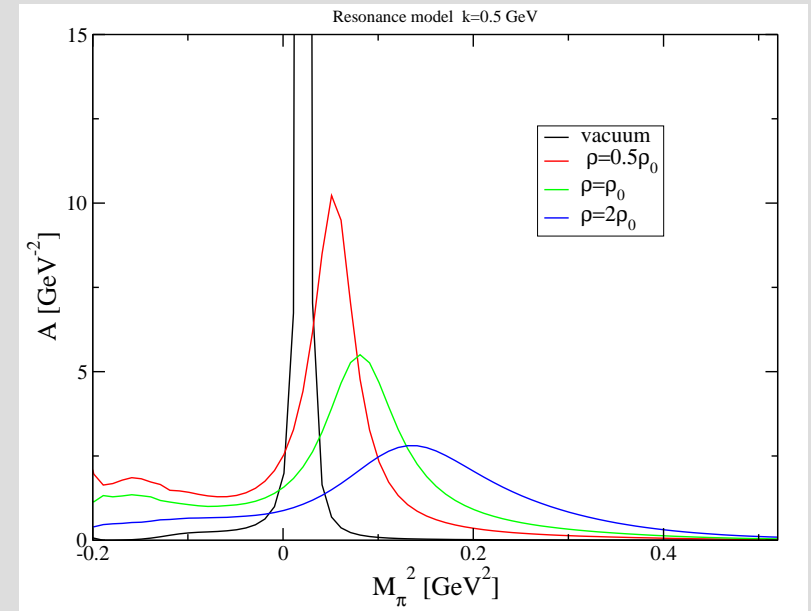
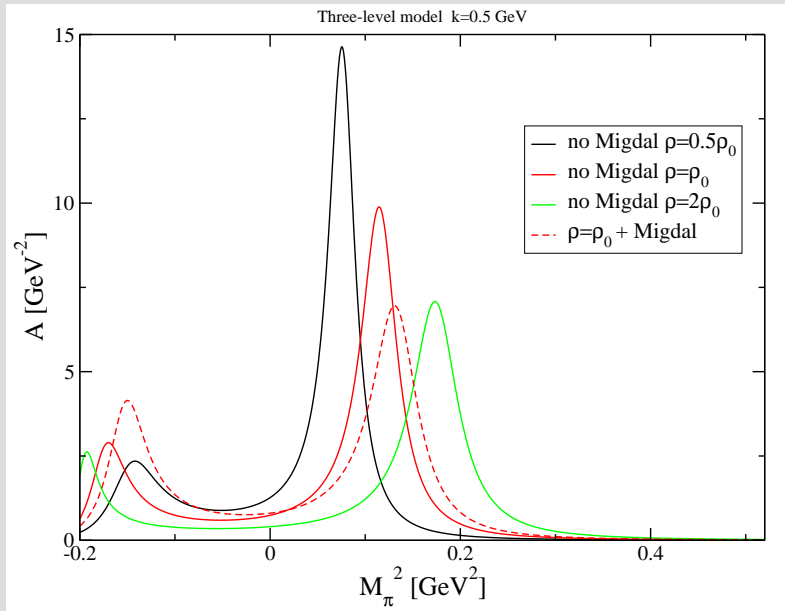


# In-medium pion spectral functions

Density expansion of the **pion propagator**



**Three-level model vs. Resonance model** pion spf



# Rho meson - pion interaction

Vacuum  $\rho$  meson - pion interaction

$$\mathcal{L}_0 = \frac{1}{2} \partial_\mu \vec{\pi} \cdot \partial^\mu \vec{\pi} - \frac{1}{2} m_\pi^2 \vec{\pi} \cdot \vec{\pi} - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} m_V^2 V_\mu V^\mu$$

$$\mathcal{L}_{\pi\rho} = \frac{i}{2} g V_\mu^a (\partial^\mu \pi_i T_{ij}^a \pi_j + \pi_i T_{ij}^a \partial^\mu \pi_j) - \frac{1}{2} g^2 V_\mu^a V^{\mu,b} T_{ij}^a \pi_j T_{ik}^b \pi_k$$

General expression for self-energy:

$$i\Sigma_{\mu\nu}(p) = \frac{1}{2} \int \frac{d^4k}{(2\pi)^4} iD_\pi(k) \Gamma_{\mu ab}(k, p) iD_\pi(k+p) \Gamma_{\nu ba}(k+p, -p)$$

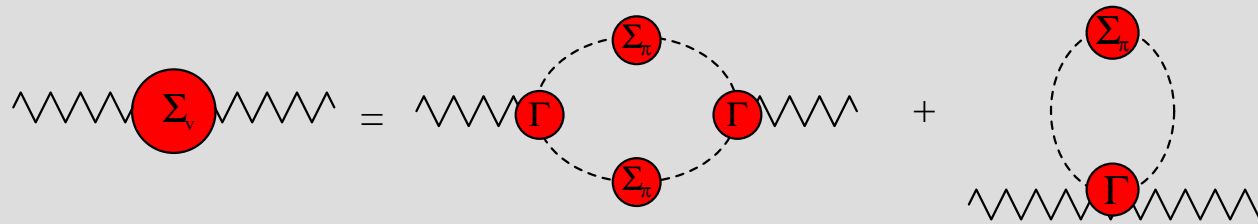
$$+ \frac{1}{2} \int \frac{d^4k}{(2\pi)^4} iD_\pi(k) \Gamma_{\mu\nu aa}(k, k, q)$$

$$\Gamma_{\mu ab}(k, q) = g\varepsilon_{3ab} (2k+p)_\mu + \Gamma'_{\mu ab}(k, q)$$

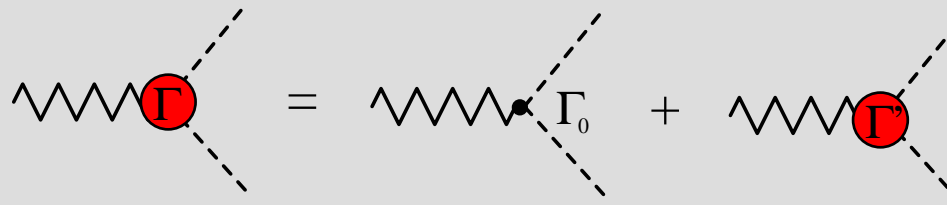
$$\Gamma_{\mu\nu ab}(k_1, k_2, p) = 2ig^2 (\delta_{ab} - \delta_{3a}\delta_{3b}) g_{\mu\nu} + \Gamma'_{\mu\nu ab}(k_1, k_2, p)$$

# Rho meson diagrammatics

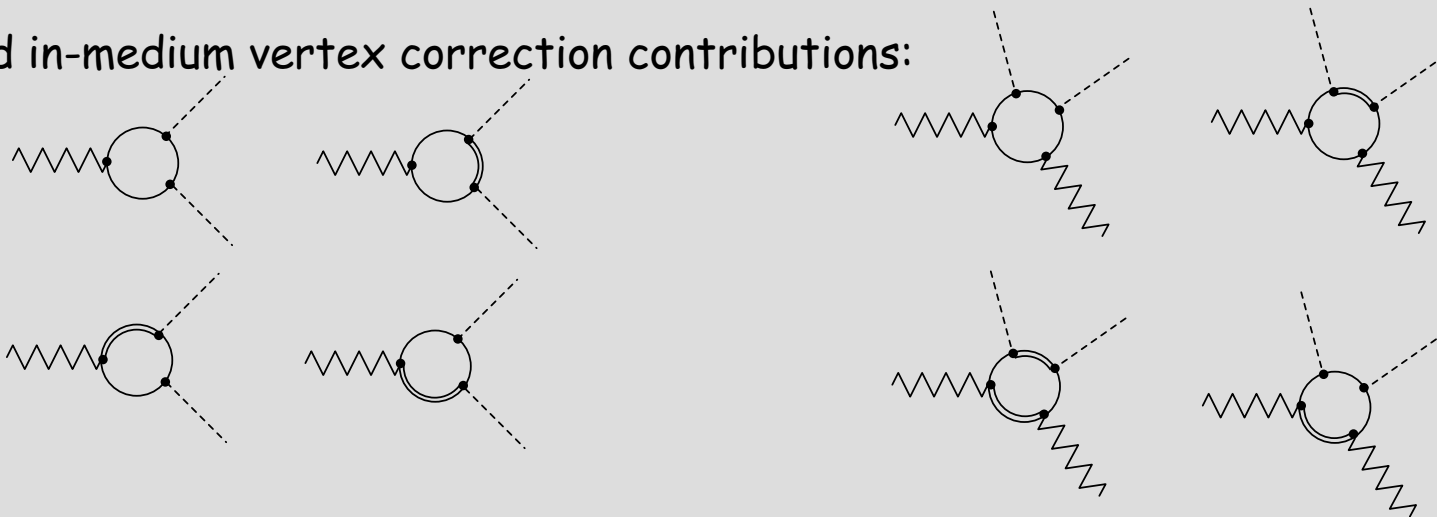
Diagrammatic representation of *in-medium rho meson self-energy*:



*In-medium corrections* to the  $\rho\pi\pi$  and  $\rho\rho\pi\pi$  vertices



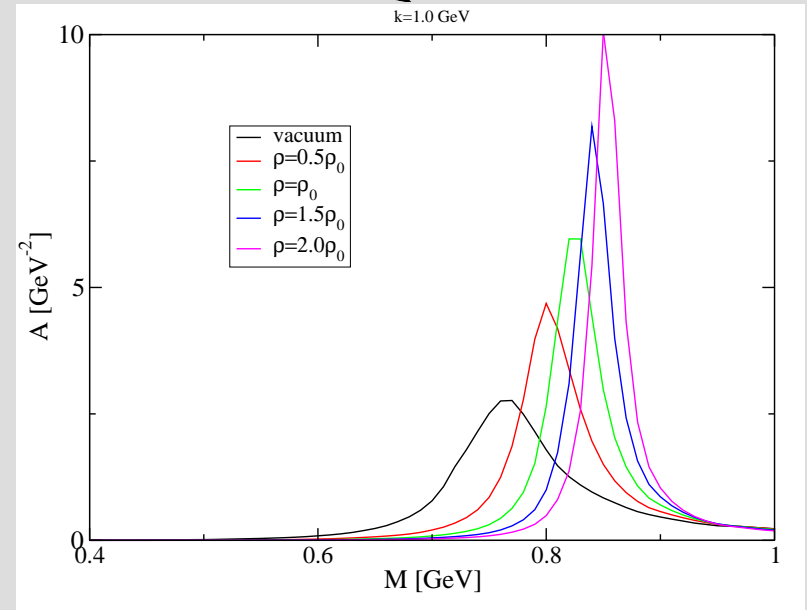
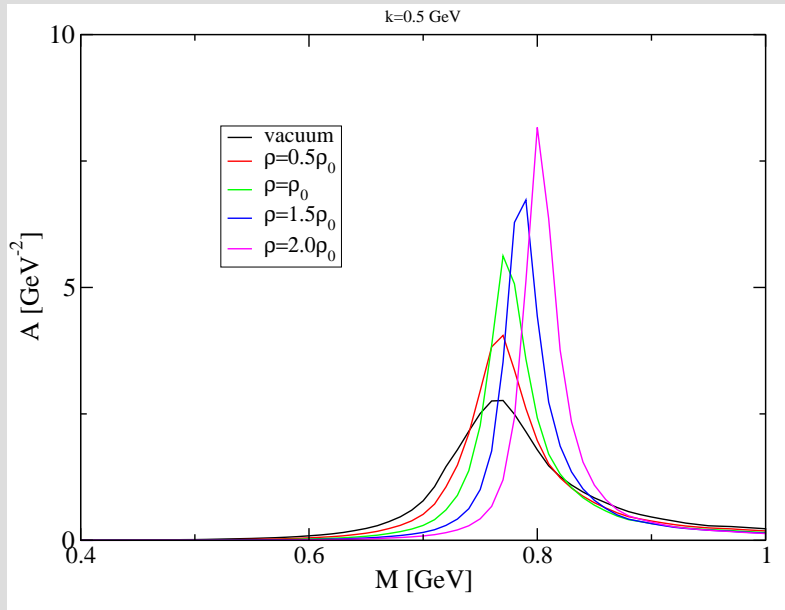
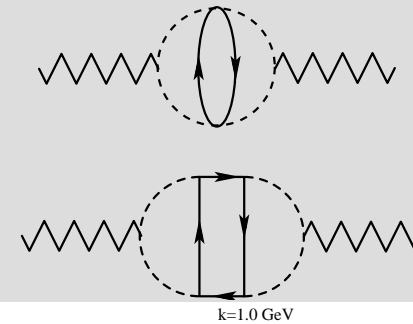
Selected in-medium vertex correction contributions:



# Rho meson spectral functions

Only contributions from the in-medium decay channel  $\rho \rightarrow \pi\pi$   
No resonance contributions !

Intentionally omitted graphs (would lead to double-counting):



# Omega meson effective model

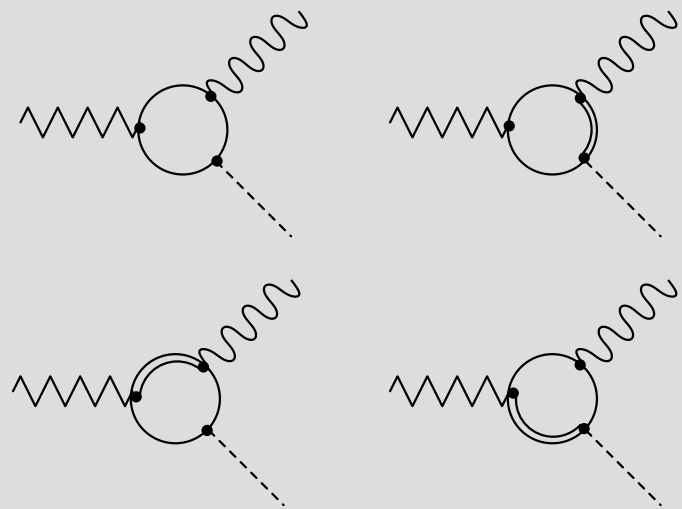
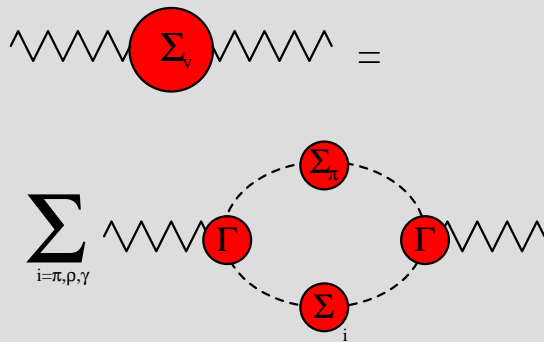
**Model** to explain the main **decay channels** in vacuum:

$$\mathcal{L}_{\omega\rho\pi} = -\frac{g_{\omega\rho\pi}}{4m_\pi} \vec{\pi} \epsilon_{\mu\nu\alpha\beta} \vec{\rho}^{\mu\nu} \omega^{\alpha\beta}$$

$$\mathcal{L}_{\omega\pi\gamma} = -e \frac{g_{\omega\pi\gamma}}{4m_\pi} \pi_0 \epsilon_{\mu\nu\alpha\beta} \omega^{\mu\nu} F^{\alpha\beta}$$

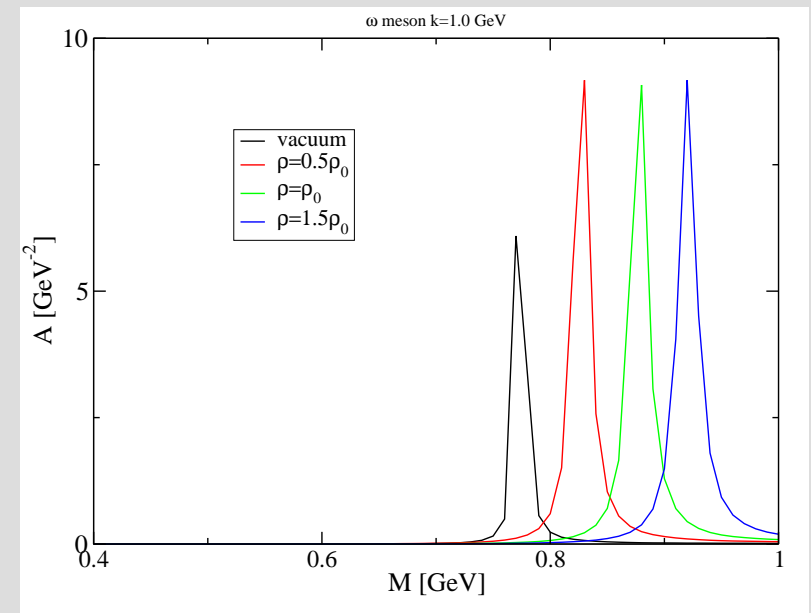
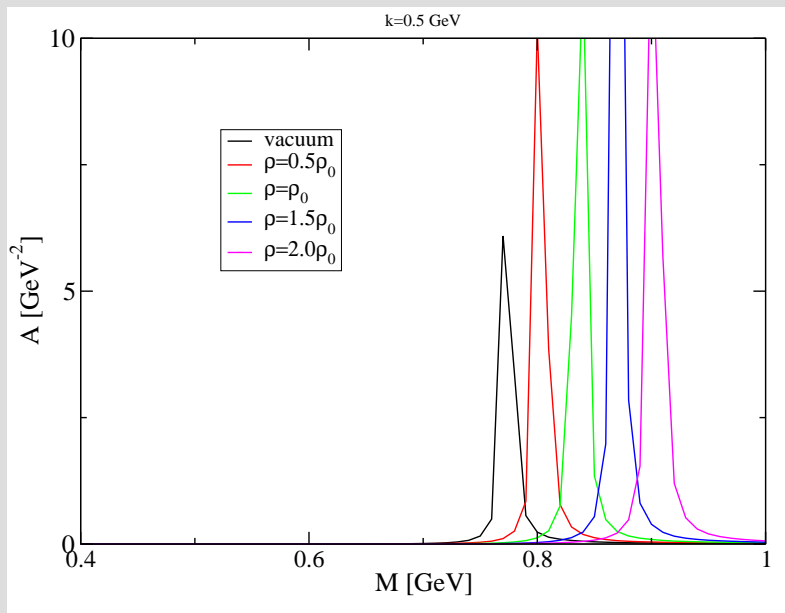
$$\mathcal{L}_{\omega\pi\pi} = -\frac{g_{\omega\pi\pi}}{2m_\pi} \omega_\mu (\partial^\mu \vec{\pi} \cdot \vec{\pi} + \vec{\pi} \cdot \partial^\mu \vec{\pi})$$

**In-medium self-energy** vs. **Medium corrections to the vertex function**:



# Omega meson spectral functions

No resonance contributions to self-energy (same as for  $\rho$ )



# In-medium $\eta$ (547) meson $\sigma$ f

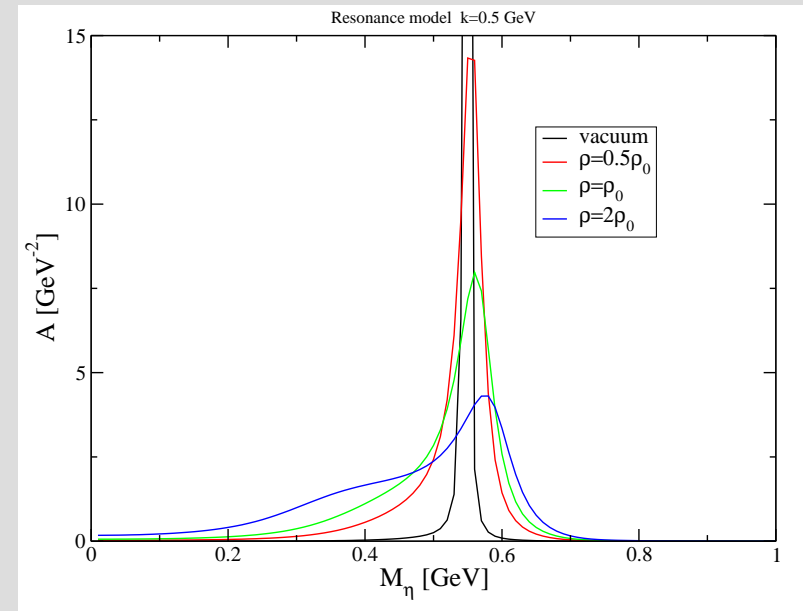
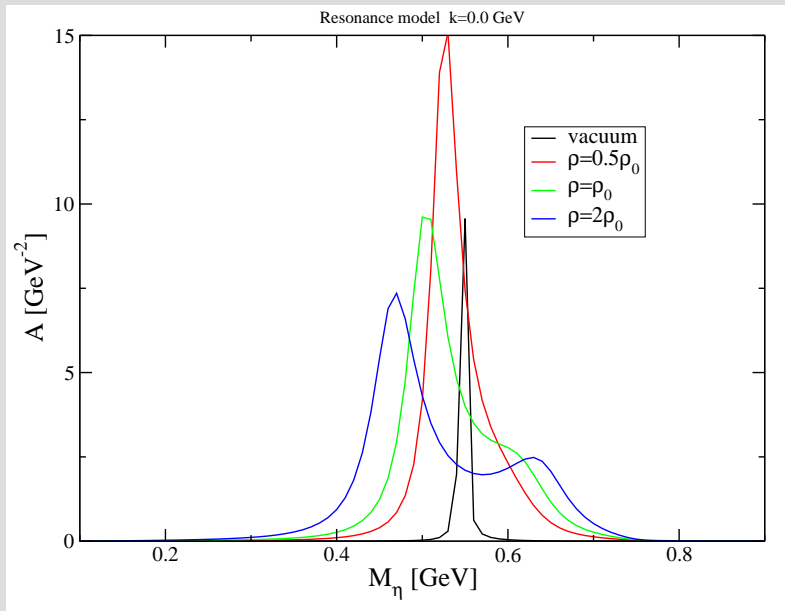
the only quantum number different from pion is isospin

use relevant  $\pi NR$  couplings as  $\eta NR$

non zero  $\Gamma_{R \rightarrow N\eta}$  decay widths: N(1535), N(1650), N(1700), N(1710)

background contribution:  $NN\eta$  - from an OBE model (not Bonn CD!)

Spectral function results:





# Summary and Outlook

- It is necessary to include medium corrections to the  $\omega$  vacuum self energy diagrams
- Extended the eVMD resonance model by including explicit  $\pi NR$  and  $\eta NR$  couplings
- Important medium-modification of the pion propagator, inline with findings by other authors
- Computed medium-corrections to the  $\rho$  and  $\omega$  vacuum self-energies by considering medium contributions to the virtual meson propagators and vertices
- Preliminary results indicate important contributions leading to a upward shift of vacuum masses
- Result for the  $\rho$  meson counter-intuitive
- To be done: Take into account all the vertex corrections contributing to the leading order in a expansion over density