

Heavy Ion Physics from molecular resonances to deconfinement (brief review)

A few remarks !

*“If you want to live a happy life,
tie it to a goal, not to people or things”*
(Albert Einstein)

“I want to know God's thoughts; the rest are details.”
(Albert Einstein)

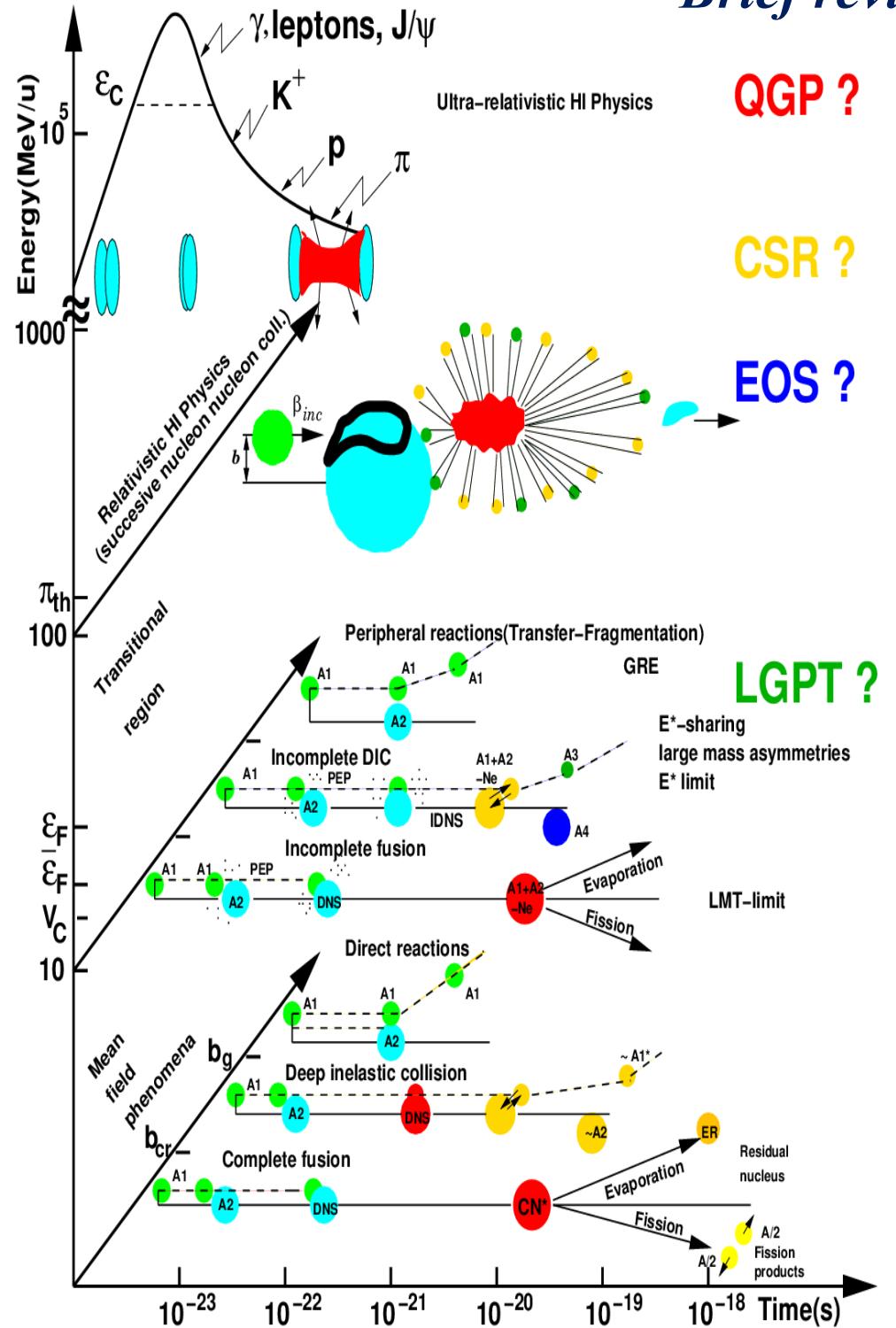
*“We are not to tell nature what she's gotta be ...
She's always got better imagination than we have.”*
(Richard Feynman)

*“The only way to make progress
is to defy one of those prohibitions that are
uncritically accepted without good reasons”*
(M. Gell-Mann)

*“If you thought that science was certain,
well that is just an error on your part.”*
(Richard Feynman)

*“Attempts to calculate the electron mass from the first principles
might be as futile as attempts to calculate the shape of the Solar System,
or the anatomy of frogs.
Still, we must try.”*
(Frank Wilczek)

Brief review



*The very first tandem accelerator experiments with heavy ions.
D.A.Bromley et al., Phys.Rev.Lett. 4(1960)365*

1978

Example of Molecular Resonances - experiment

Accélérateur tandem linéaire Van de Graaff. (Centre d'études nucléaires de Saclay.)

Saclay
Tandem

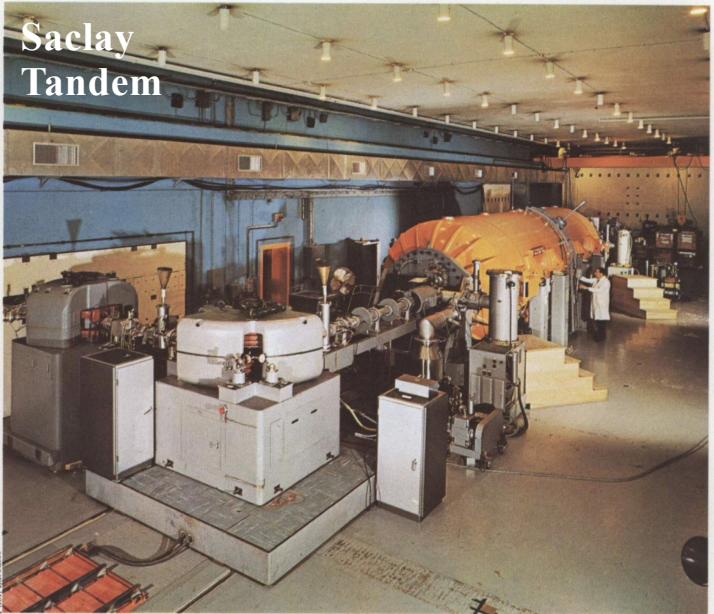
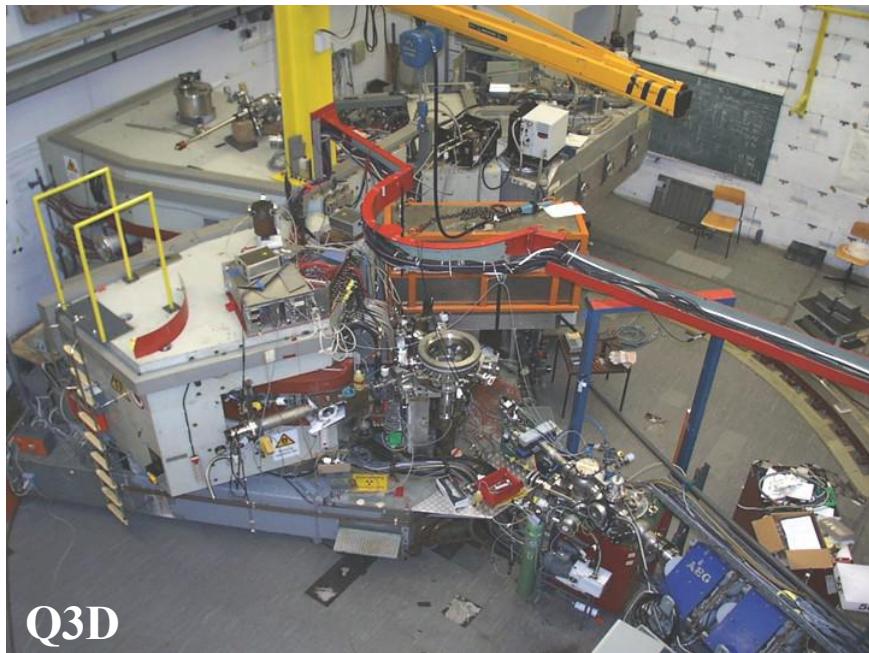
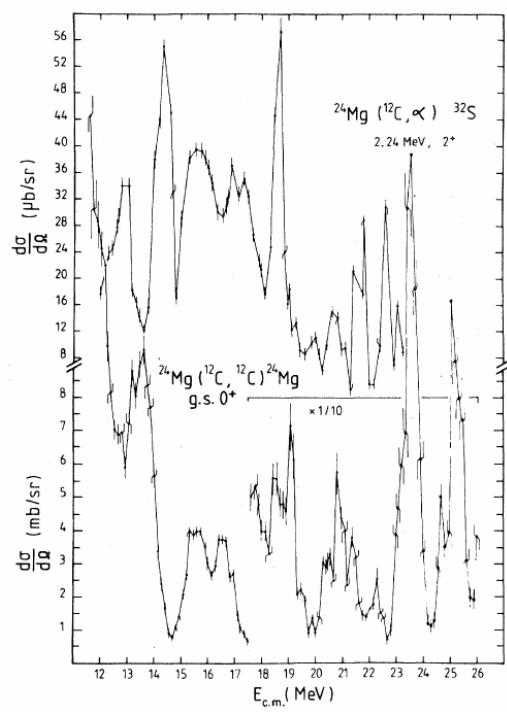
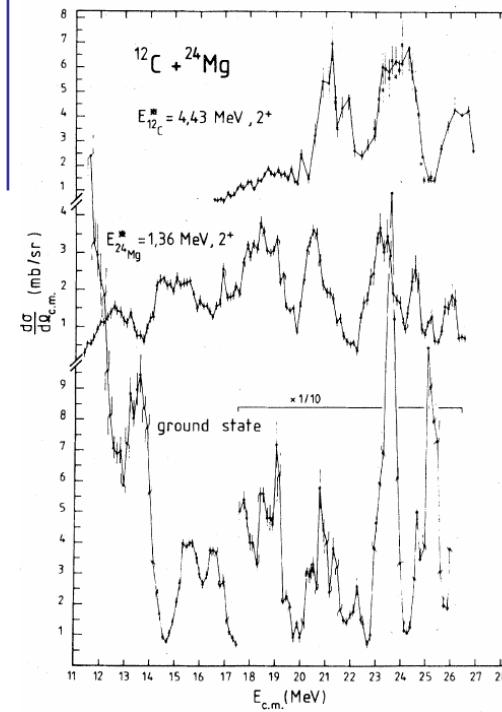
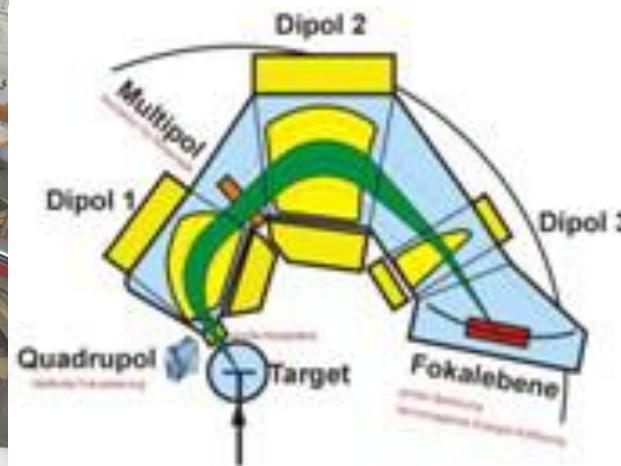


photo Lemaire



Q3D



M.C.Mermaz, A.Greiner, B.T.Kim, M.J.LeVine, E.Müller, M.Ruscev, M.Petrascu, M.Petrovici, and V.Simion, Phys.Rev. C24(1981)1512

Molecular Resonances - theory

For details see:

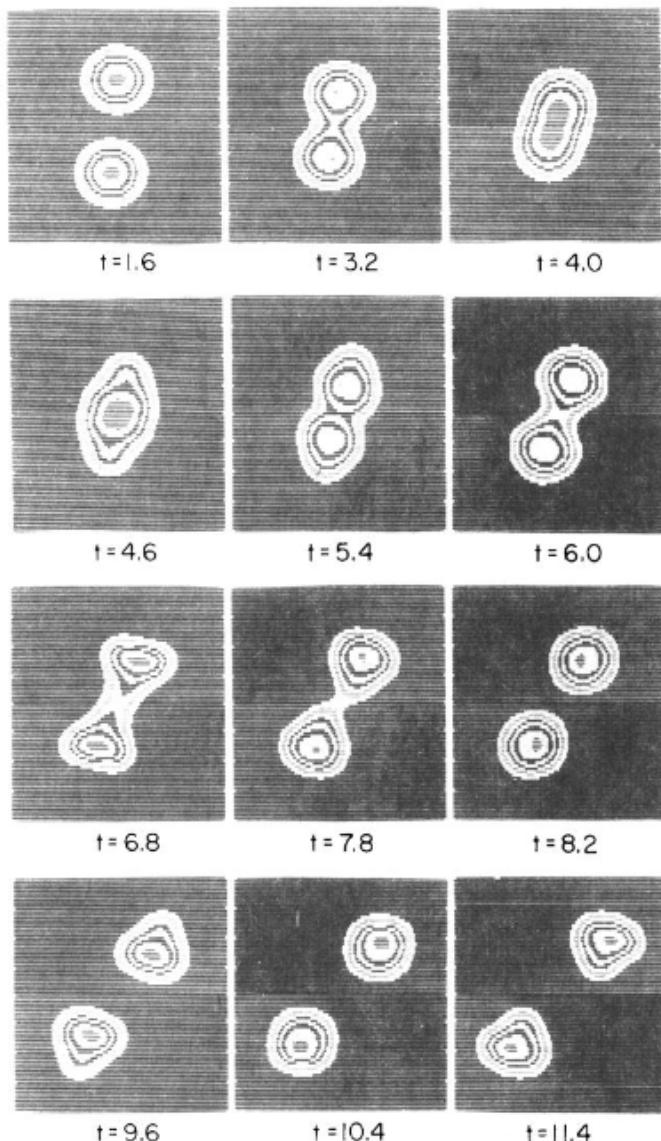
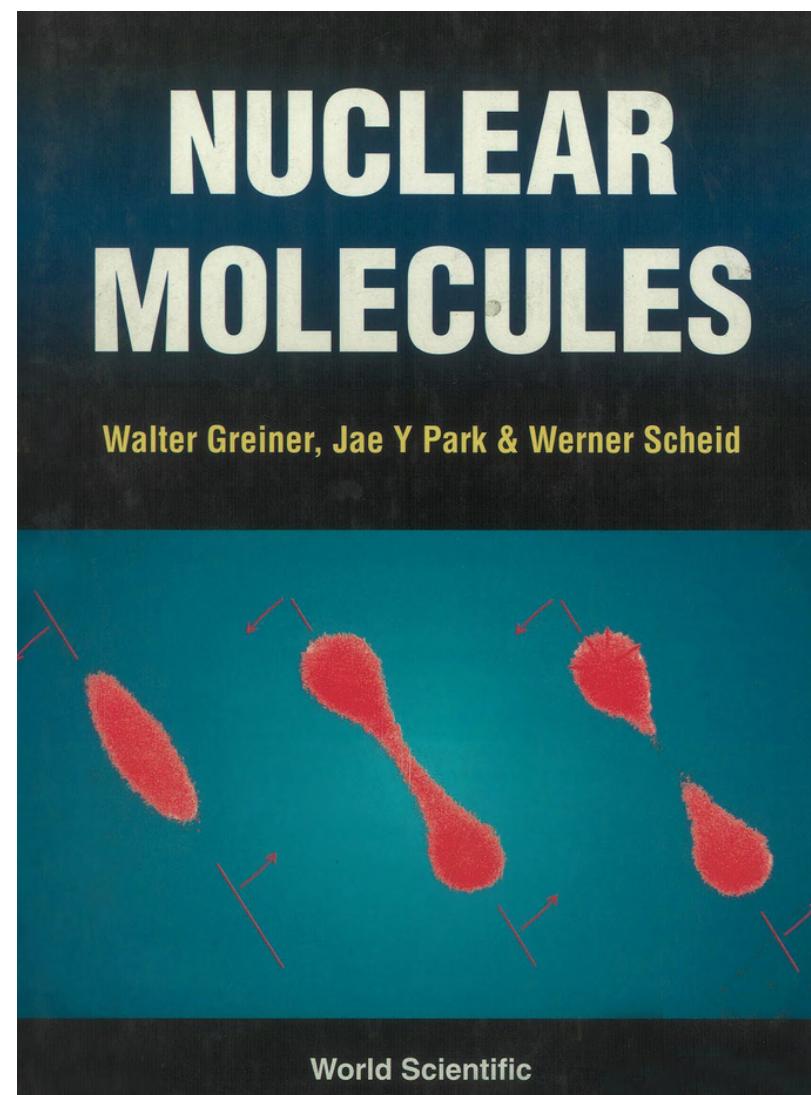


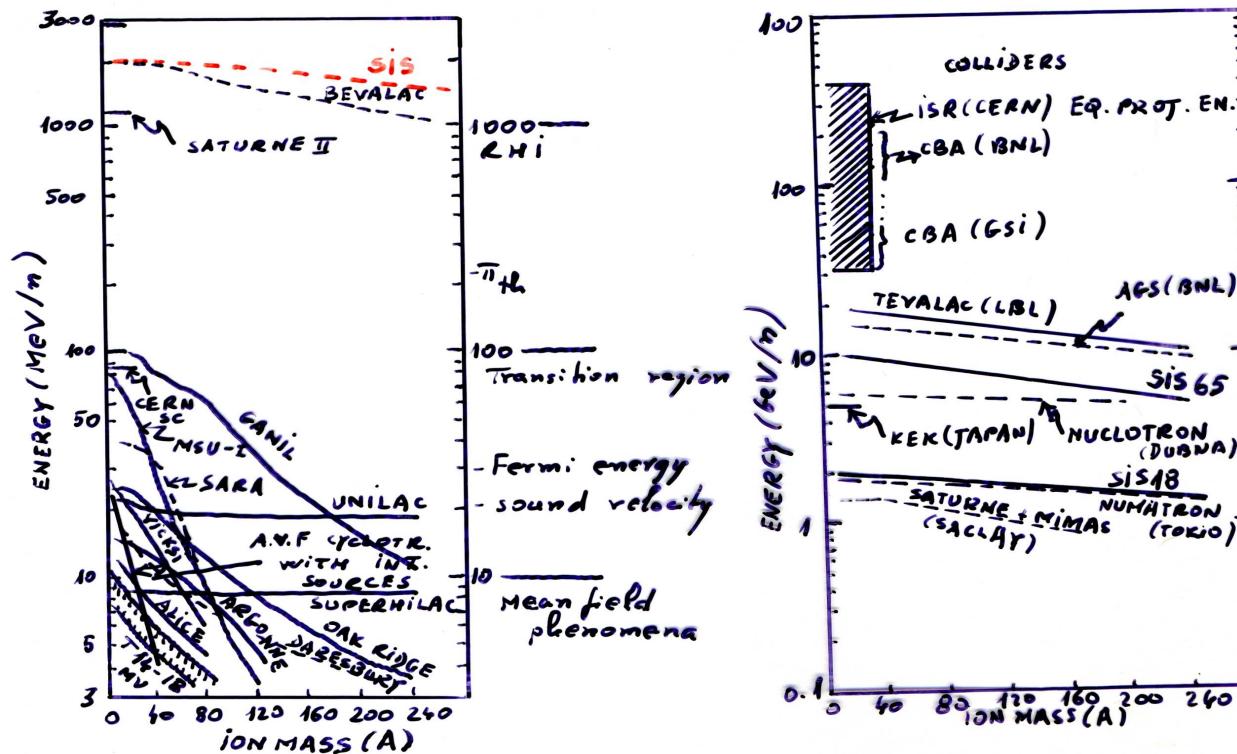
FIG. 3. Contour lines of the density integrated over the coordinate normal to the scattering plane for an $^{16}\text{O} + ^{16}\text{O}$ collision at $E_{\text{lab}} = 105$ MeV and incident angular momentum $L = 5\hbar$. The times t are given in units of 10^{-22} sec.

H.Flokard et al., Phys.Rev. C17(1978)1682



1995; ISBN 981-02-1723-4 & references therein

Status of the main facilities - 1980



The SSC: A machine for the nineties

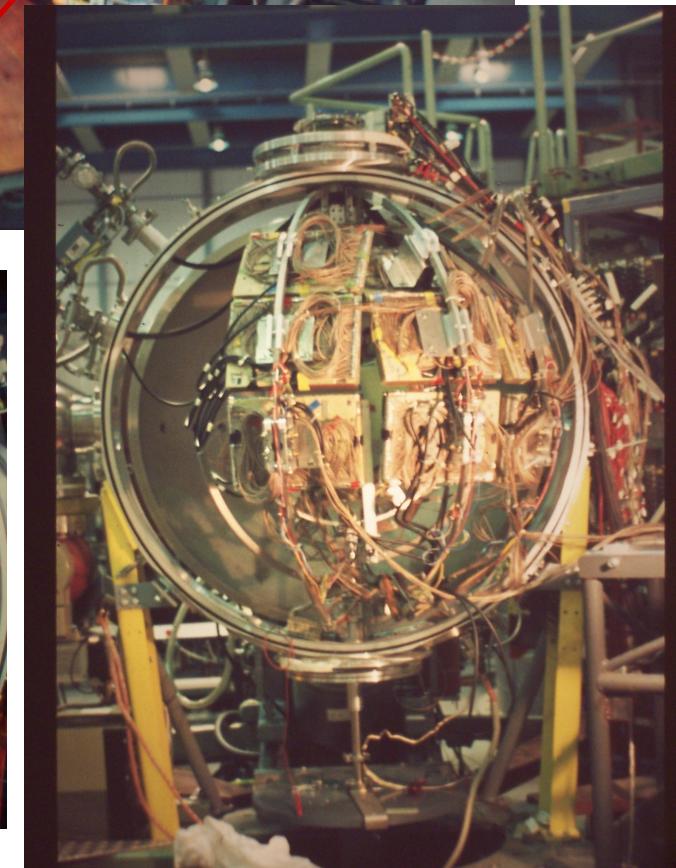
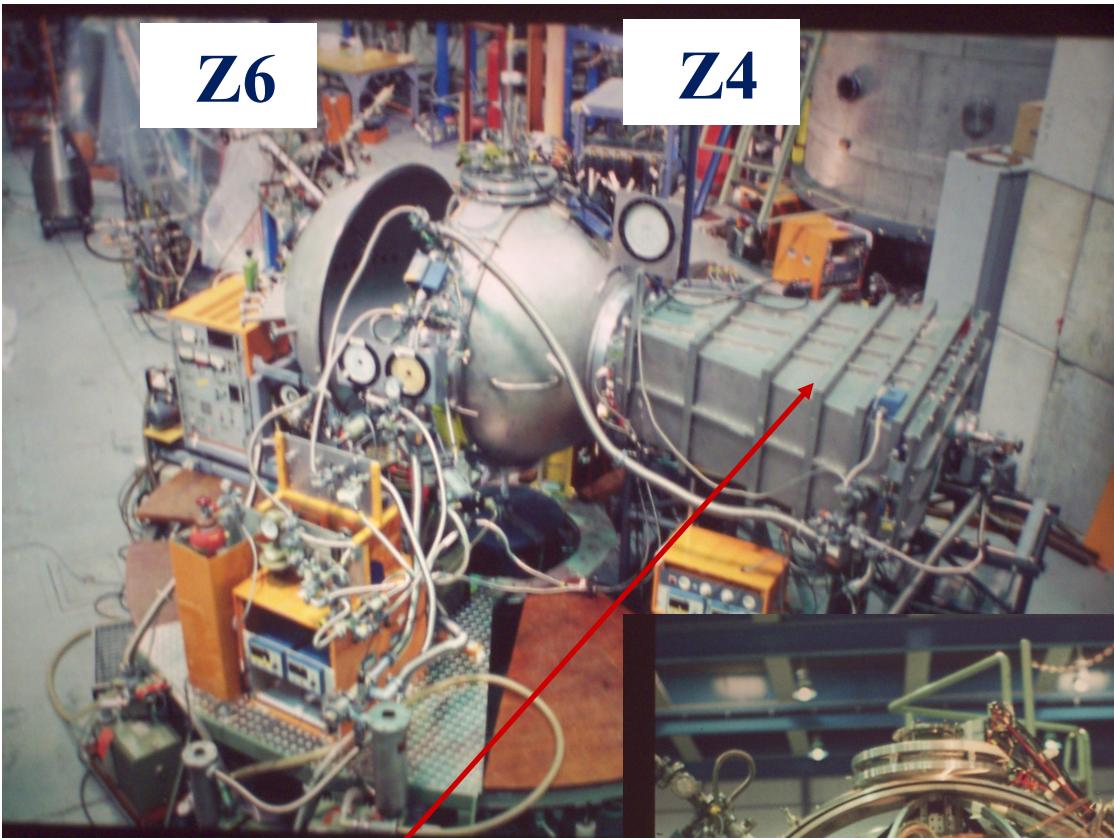
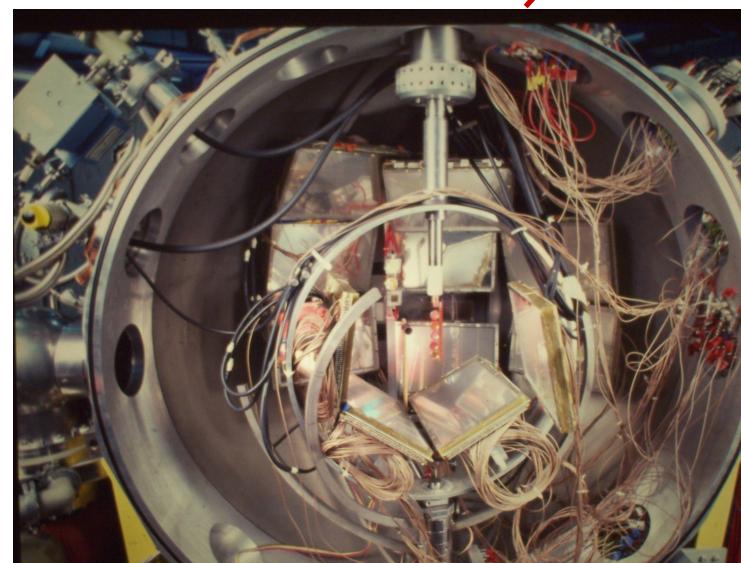
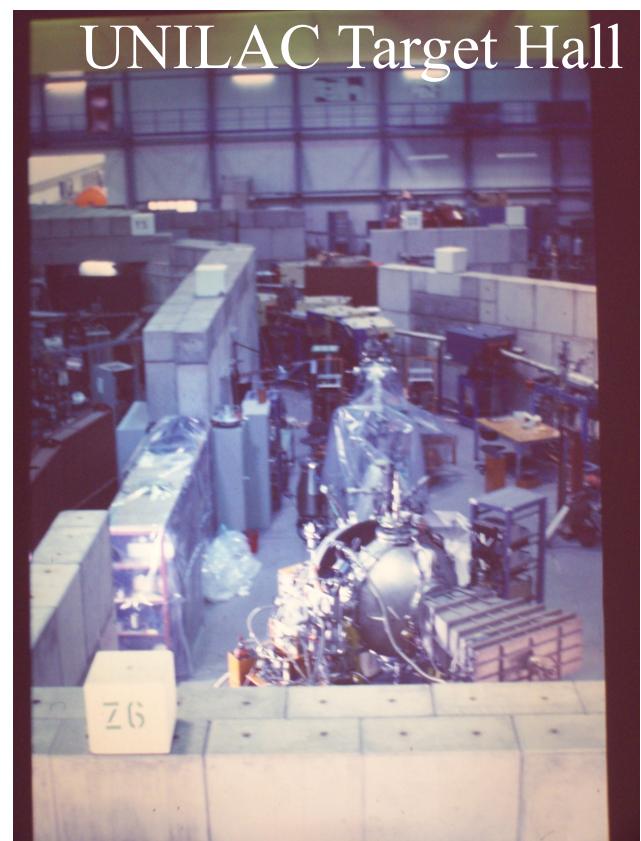
by Sheldon L. Glashow & Leon M. Lederman

The high-energy hadron accelerators

Machine	Location	Type	Beam energy (TeV)	CM energy (TeV)	Status
SPS	CERN	Fixed target	0.4	0.03	Operating
Tevatron II	Fermilab	"	0.8	0.04	"
ISR	CERN	pp collider	0.03	0.06	"
CBA (Isabelle)	BNL	pp - "	0.4	0.8	(Cancelled)
SppS	CERN	pp - "	0.32	0.64	Operating (84/85)
Tevatron I	Fermilab	pp - "	≥ 0.9	≥ 1.8	1986
Dedicated Coll.	Fermilab	pp - "	2.0	4.0	Not recommended
UNK	USSR	pp - "	3.0	6.0	1993 ?
SSC	?	pp collider	20	40	Our dream

Heavy Ion Dissipative Collisions

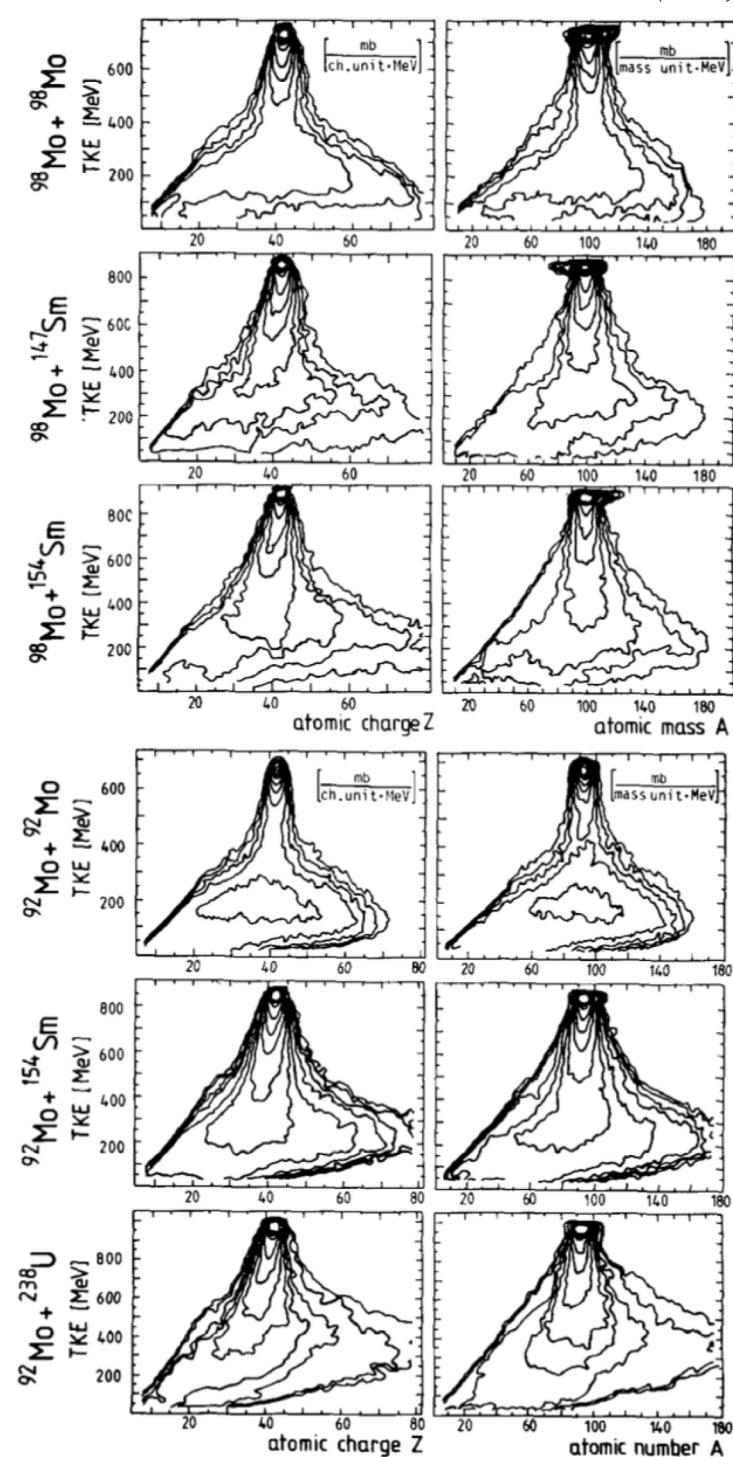
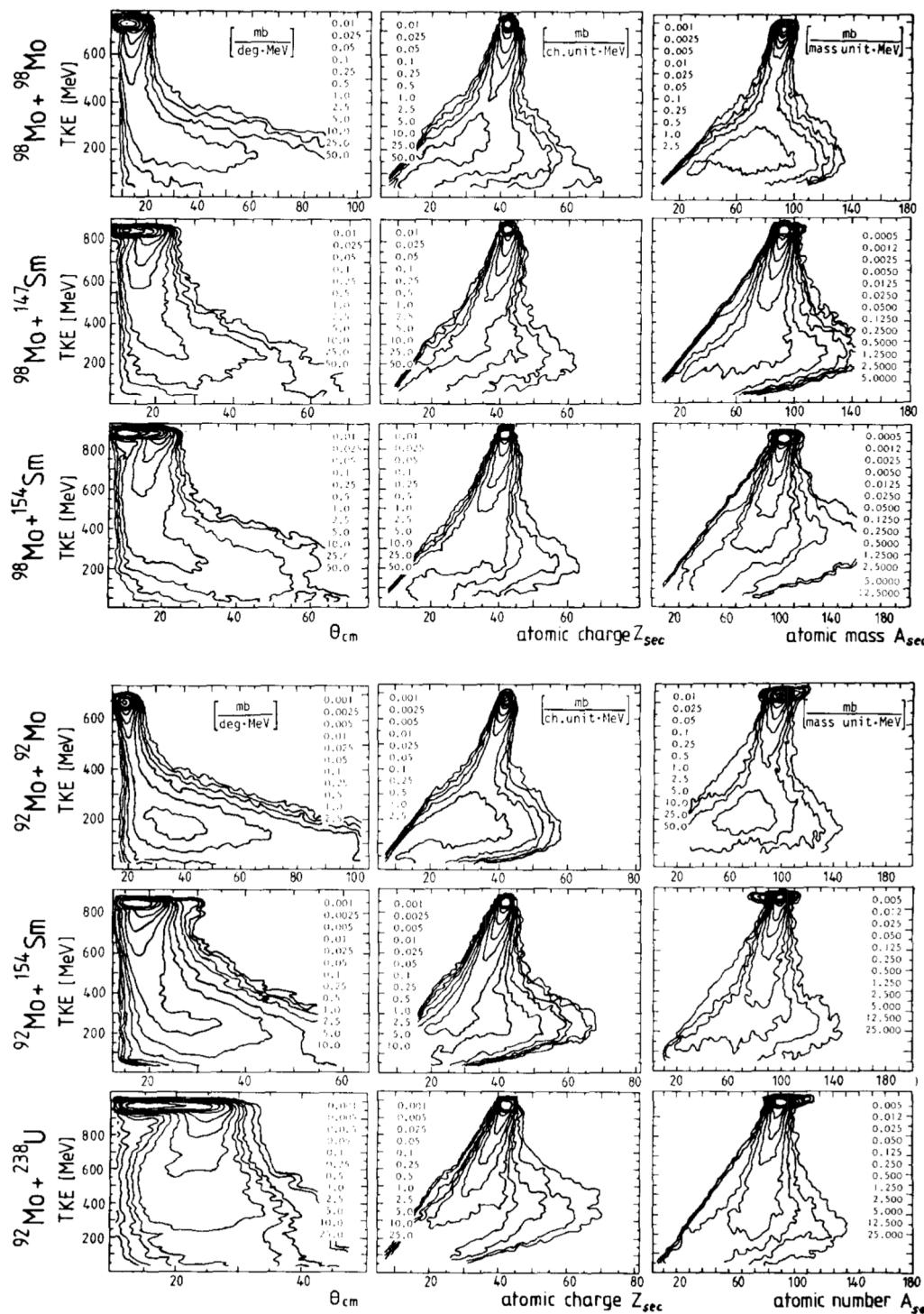
1981



Heavy ion dissipative collisions

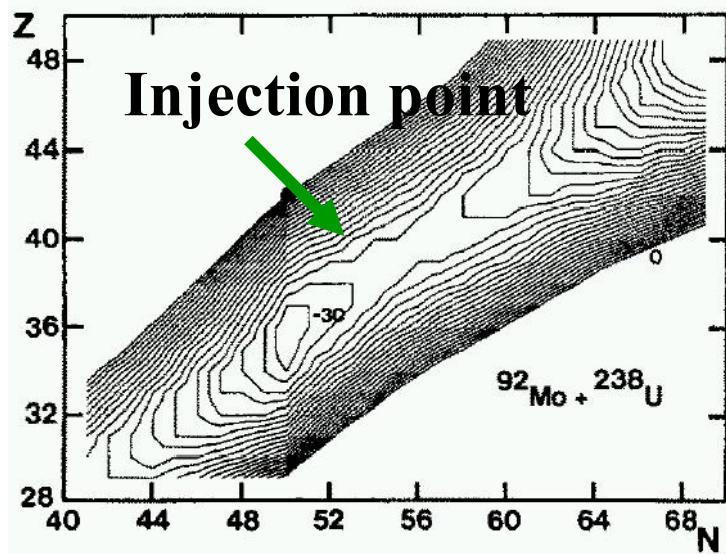
14.7 A•MeV

M. Petrovici et al., NPA477(1988)277



Heavy ion dissipative collisions

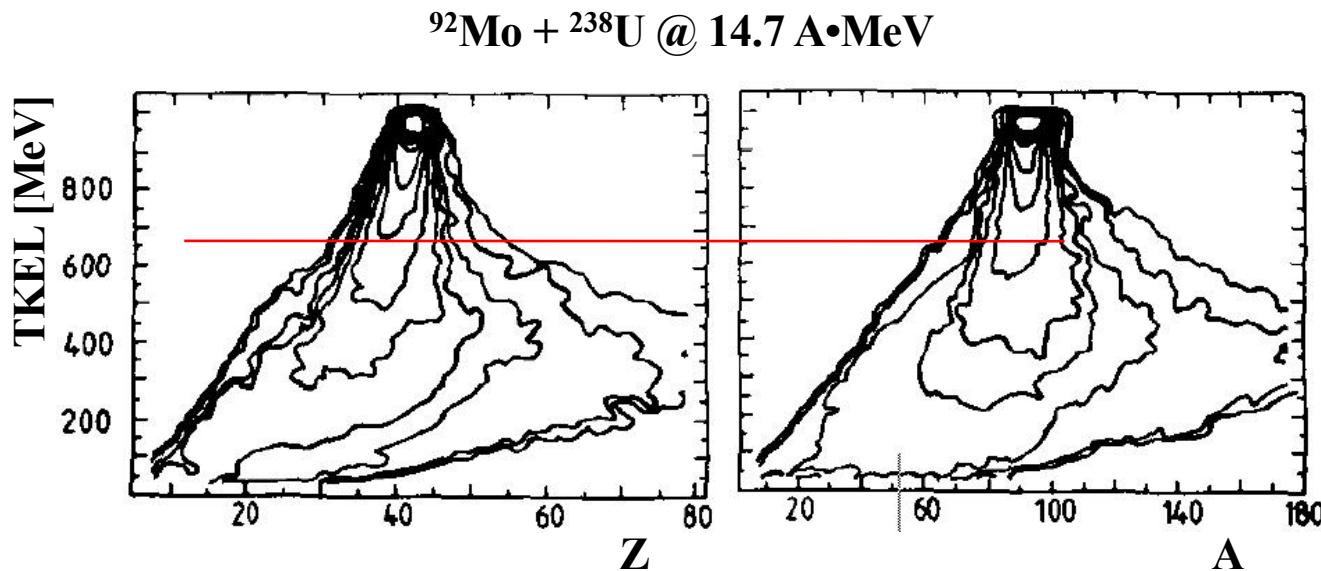
Dinuclear potential-energy



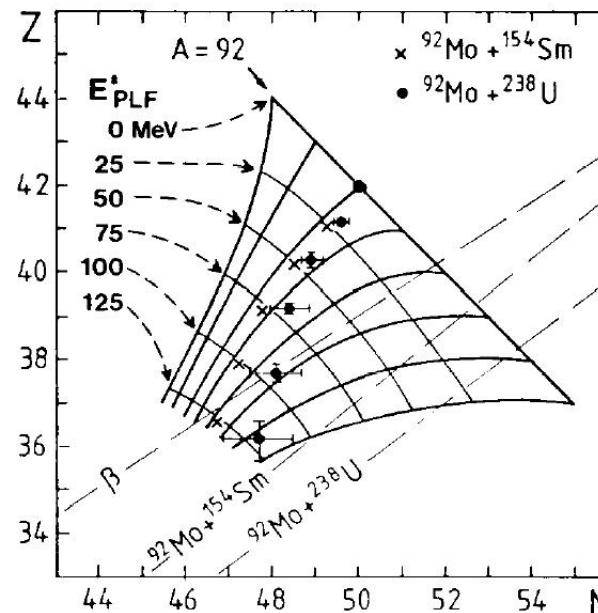
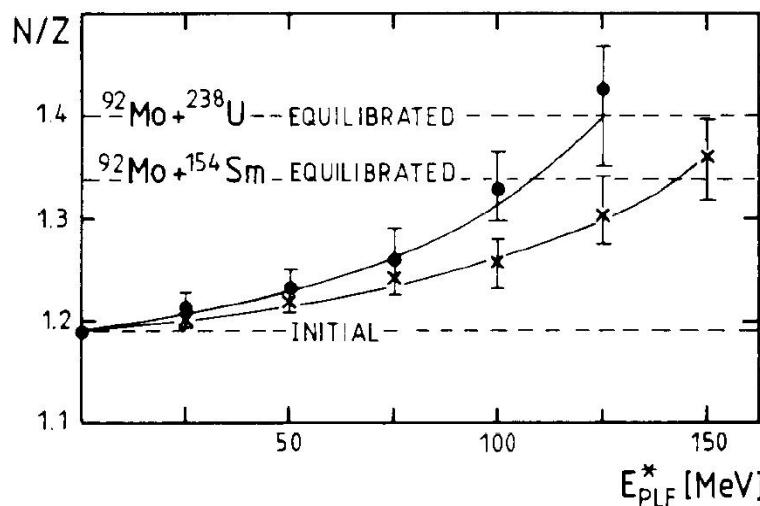
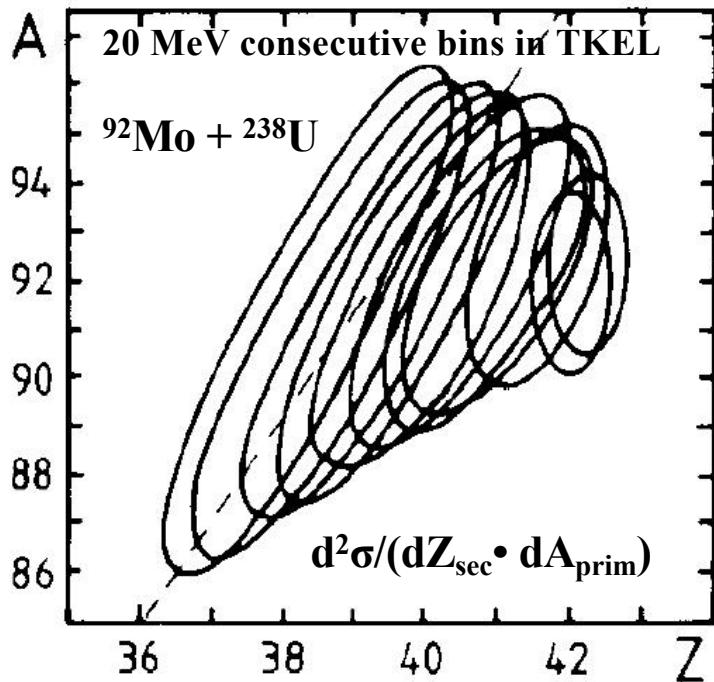
Strong gradient in the isospin dependent potential



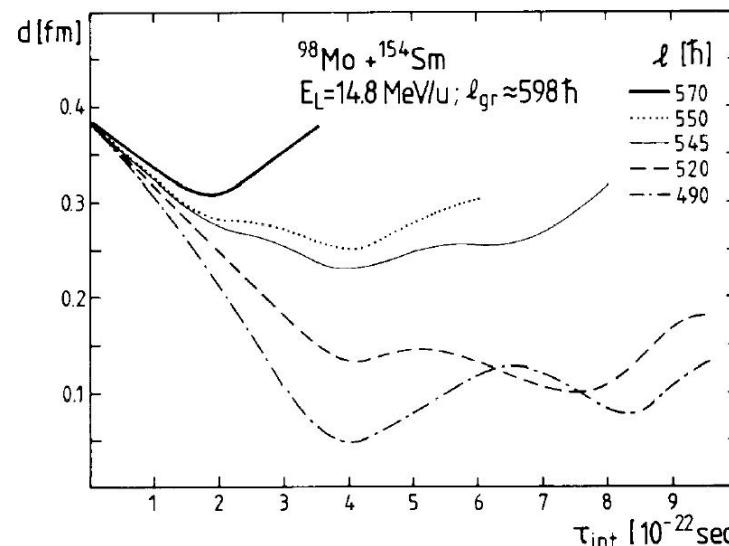
- *On a quantum treatment of charge equilibration in damped nuclear collisions*
M. Petrovici
J. Phys. G: Nucl. Phys. 7 (1981) 1515
- *Fast processes induced by heavy projectiles at incident energies of 10-20 MeV/u*
M. Petrovici, Invited talk
Int. Conf. on Selected Aspects in Heavy Ion Reactions, Saclay, 1982
Nucl. Phys. A387(1982)313c
- *The $^{92}\text{Mo}+^{92}\text{Mo}$ reaction at 14.7 MeV/u: approaching the limits of the classical deep inelastic process*
S. Gralla, R. Bock, A. Gobbi, K. D. Hildenbrand, J. Kuzminski, U. Lynen, W. F. J. Muller, A. Olmi, M. Petrovici, H. Sann, H. Stelzer, J. Toke, H. J. Wollersheim
Phys. Rev. Lett. 54(1985)1898



Heavy ion dissipative collisions



TDHF calculations

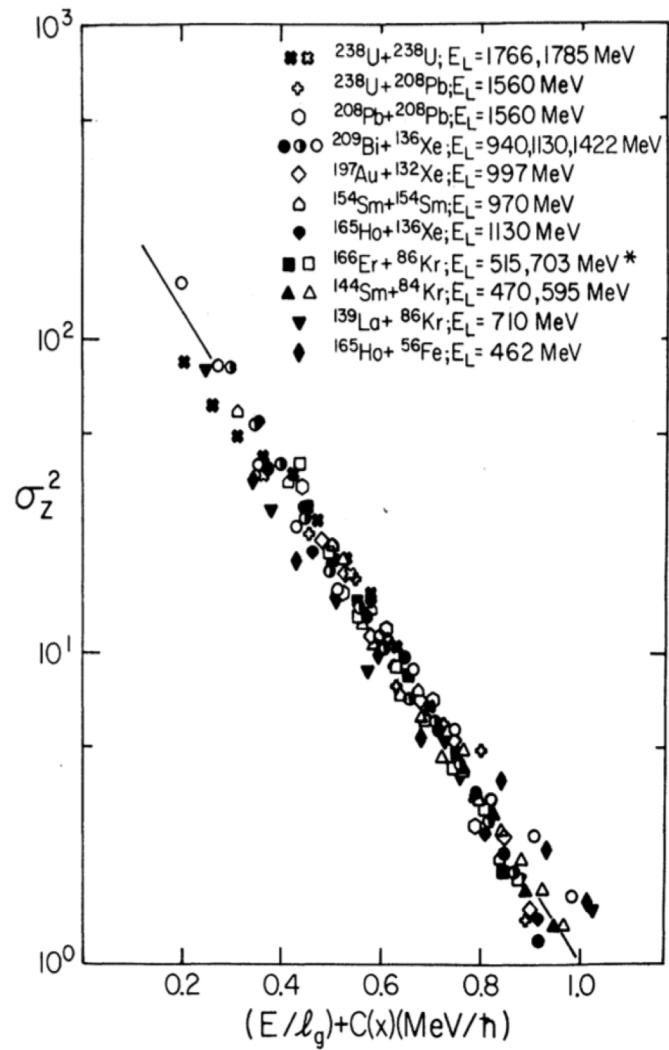


The grid - experimental centroids of the secondary charge and mass distributions for $A=92$ isobar in steps of 25 MeV excitation energy

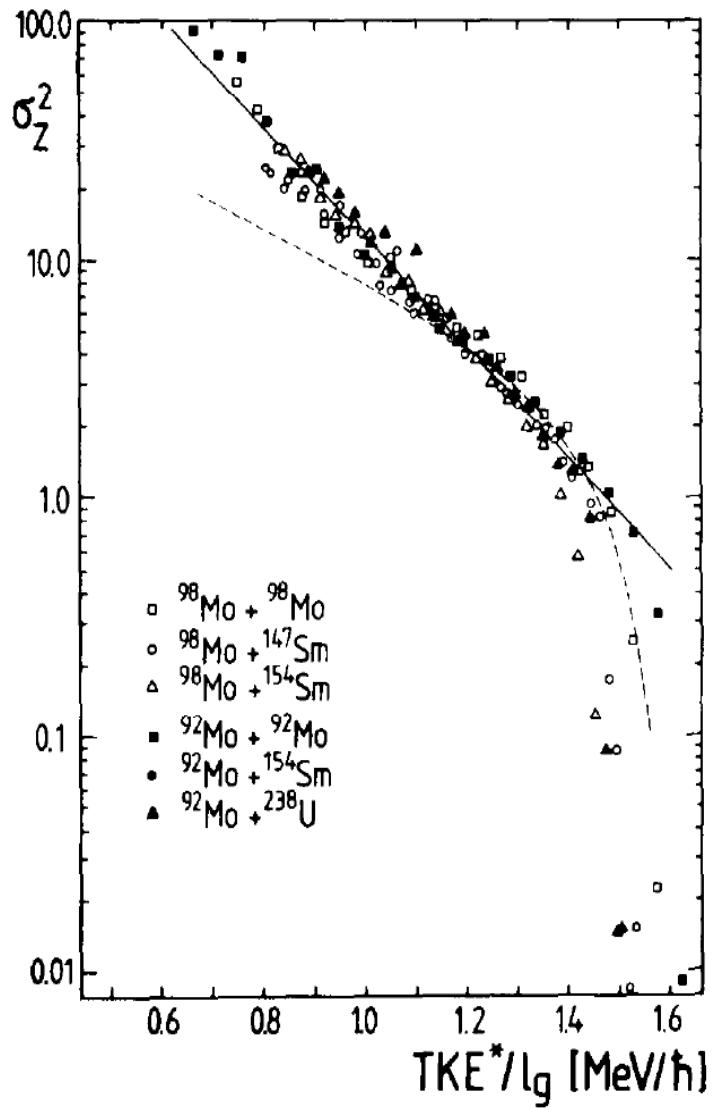
x & \bullet - centroids of the secondary N - Z distributions for $^{92}\text{Mo} + ^{154}\text{Sm}$ and $^{92}\text{Mo} + ^{238}\text{U}$, respectively

d – distance between the centre of mass of protons and neutrons

Heavy ion dissipative collisions (scaling)

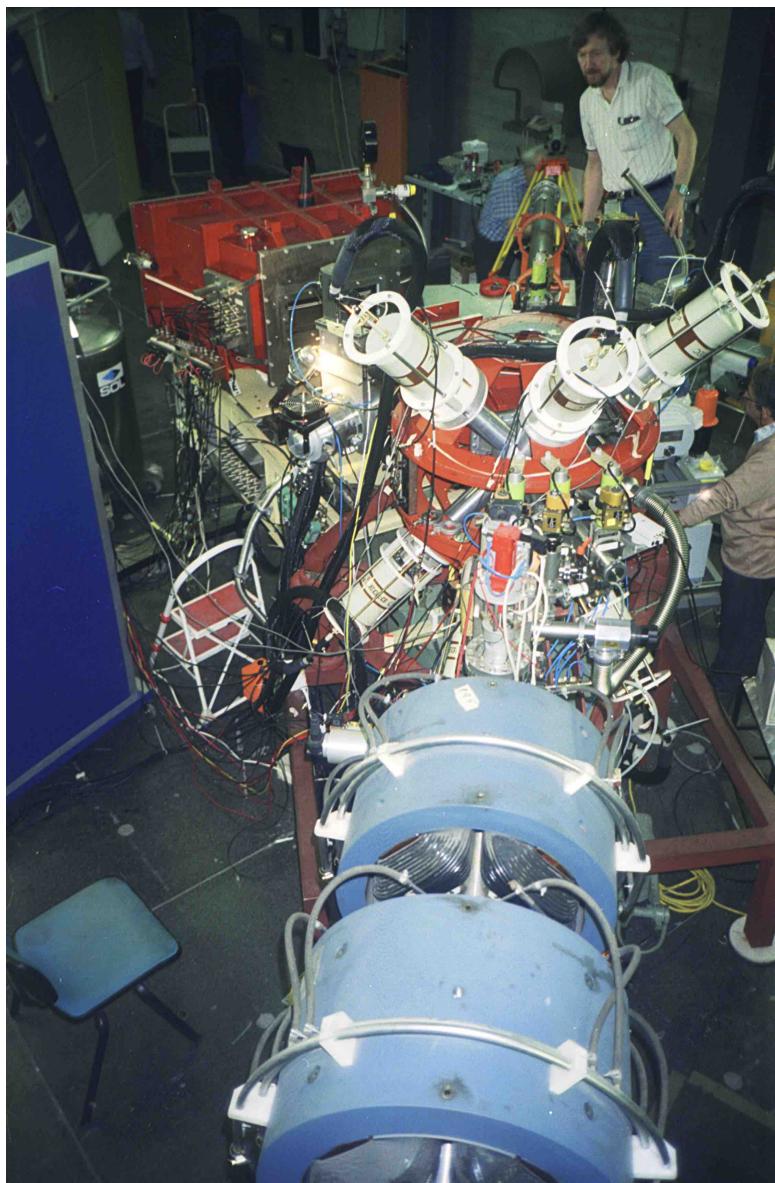


H.J.Wollersheim et al., Phys. Rev, C25(1982)338

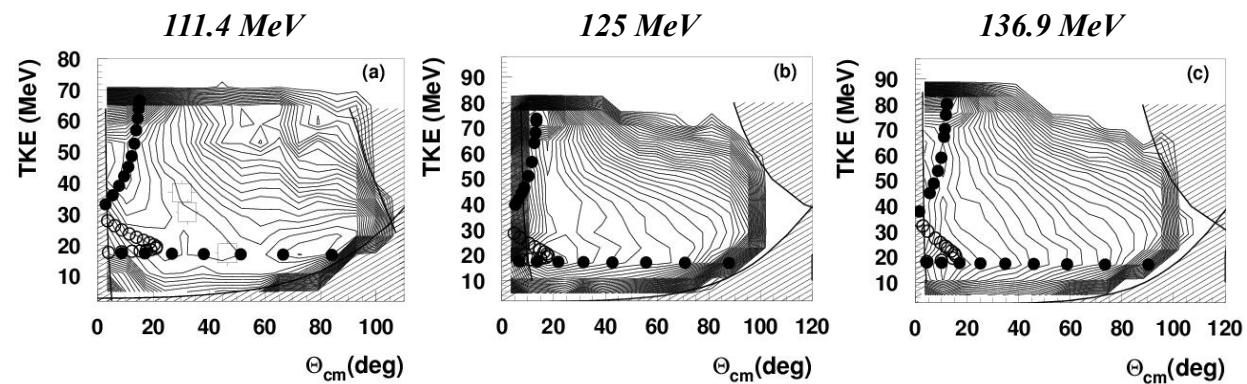


M. Petrovici et al., Nucl.Phys. A477(1988)277

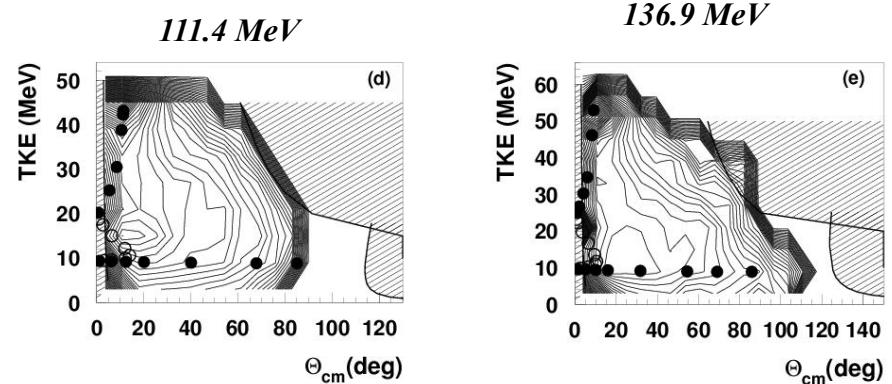
Dissipative collisions in light systems (scaling)



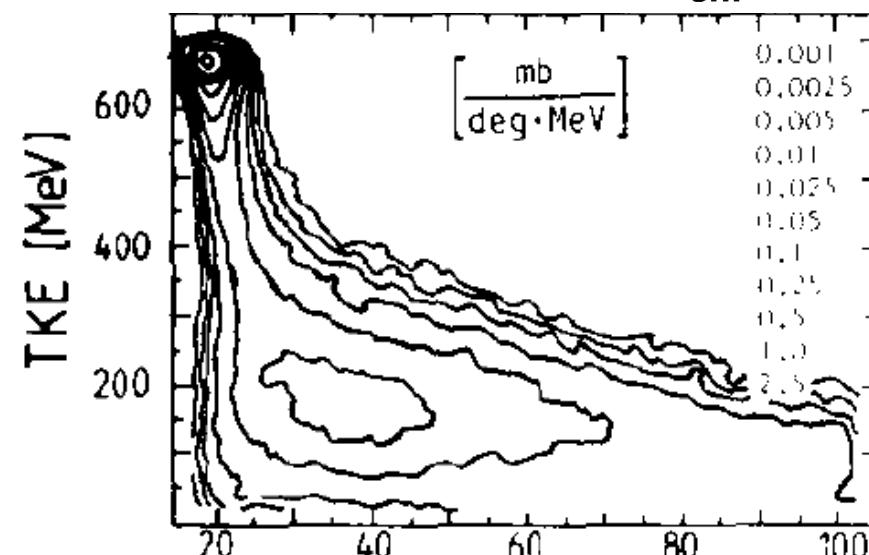
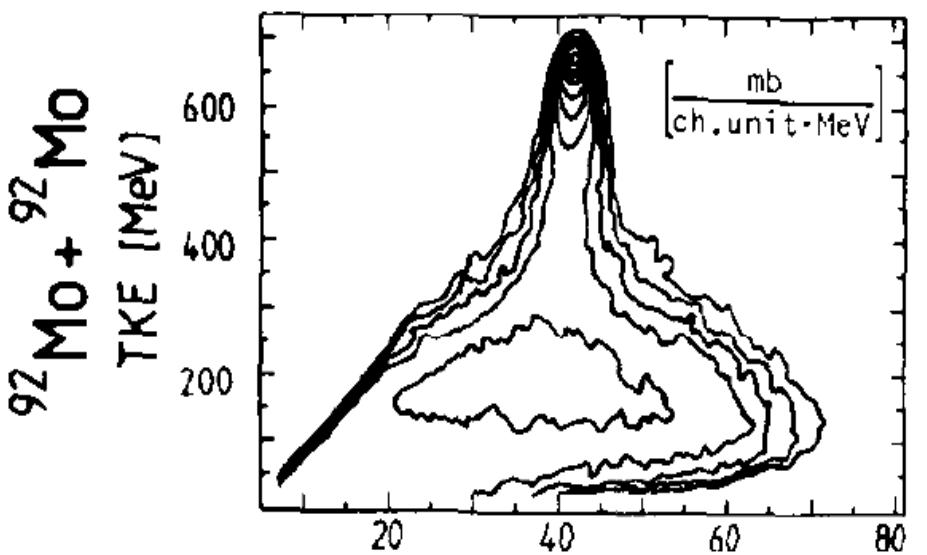
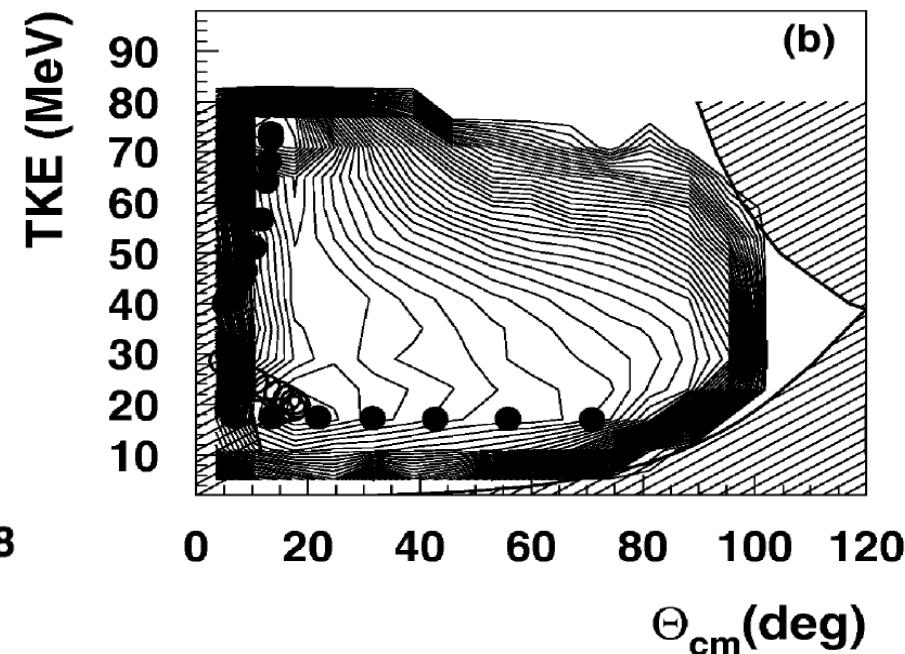
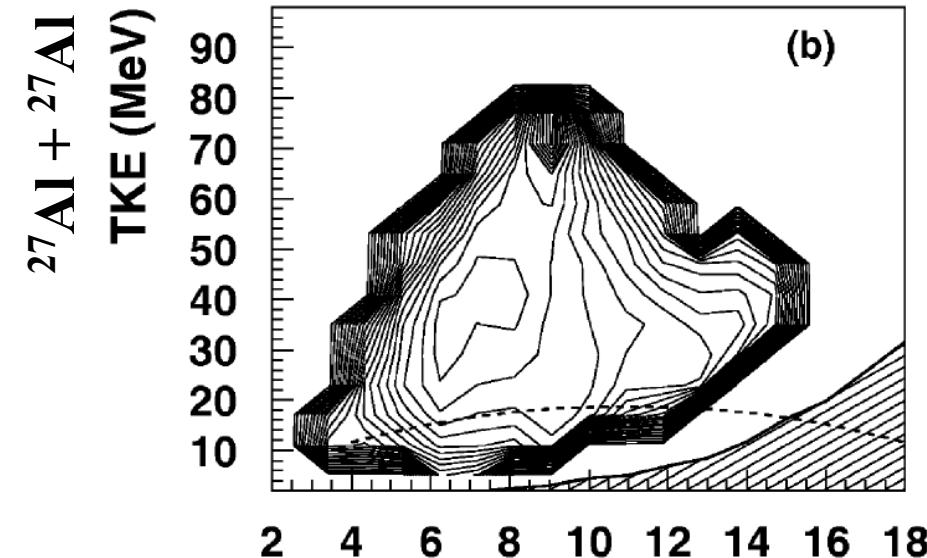
$^{19}F + ^{27}Al$ @ 111.4; 125 & 136.9 MeV



$^{19}F + ^{12}C$ @ 111.4 & 136.9 MeV



Similarities in Dissipative Processes



Similarities in Dissipative Processes

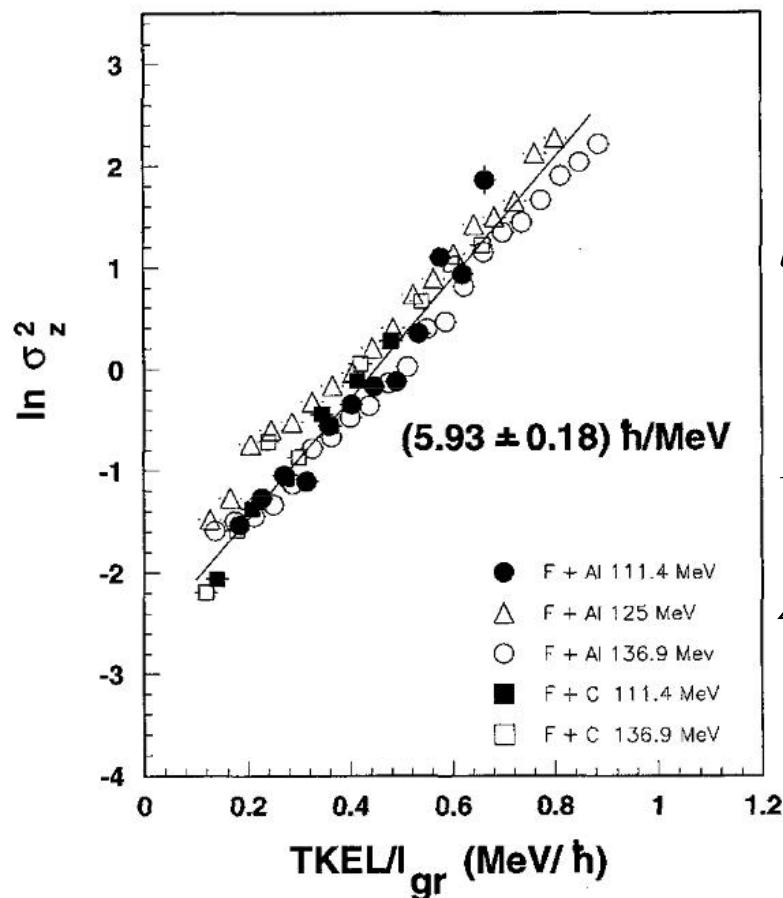
Charge variance systematic revisited

$^{19}\text{F} + ^{27}\text{Al}$ @ 111.5; 125 & 136.9 MeV

$^{19}\text{F} + ^{12}\text{C}$ @ 111.4 & 136.9 MeV

Phenomenological models predict a linear dependence of TKEL on the impact parameter

$$\Rightarrow t = t_0 \cdot \exp(s[TKEL/l_{gr} - \Delta/l_{gr}])$$

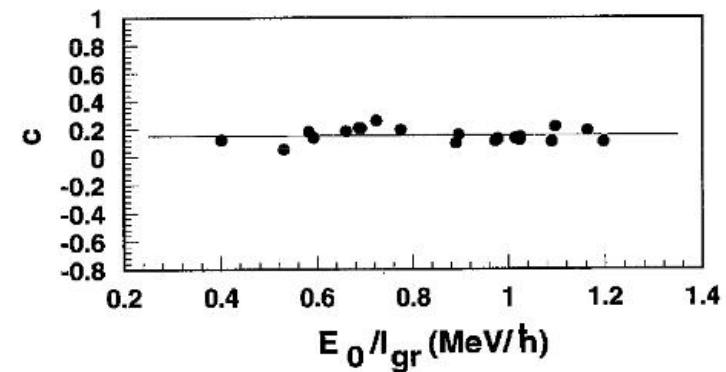
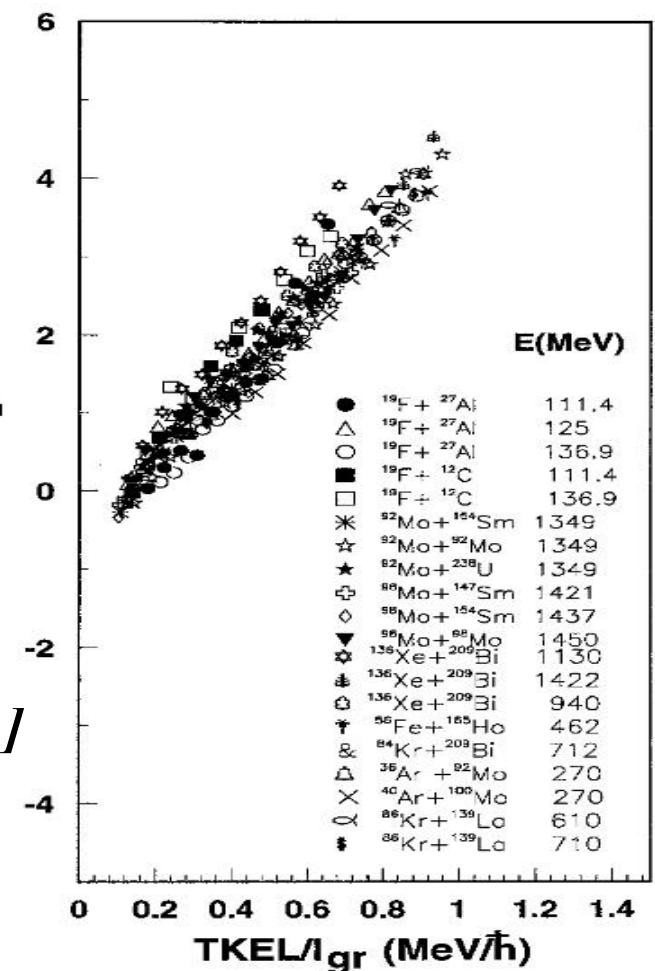


$$\ln[F\sigma_Z^2] = s[TKEL/l_{gr} - \Delta/l_{gr}]$$

$$F = s(m/\mu) \alpha(E_0/l_{gr})(A/Z)^2$$

$$\Delta = c \cdot l_{gr}$$

$$E_0 = E_{cm} - V_{coul}$$



Theoretical models

- Particle exchange picture based on Fermi gas with long mean free path

- J. Blocki et al., *Ann.Phys. (NY)* 113(1978)330
- J. Randrup, *Nucl.Phys.* A327(1979)490; A383(1982) 468
- H. Feldmeier, *Rep.Prog.Phys.* 50(1987)915
and ref. therein

- Time dependent Hartree-Fock model TDHF

- K.T.R. Devis et al., *Treatise on Heavy Ion Science*, ed. D.A. Bromley, vol.3,
Plenum Press N.Y. & London (1985)
- J.A. Marun et al., *Nucl.Phys.* A270(1976)471
- S.E. Koonin et al., *Phys.Rev. C15*(1977)1359
and ref. therein

- Landau-Vlasov - BUU

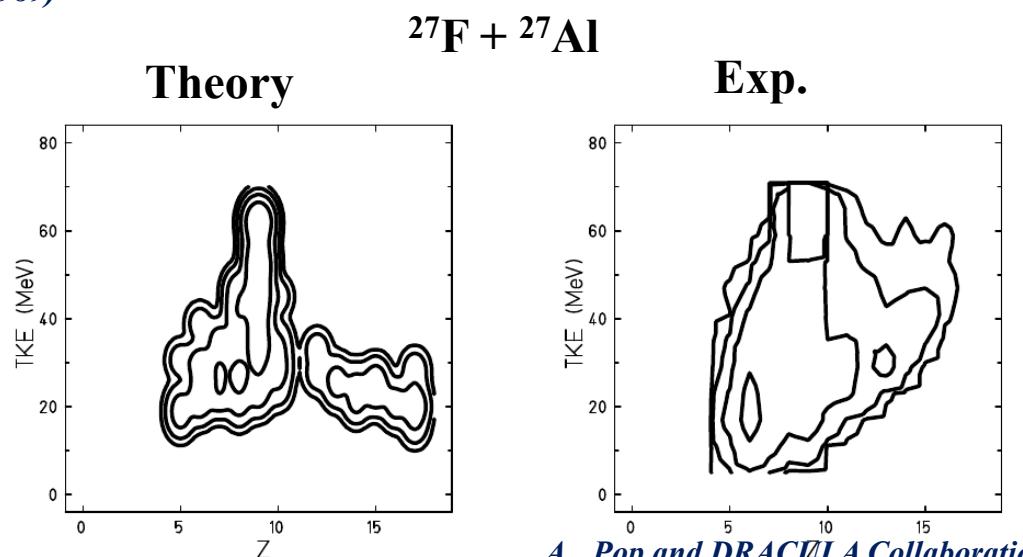
- G.F. Bertsch et al., *Phys.Rep.* (1988)189
- W. Bauer et al., *Phys.Rev. C34*(1986)2127
- A. Bonasera et al., *Proc. XXVII Winter Meeting Bormio* (1989)
and references therein

- QMD

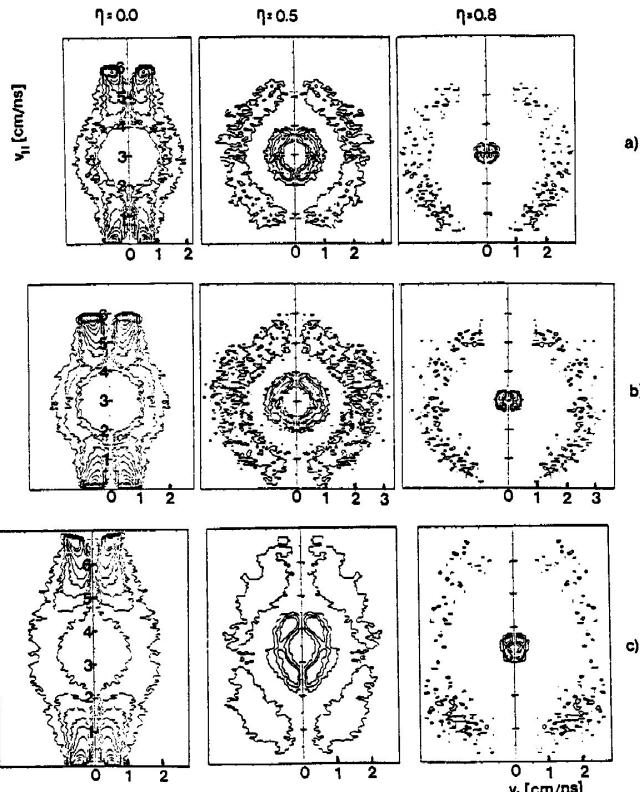
- J. Aichelin, *Phys.Rep.* 202(1991)233
and references therein

- FMD

- H. Feldmeier et al.,
Progress in Particle and Nuclear Physics 39(1997)393
and ref. therein



Incomplete Dissipative Processes - preequilibrium processes



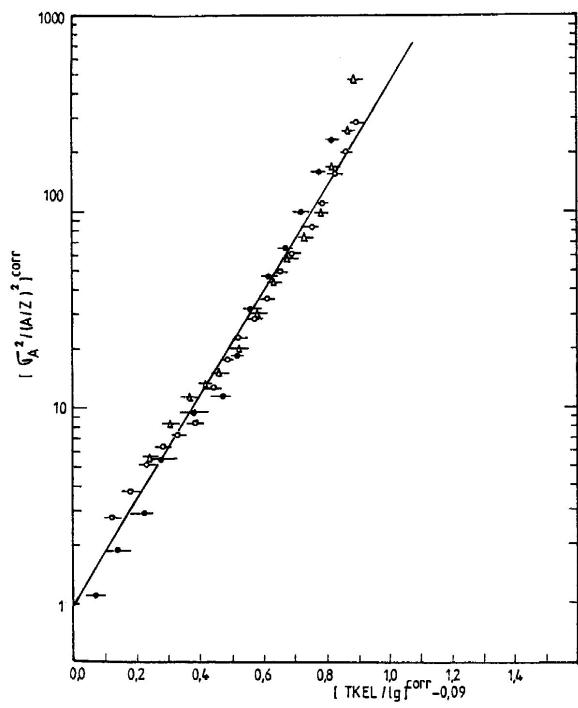
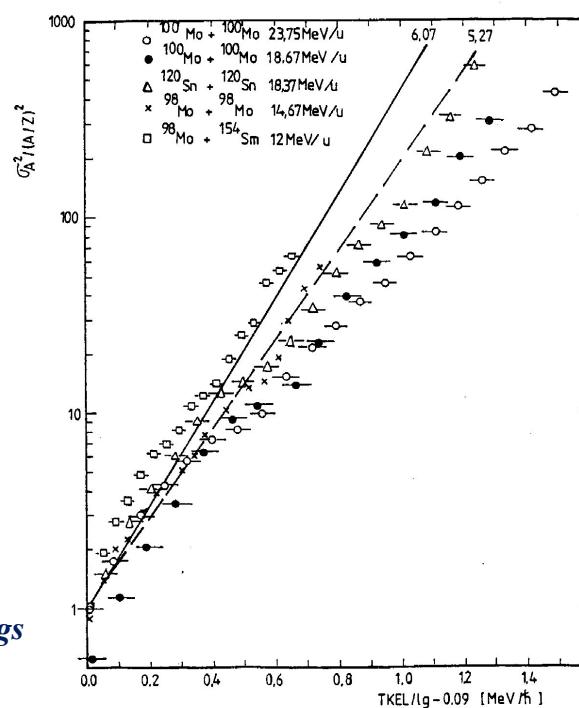
a) $^{100}\text{Mo} + ^{100}\text{Mo}$ at 18.67 MeV/u

b) $^{120}\text{Sn} + ^{120}\text{Sn}$ at 18.34 MeV/u

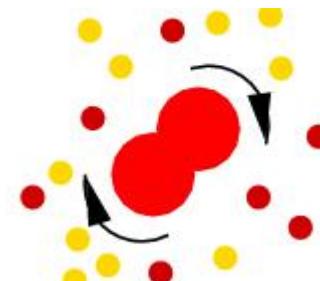
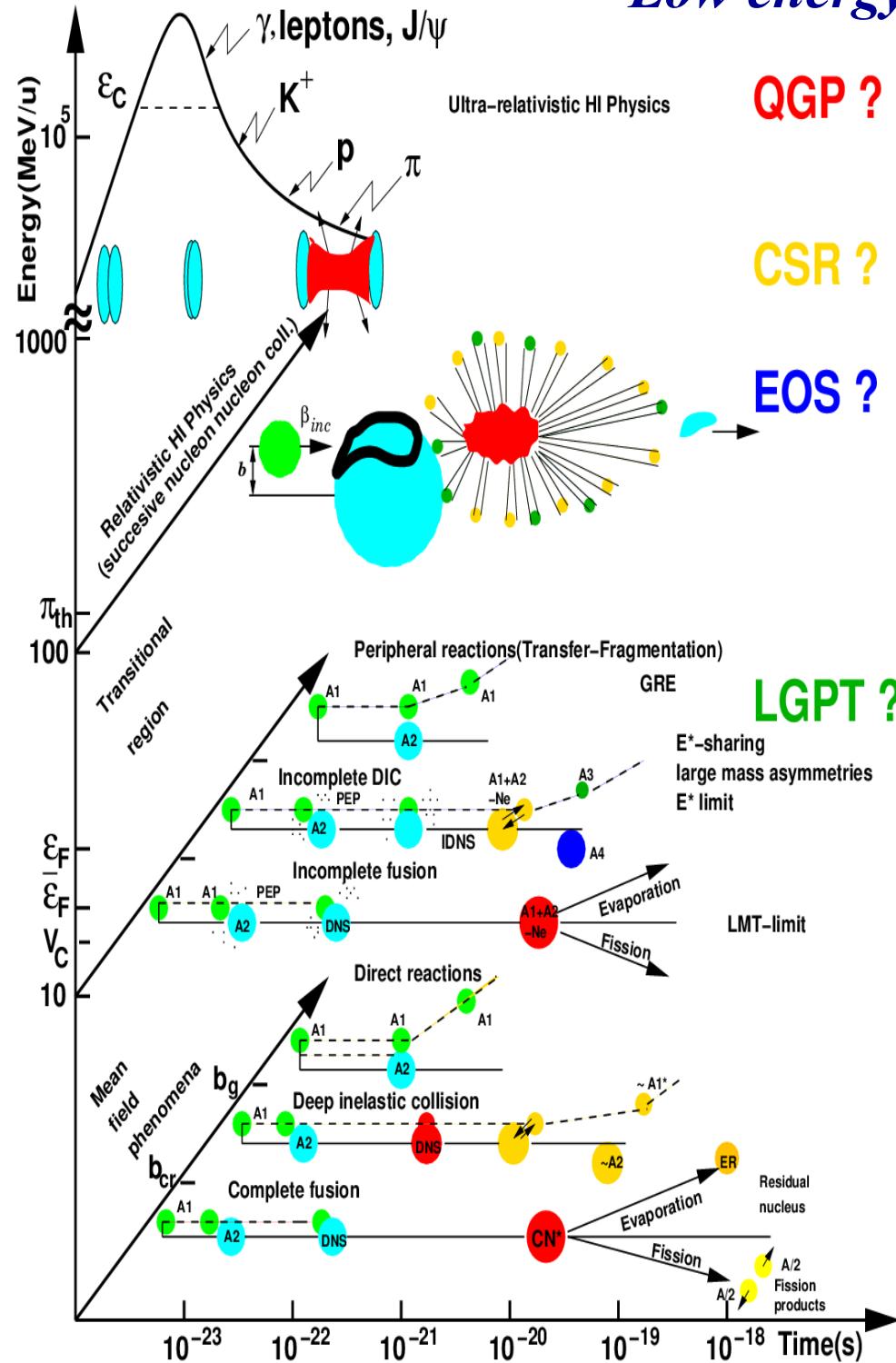
c) $^{100}\text{Mo} + ^{100}\text{Mo}$ at 23.75 MeV/u

➤ Incomplete deep inelastic processes in medium mass heavy ion collisions at 18 and 24 MeV/u
M.Petrovici – invited talk at International Symposium Nikko 1991 – „Towards a Unified Picture of Nuclear Dynamics”

➤ Fast particle emission in incomplete deep inelastic collisions
A. Pop, M. Petrovici
Rom. Jorn. of Phys. 38(1993)437
1993

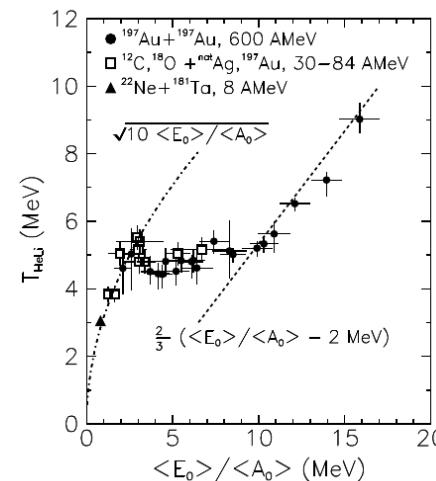
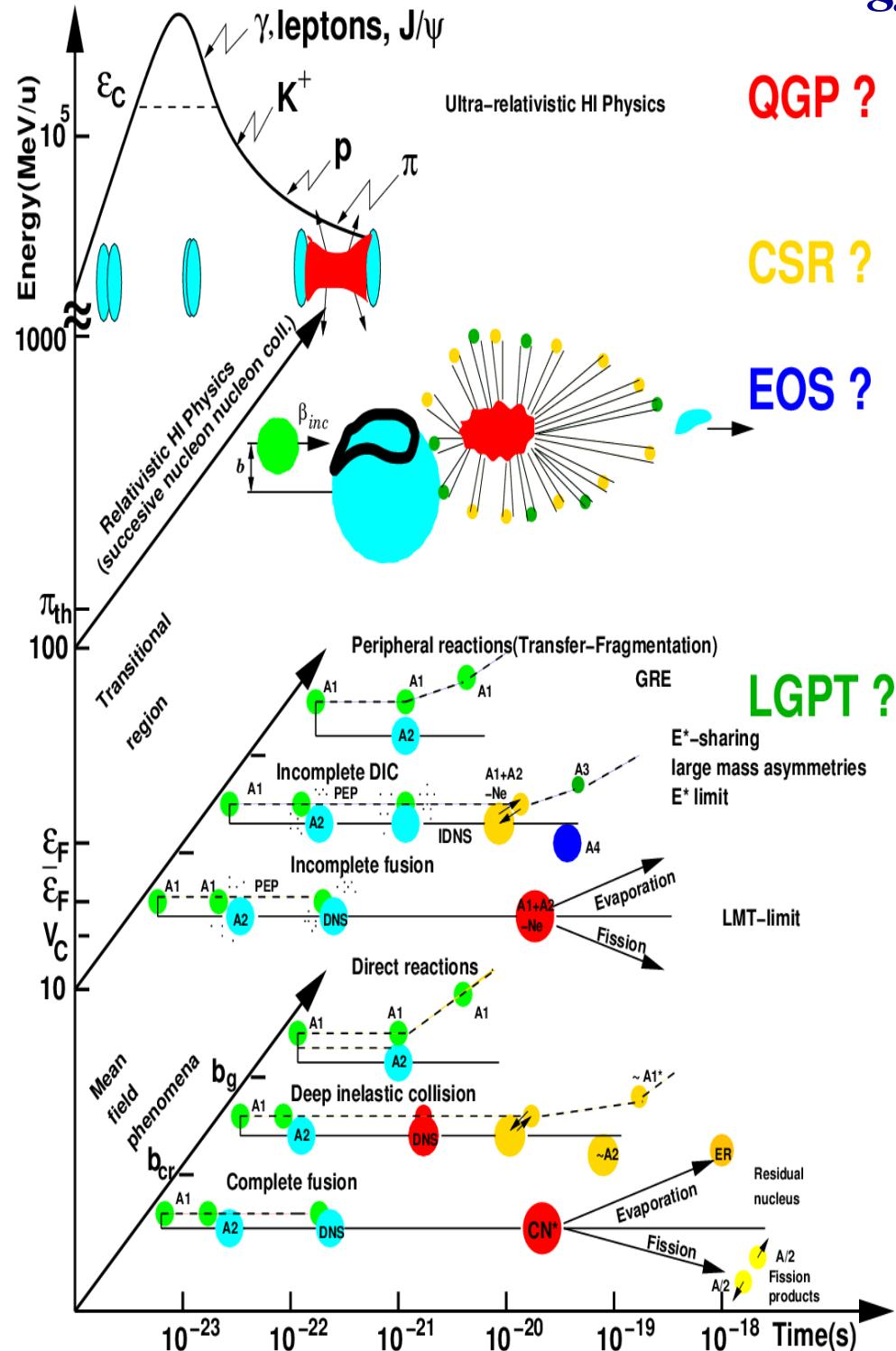


Low energy Heavy Ion Collisions

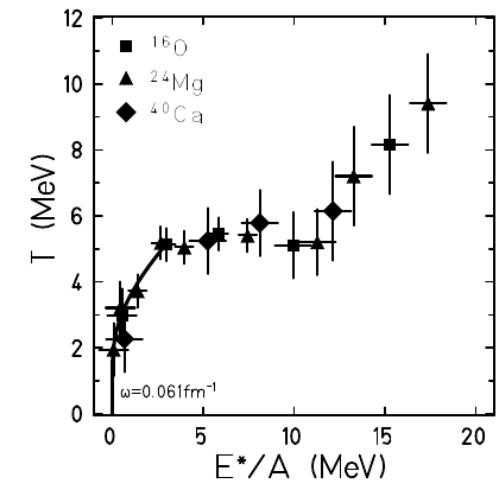


$< 100 \text{ A} \cdot \text{MeV}$

Low energy Heavy Ion Collisions

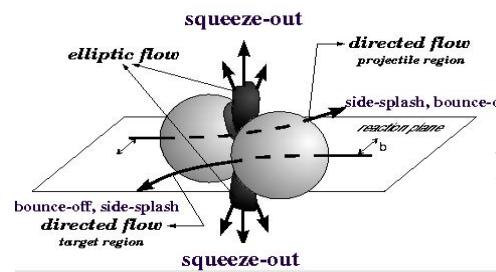
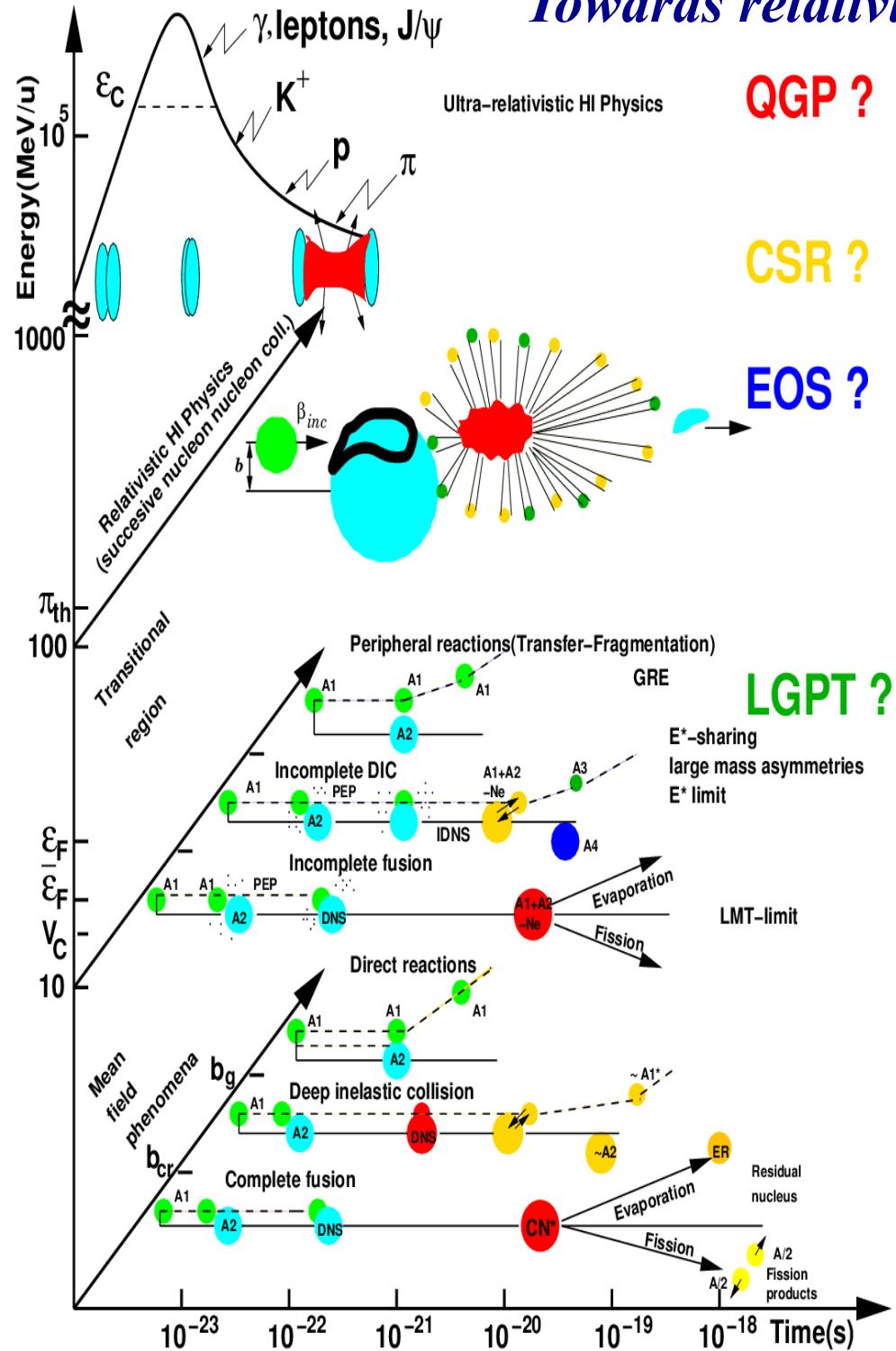


*J.Pochodzalla et al.,
arXiv:[nucl-ex]9607.004*



*H.Feldmeier et al.,
Prog. in Part. and Nucl. Phys.
39(1997)393*

Towards relativistic heavy ion collisions

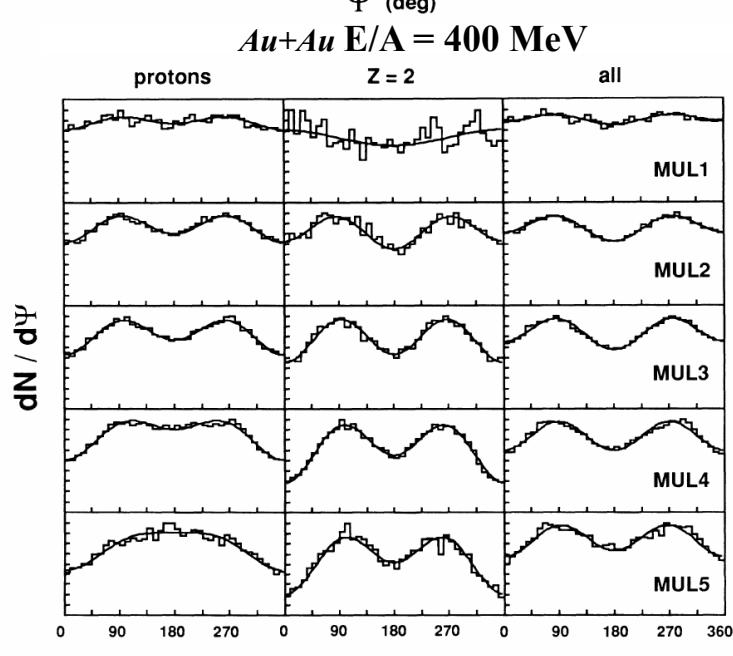
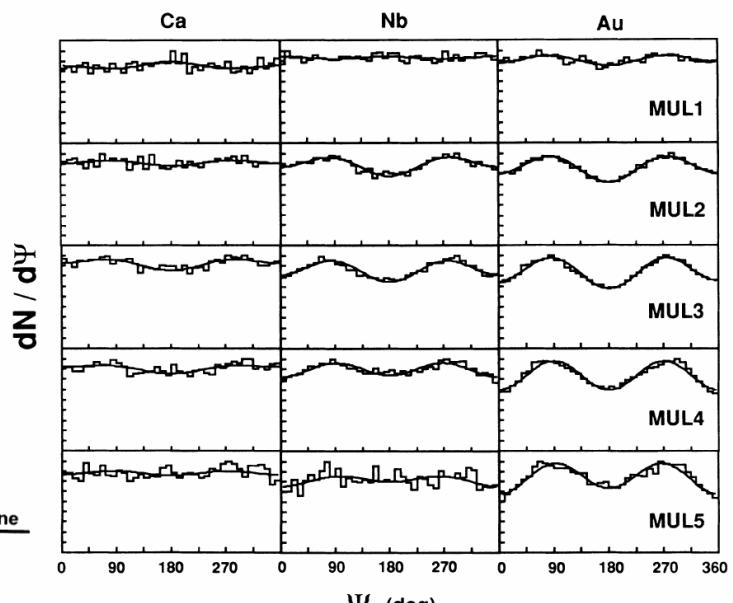
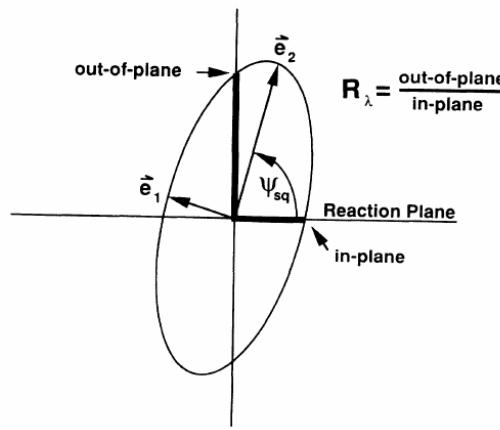
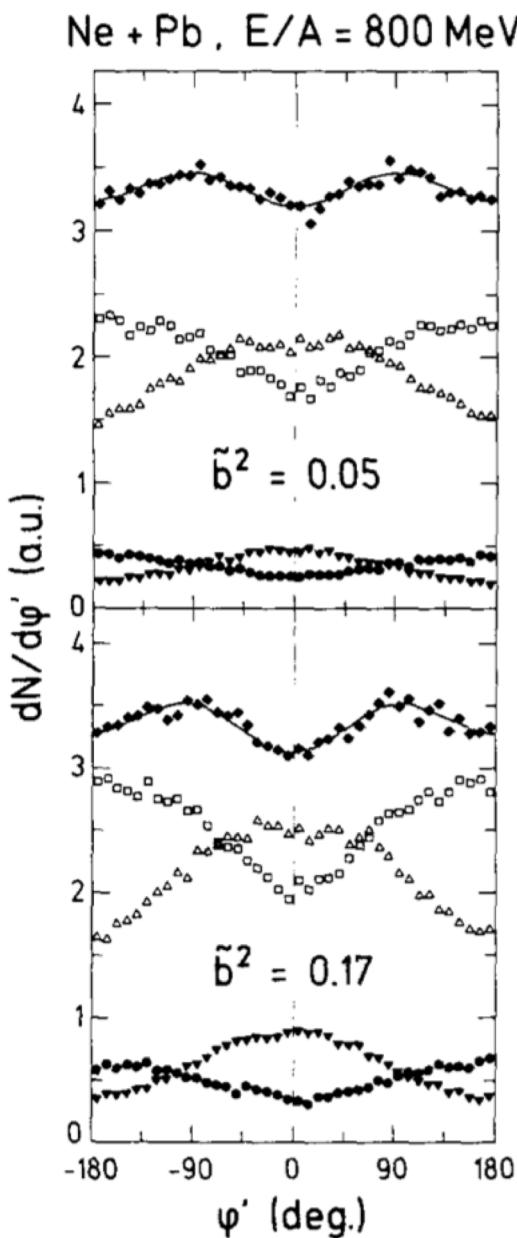


100 A•MeV - ~600 A•MeV

Towards relativistic heavy ion collisions

Azimuthal distributions

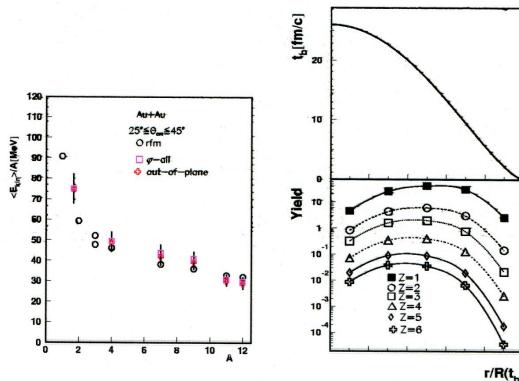
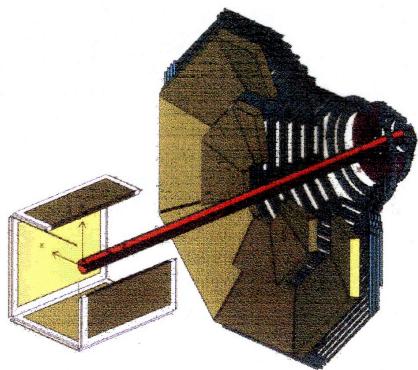
$E/A = 400 \text{ MeV}$



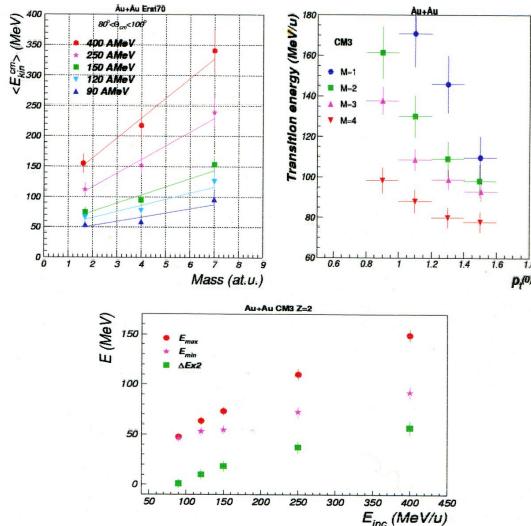
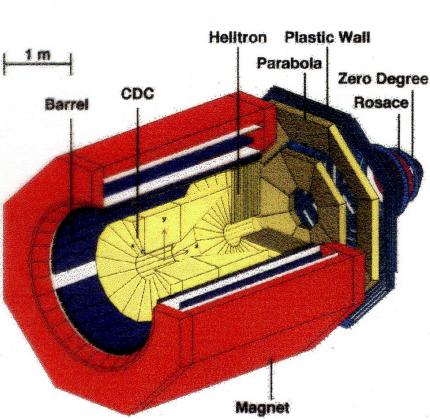
Towards relativistic heavy ion collisions

FOPI COLLABORATION

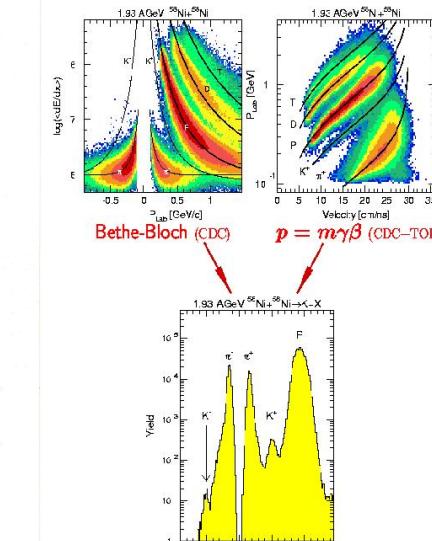
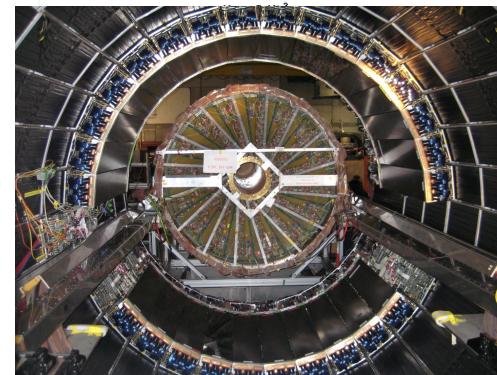
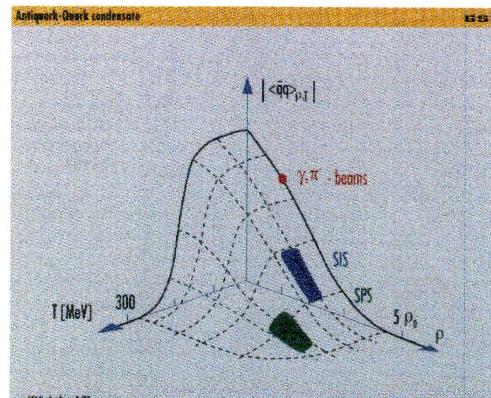
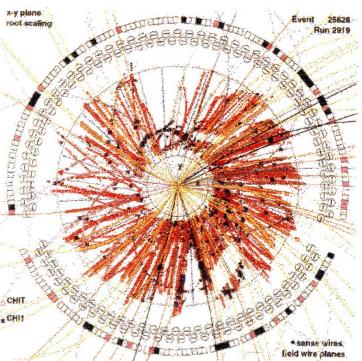
Phase I



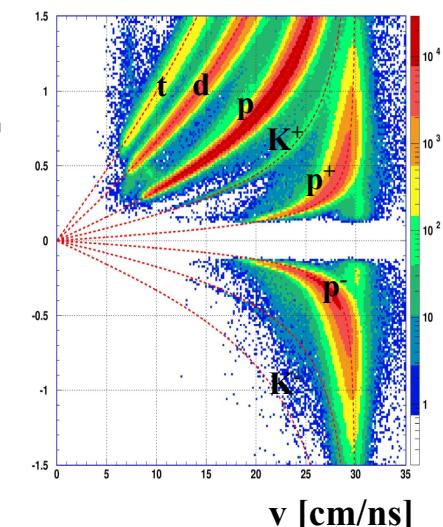
Phase II



Phase III



p [GeV/c]



v [cm/ns]

Radial expansion of compressed baryonic matter

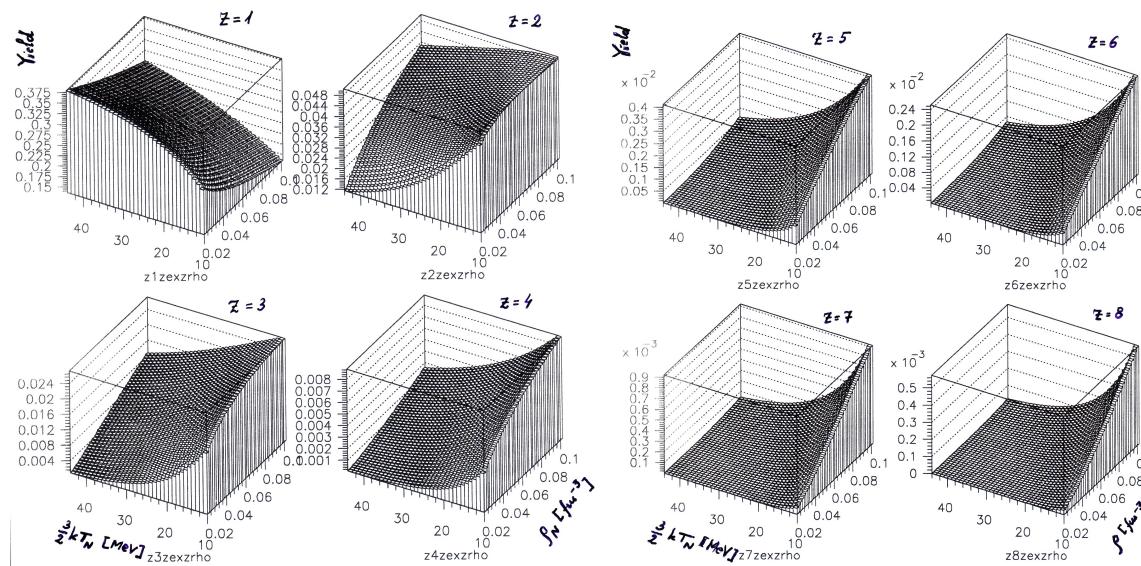
Semi analytical radial flow model
&
SM at break-up moment

M.Petrovici et al., Phys.Rev.Lett. 74(1995)5001

$$\text{RFM} \quad \left\{ \begin{array}{l} u_t + uu_r = -p_r/\rho \\ \rho_t + \rho_r u + \rho(u_r + 2u/r) = 0 \quad u = r \cdot R/\dot{R} \\ (\delta/\delta t + u \delta/\delta r)(p\rho^{-\gamma}) = 0 \quad x = r/R \end{array} \right.$$

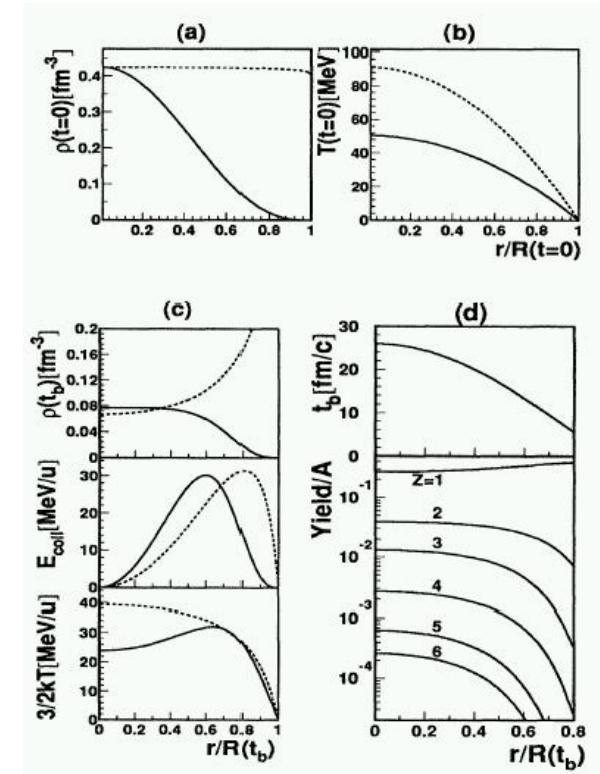
SM

G.Fai et al., Comp.Phys.Com. 42(1986)385



L.I.Sedov, Similarity and
Dimensional Methods in Mechanics

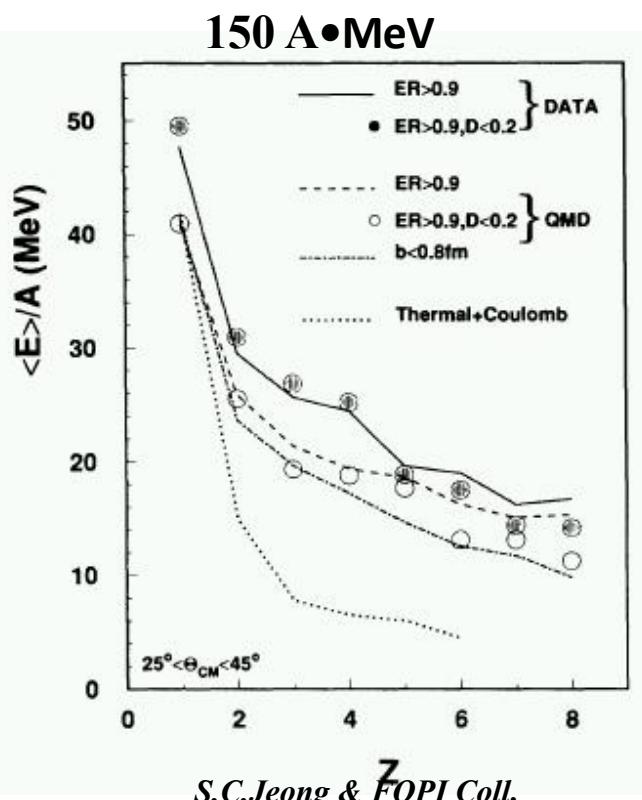
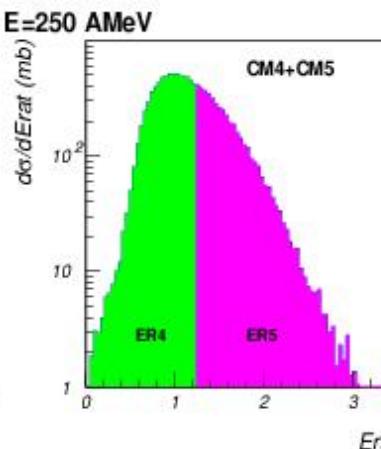
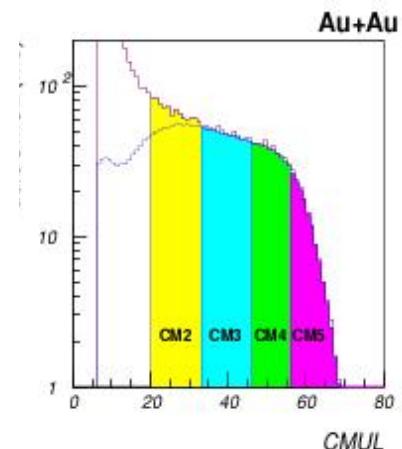
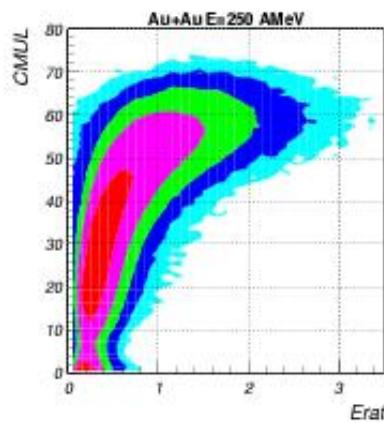
J.P.Bondorf et al., Nucl.Phys. A296(1978)320



Radial expansion of compressed baryonic matter

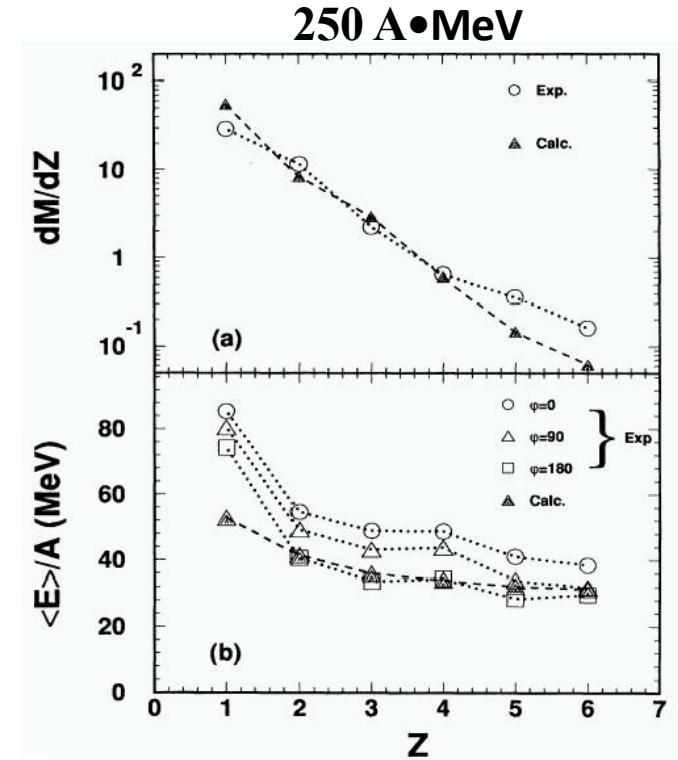
Highly central Au + Au collisions

$$E_{rat} = \sum_i \frac{E_{\perp,i}}{E_{\parallel,i}}$$



S.C.Jeong & FOPI Coll,
Phys.Rev.Lett. 72(1994)3468

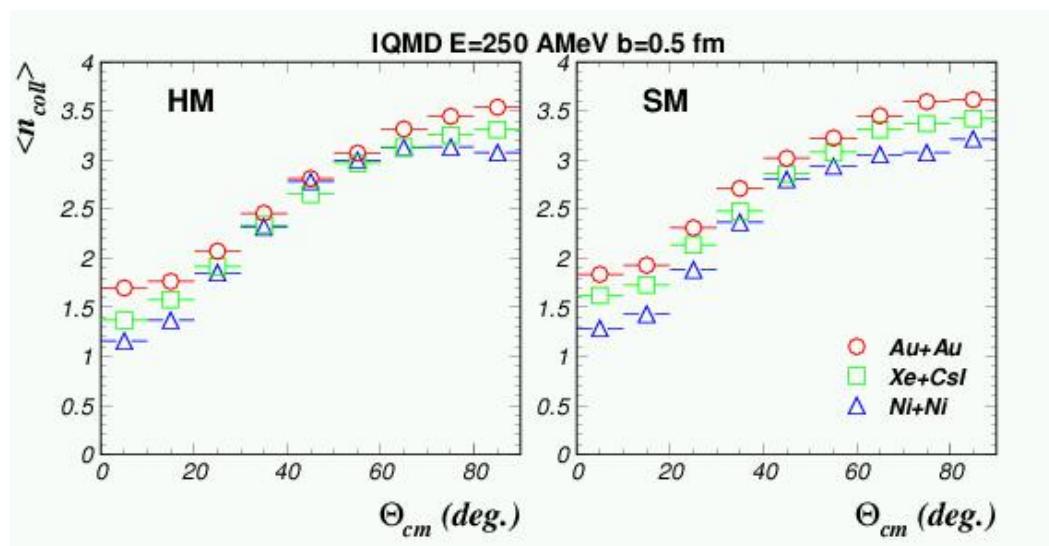
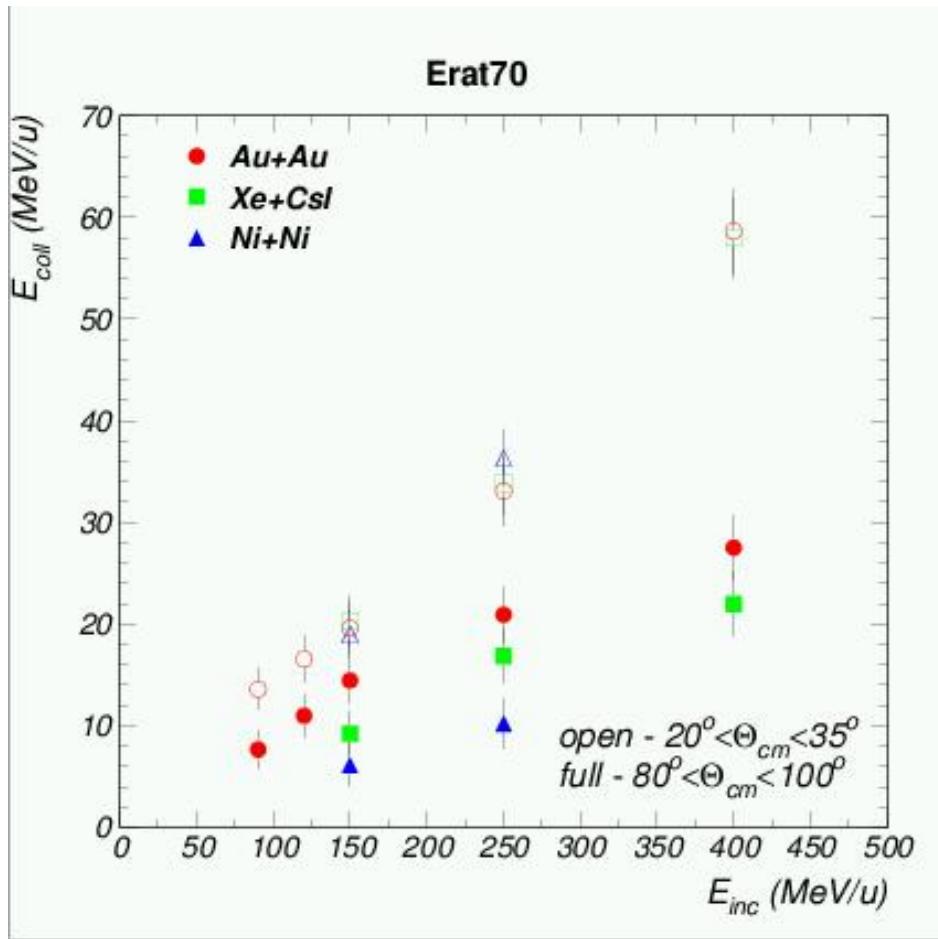
$$\langle E_{kin}^{cm} \rangle \approx \frac{1}{2} m_0 \langle \beta_{flow}^2 \rangle A_{IMF} + \frac{3}{2} T''$$



M.Petrovici & FOPI Coll,
Phys.Rev.Lett. 74(1995)5001

Radial expansion of compressed baryonic matter

Highly central A-A collisions

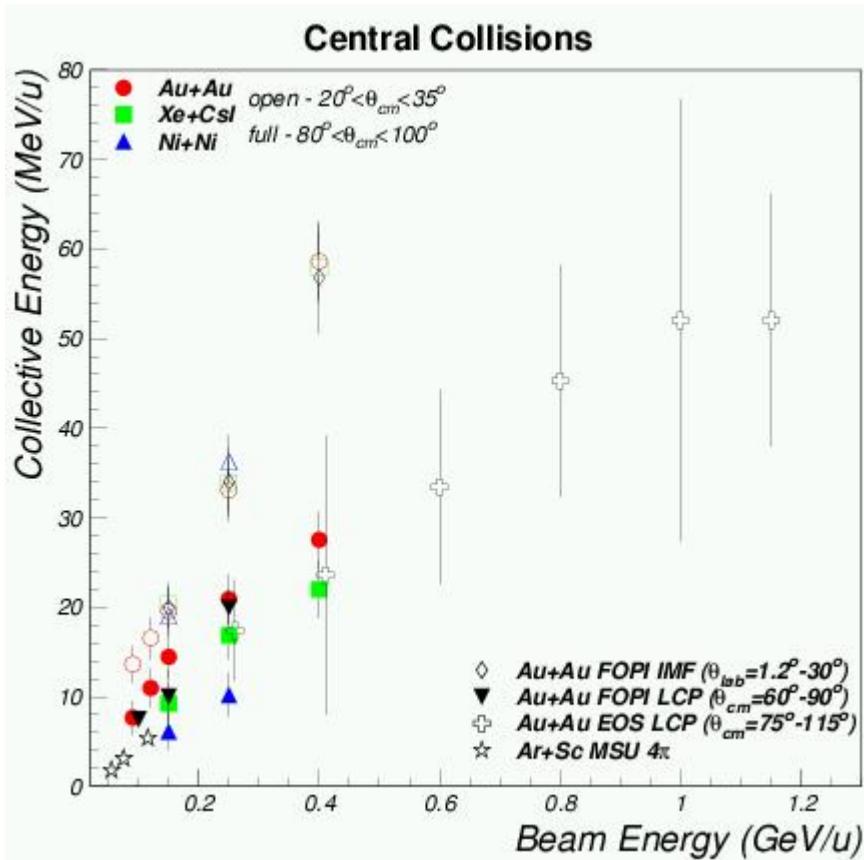


M.Petrovici, "Exotic Nuclei and Nuclear/Particle Astrophysics",

AIP Conf.Proc. 972(2004)072303

A.Andronic PhD Thesis

Compilation of different experimental results central collisions



$$\langle T_i \rangle = (\langle \gamma_F \rangle - 1) A_i m_0 + \langle \gamma_F \rangle \langle T_i \rangle_{un}$$

$$\langle T_i \rangle \approx \frac{1}{2} A_i m_0 \langle \beta_F^2 \rangle + \frac{3}{2} \tau$$

$$\frac{dN}{dE} \sim p \exp^{-\gamma E/T} \left\{ \frac{\sinh \alpha}{\alpha} (\gamma E + T) - T \cosh \alpha \right\}$$

$$\gamma = (1 - \beta^2)^{-1/2}, \alpha = \gamma \beta p/T$$

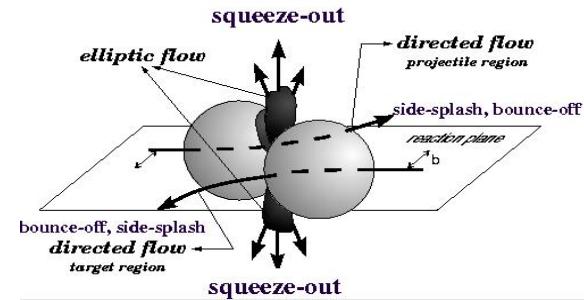
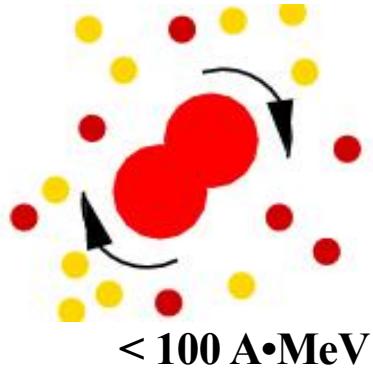
EOS – M.A.Lisa & EOS Coll., PRL 75(1995)2662

MSU - R.Pak et al., PRC 54(1996)1681

A.Andronic PhD Thesis

Azimuthal distributions

What should be expected as a function of incident energy ?

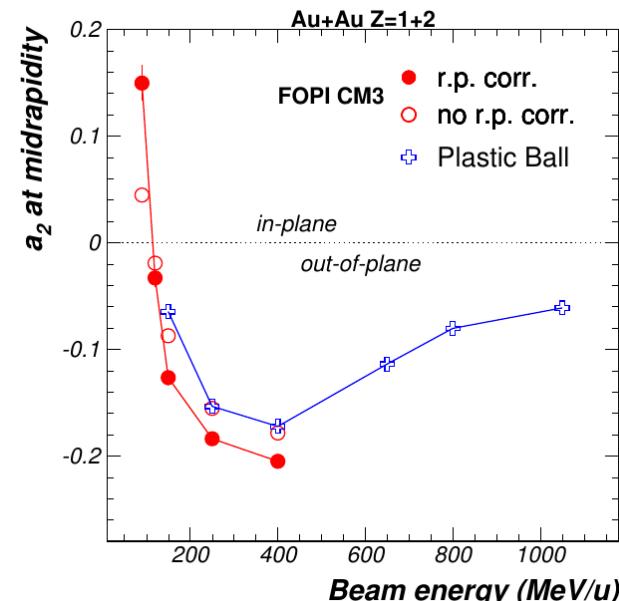
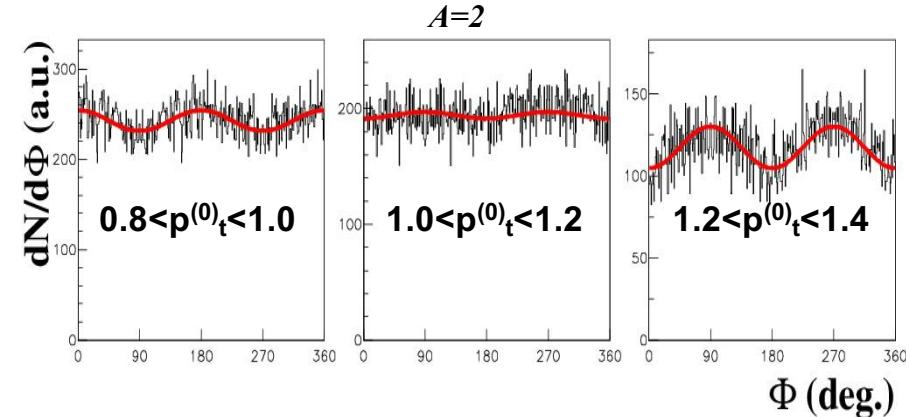


$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} \left(1 + \sum_{n=1}^{\infty} 2v_n \cos(n(\phi - \Psi_r)) \right)$$

$$v_2 = \langle \cos 2(\phi - \Psi_r) \rangle, \quad \phi = \tan^{-1} \left(\frac{p_y}{p_x} \right)$$

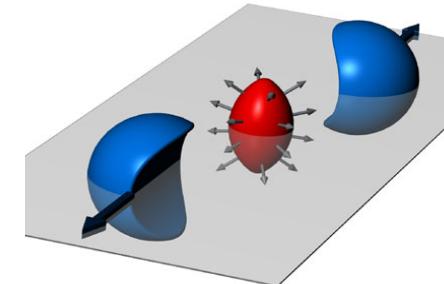
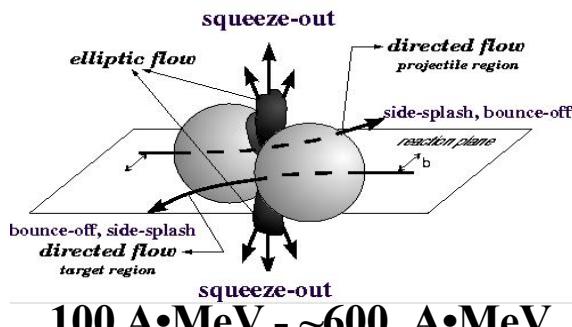
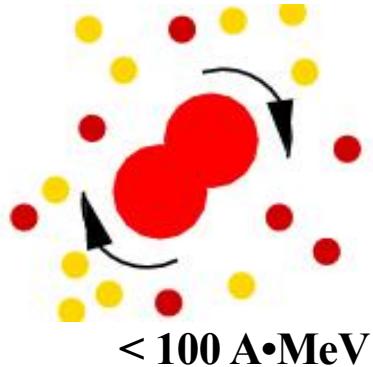
The experimental evidences

Au+Au 120 Mev/u, CM3



Azimuthal distributions

What should be expected as a function of incident energy ?

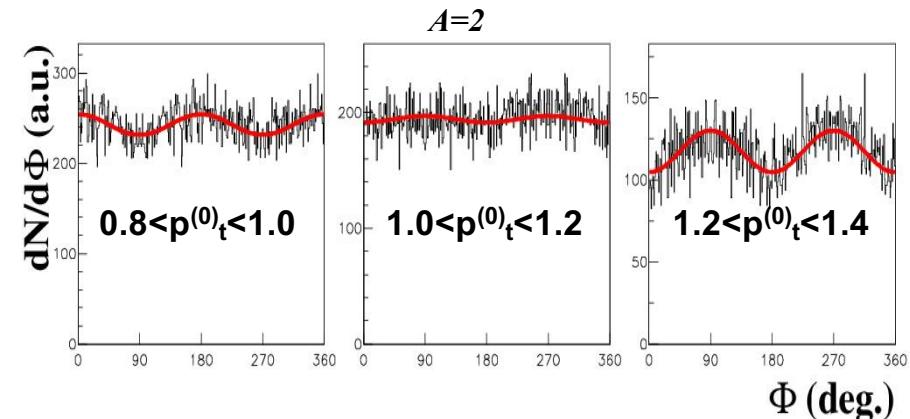


$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} \left(1 + \sum_{n=1}^{\infty} 2v_n \cos(n(\phi - \Psi_r)) \right)$$

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The experimental evidences

Au+Au 120 Mev/u, CM3



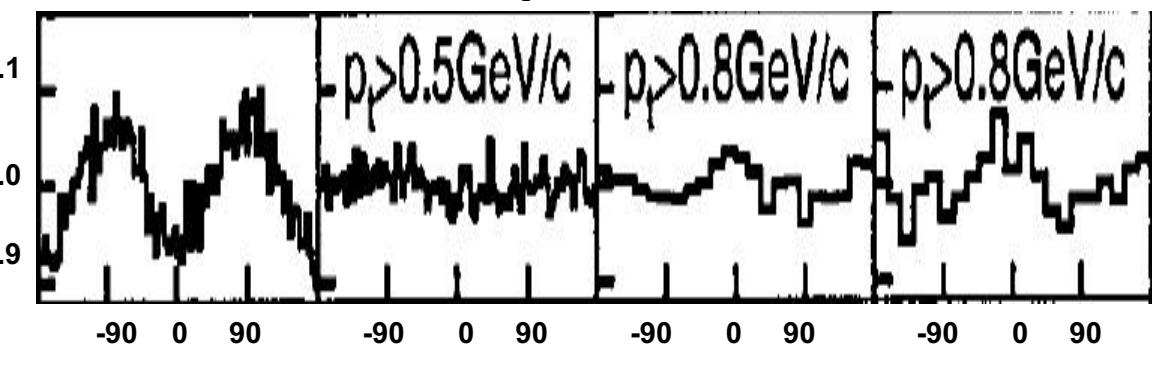
2 A·GeV

4 A·GeV

6 A·GeV

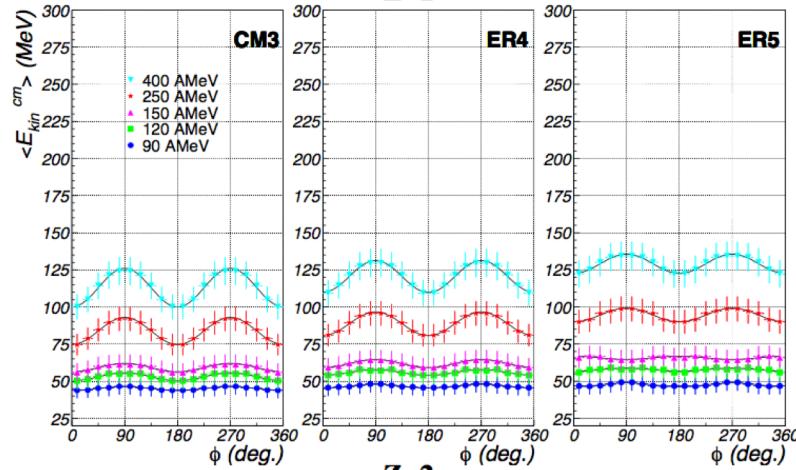
8 A·GeV

protons

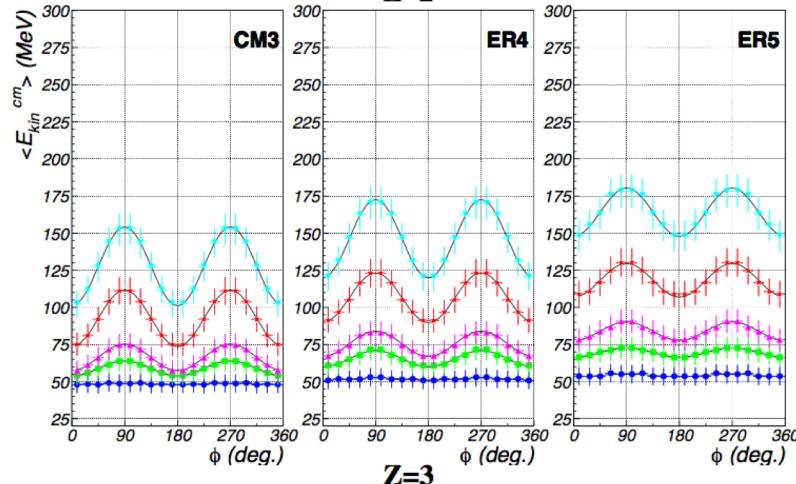


Mean kinetic energy azimuthal distributions

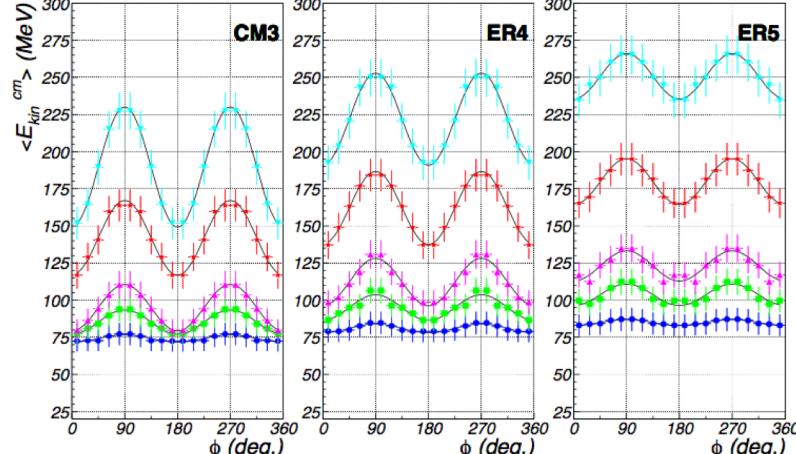
Z=1



Z=2



Z=3

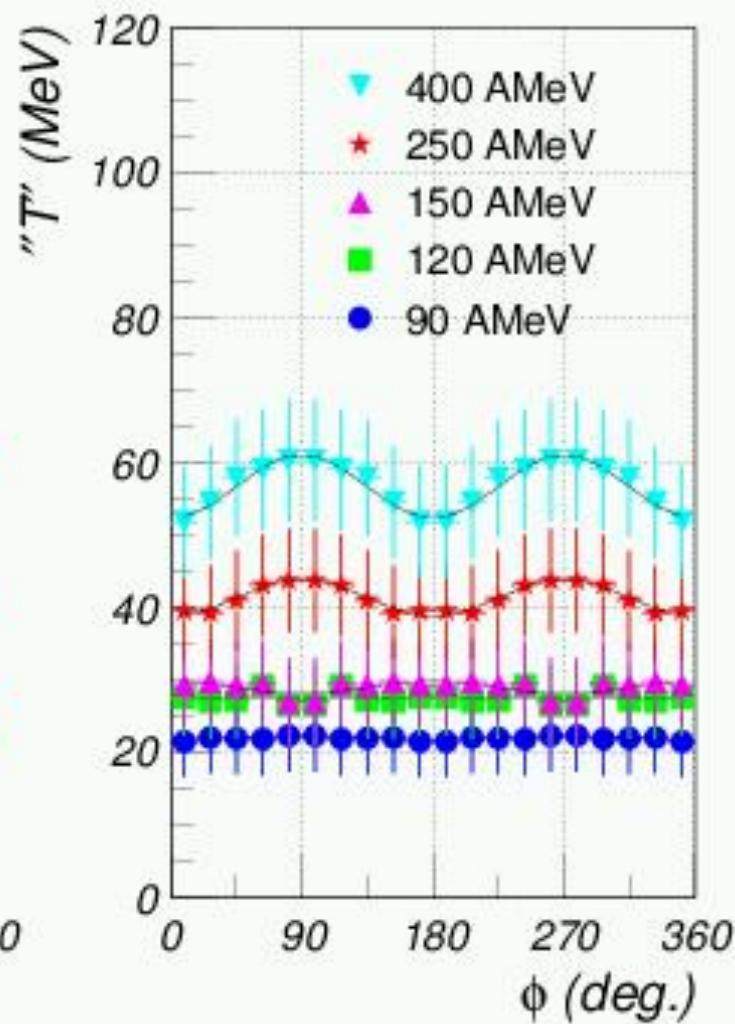
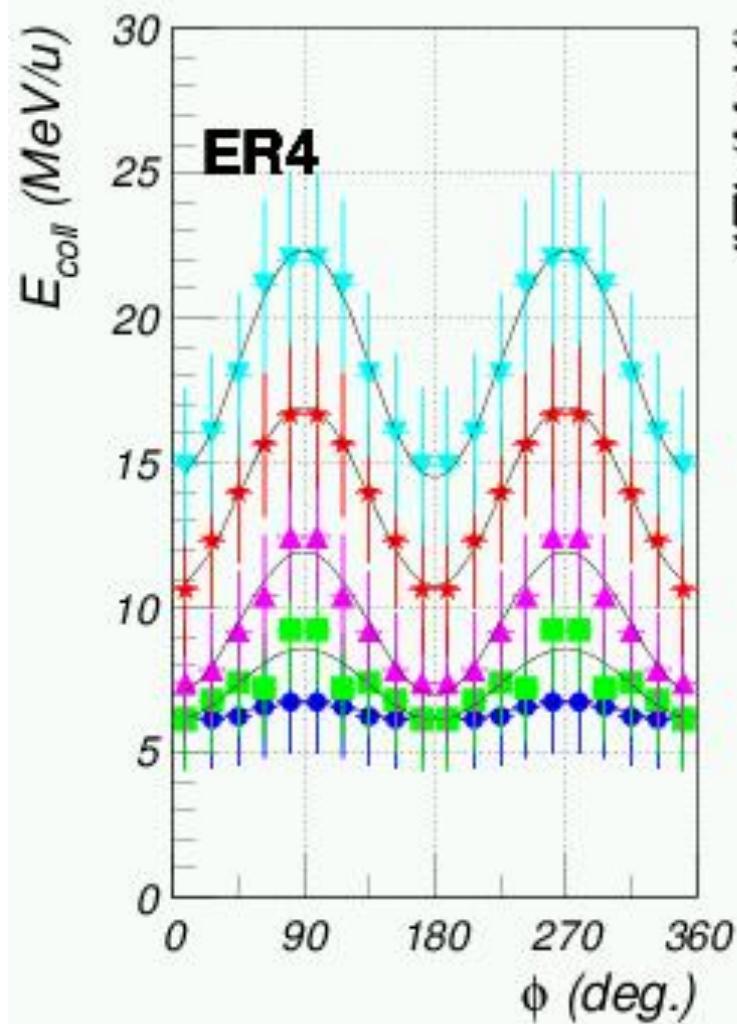


$$\langle E_{kin}^{cm} \rangle \approx \frac{1}{2} m_0 \langle \beta_{flow}^2 \rangle A_{IMF} + \frac{3}{2} "T"$$

$$E_{coll} = \frac{1}{2} m_0 \langle \beta_{flow}^2 \rangle$$

G.Stoicea, M.Petrovici & FOPI Phys.Rev.Lett. 92(2004)072303
G.Stoicea PhD Thesis

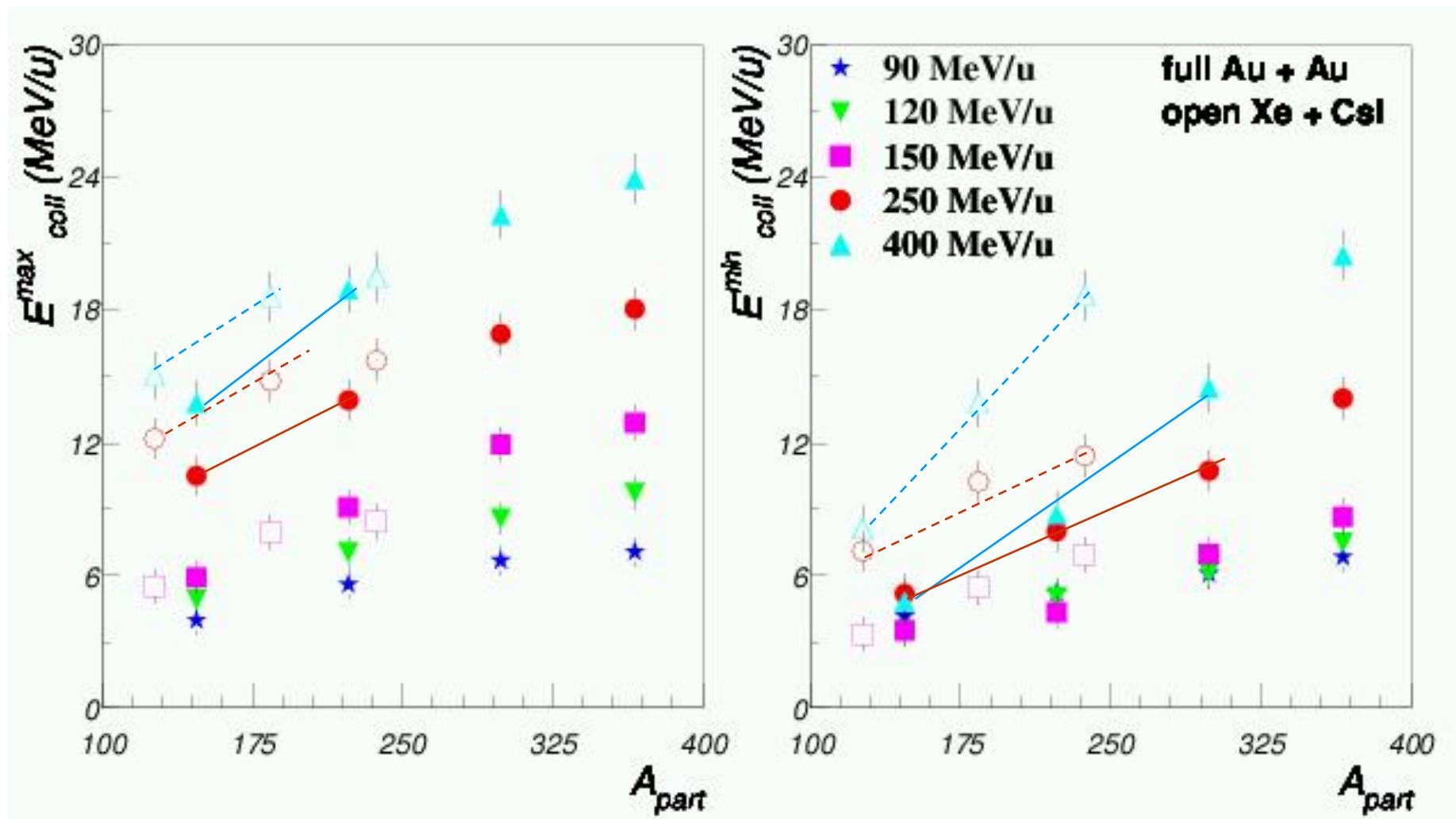
E_{coll} & "T" azimuthal distributions



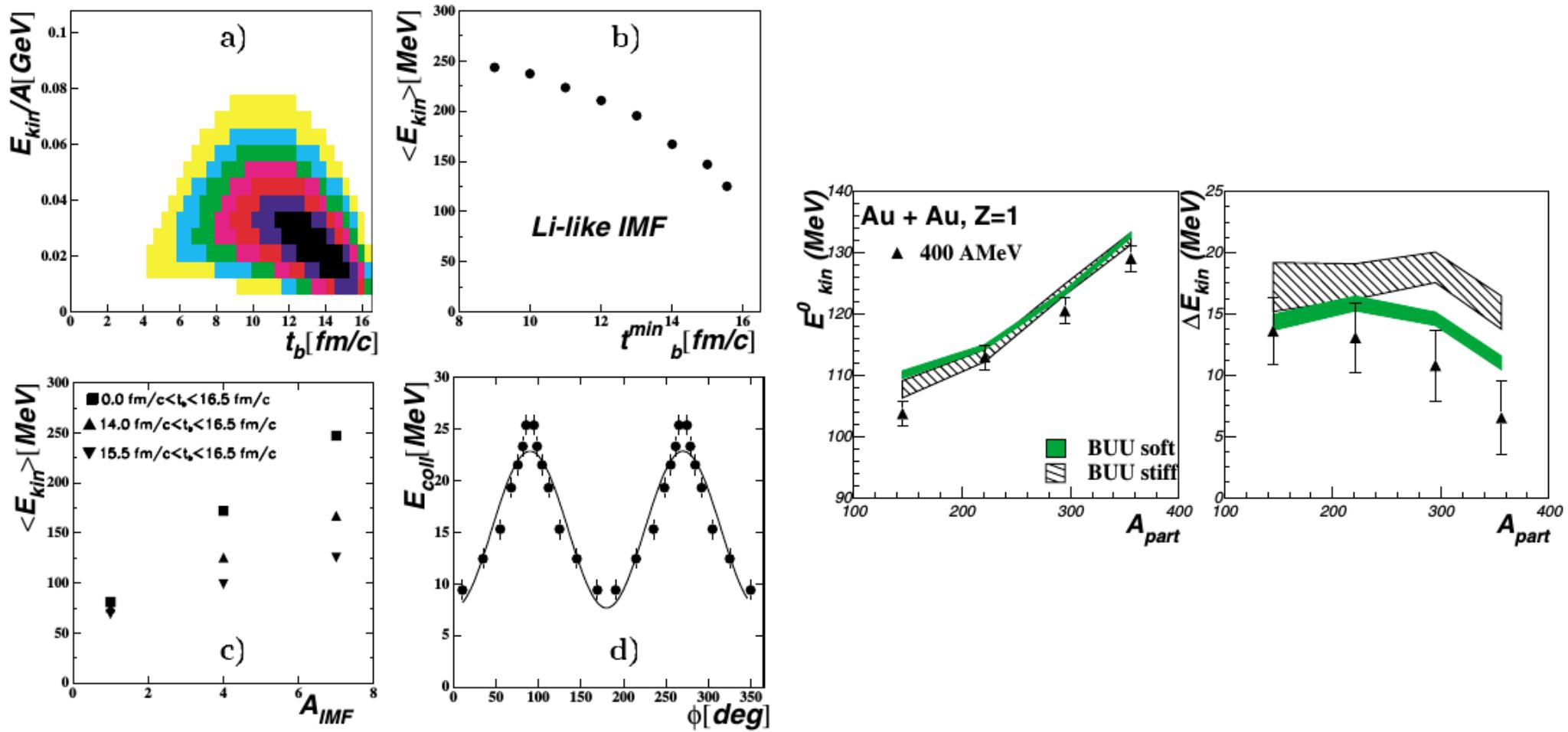
$$E_{coll} = E_{coll}^0 - \Delta E_{coll} \cdot \cos 2\Phi$$

$$"T" = "T"_0 - \Delta "T" \cdot \cos 2\Phi$$

Fireball shape & shadowing effects at SIS18



Shadowing effects - EoS



M.Petrovici et al., Phys.Rev.Lett. 74(1995)5001

G.Stoicea, M.Petrovici & FOPI Coll., Phys.Rev.Lett. 92(2004)072303

P.Danielewicz, Nucl.Phys. A6873(2000)375 and ref. therein

Expectations based on QCD

QCD – non-Abelian gauge theory & asymptotic freedom

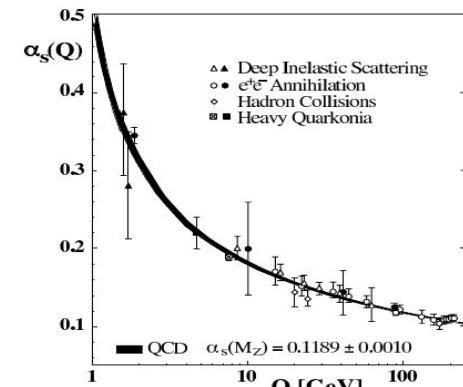
D.J.Gross, H.D.Politzer and F.Wilczek - Nobel Prize 2004

QCD - running coupling constant $\alpha_s(Q^2) = \frac{\alpha_s(\mu^2)}{1 + \frac{\alpha_s(\mu^2)}{12\pi}(33 - 2n_f)\log(Q^2/\mu^2)}$

QCD – intrinsic scale $\Lambda^2 = \mu^2 \exp\left[\frac{12\pi}{(33 - 2n_f)\alpha_s(\mu^2)}\right]$

$$\Rightarrow \quad \alpha_s(Q^2) = \frac{12\pi}{(33 - 2n_f)\log(Q^2/\Lambda^2)}$$

for $Q^2 \gg \Lambda^2$ α_s is small \Rightarrow a perturbative description in terms of Quarks and Gluons interacting weekly



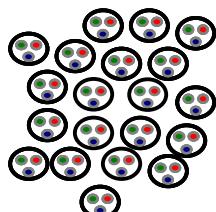
\Rightarrow for $Q^2 \sim \Lambda^2$ Quarks and Gluons arrange themselves in Strongly Bound Clusters - Hadrons

Since $\Lambda_{QCD} \sim 200$ MeV a phase transition is expected at:

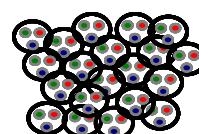
$$T \sim \Lambda_{QCD} \sim 0 (10^{12} K)$$

or

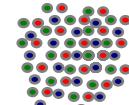
$$\rho_B \sim \Lambda_{QCD}^3 \sim 1 fm^{-3}$$



Strongly Bound Clusters
Hadrons



Phase transition



Weekly interacting
Quarks and Gluons

Related theoretical considerations in a chronological sequence

- **Highly Excited Nuclear Matter** - G.F. Chapline et al., Phys.Rev. D8(1973)4302

- *It is suggested that very hot and dense nuclear matter may be formed in a transient state in “head-on” collisions of very energetic heavy ions*

- **Vacuum stability and vacuum excitation in a spin-0 field theory**

- T.D.Lee et al., Phys.Rev. D9(1974)2291
- *One can produce the abnormal nuclear state by increasing the nuclear density through high energy collisions between very heavy nuclei*

- **Super dense matter: Neutrons or asymptotically free quarks ?**

- J.C.Collins et al., Phys.Rev. Lett. 34(1975)1353
- *The quark model implies that superdense matter (found in neutron-star cores, exploding black holes, and early big-bang universe) consist of quarks rather than of hadrons*

- **Asymtotic freedom and the baryon-quark phase transition**

- G.Chapline et al., Phys.Rev. D16(1977)450
- *Our calculations show that the baryon-quark transition takes place at densities on the order of 10-20 times that of ordinary nuclei*

- **On the possibility of making quark-gluon matter in nuclear collisions**

- G.Chapline et al., Lawrence Livermore Laboratory (1978) March, CTP #695

- **Quark matter transition in the baryon rich domain**

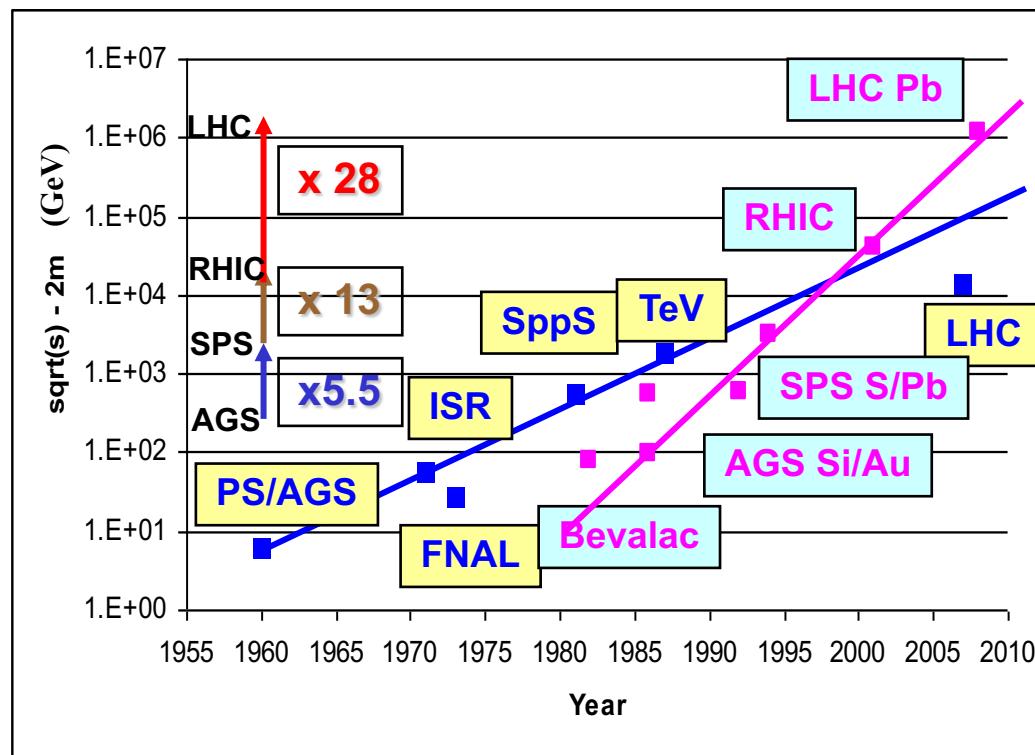
- G.Chapline, Lawrence Livermore Laboratory (1984) December, UCRL-91875

- **And many others after ...**

Experimental facilities

- *Particle Physics: energy doubling time ~ 4 years*
- *Heavy Ion Physics: doubling time ~ 2 years*

Total center-of-mass energy versus time



Experimental facilities

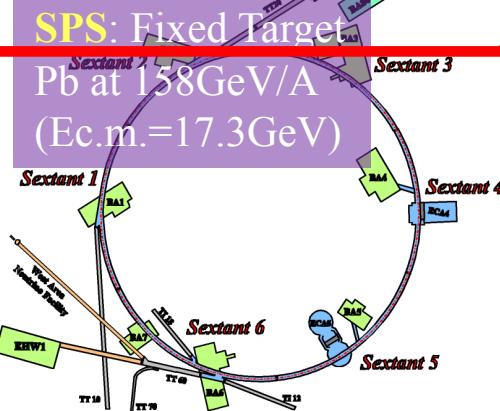
LHC: Collider
Pb+Pb @5500GeV/A



RHIC: Collider
Au+Au @ 200GeV/A



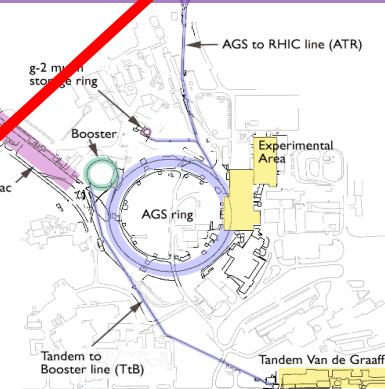
AGS: Fixed Target
Au at 11.7GeV/A
(Ec.m.=4.56GeV)



Bevalac
Fixed Target
1-2GeV/A



SIS 18

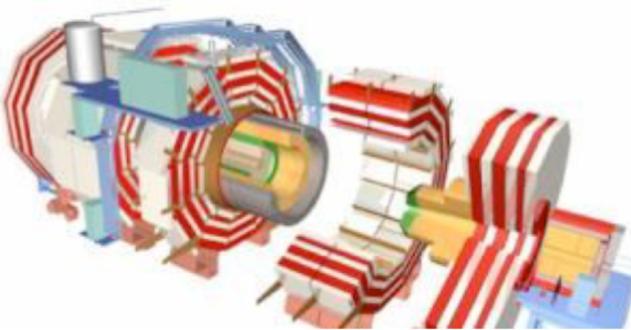


Some of the experiments dedicated to:

- EoS
- In medium effects
- QGP

studies

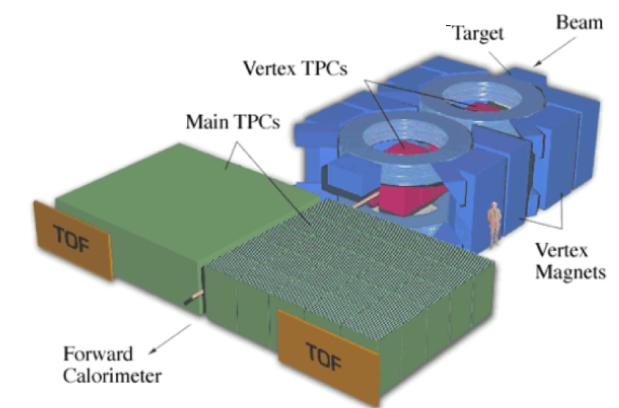
CMS at LHC



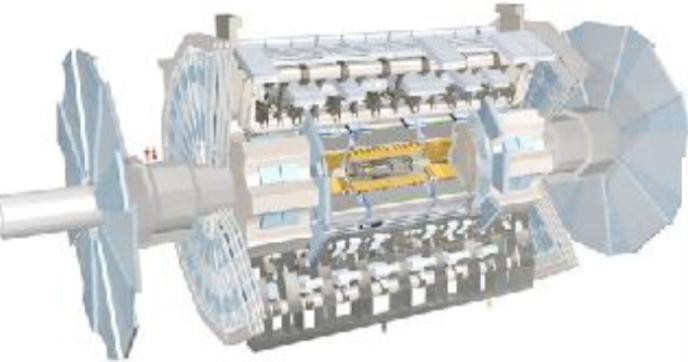
LHCb at LHC



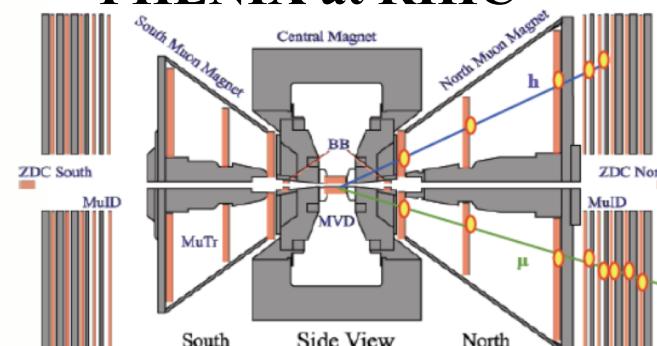
NA49 at SPS



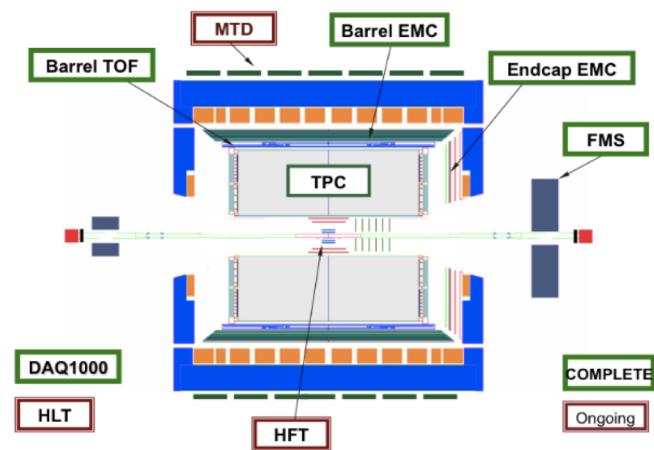
ATLAS at LHC



PHENIX at RHIC

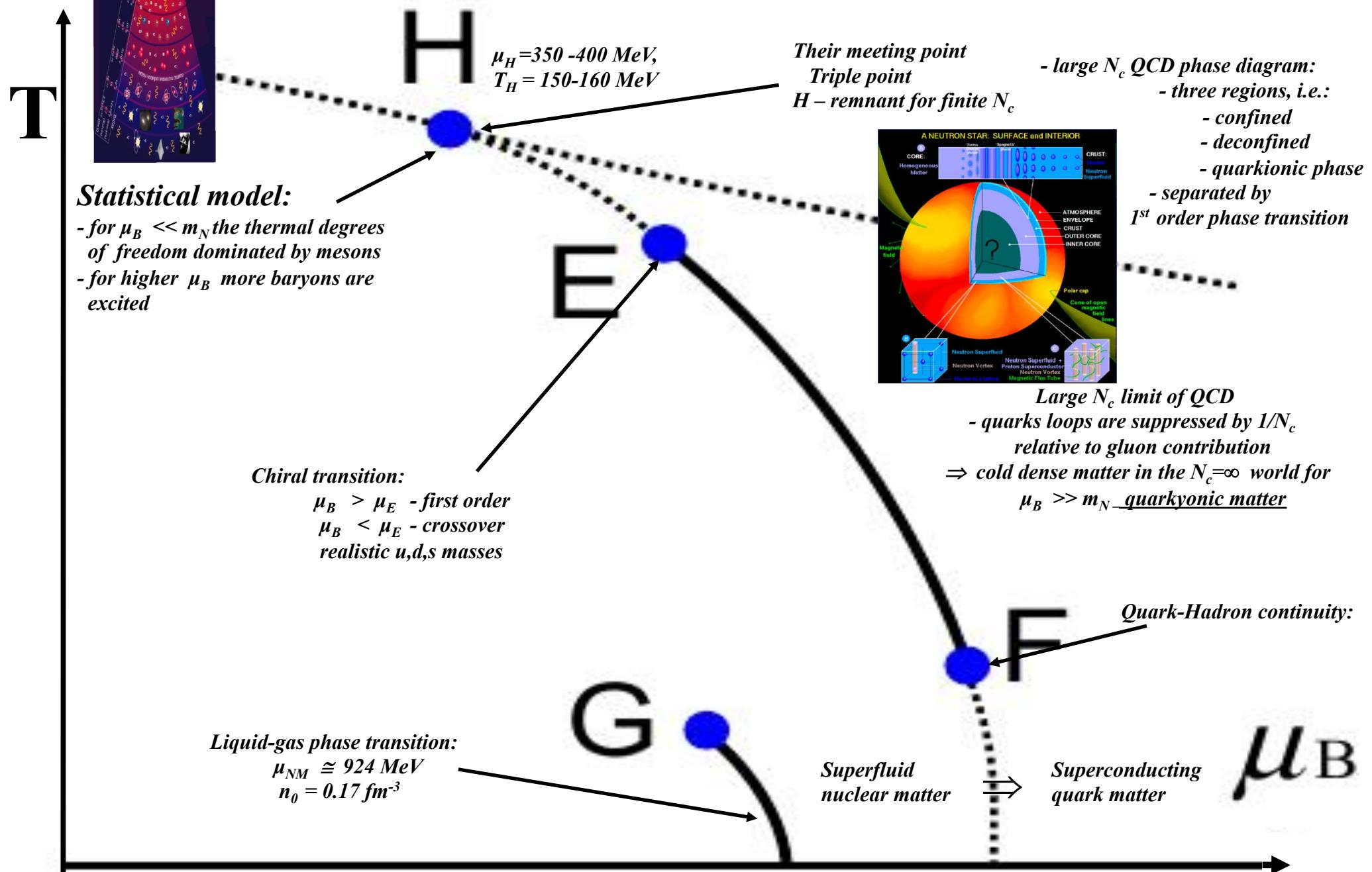


STAR at RHIC

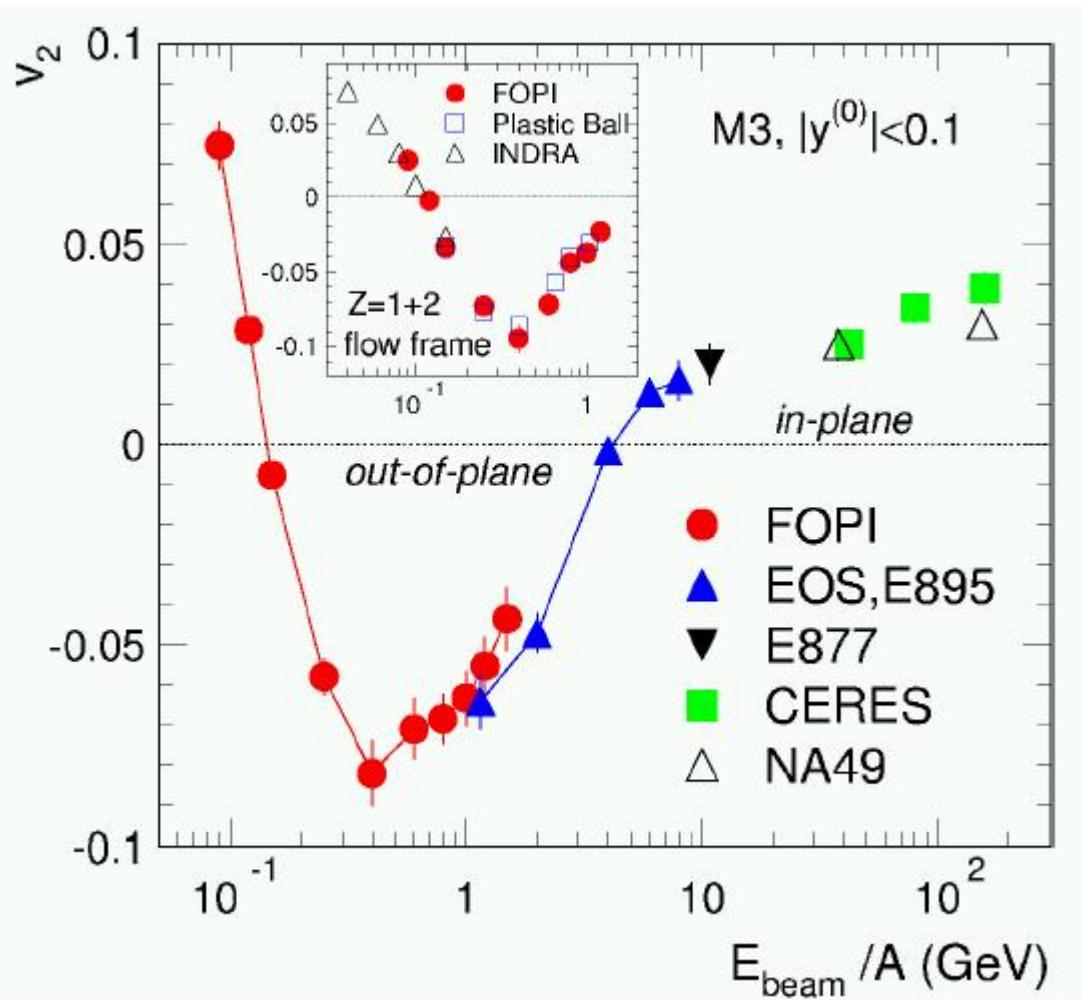


Expectations based on QCD

QCD Critical Points



v_2 excitation function - AGS and SPS



FOPI – Z=1 particles

A. Andronic & FOPI Coll.,
Phys. Lett. B 612 (2005) 173

EOS,E895 – protons

C. Pinkenburg & EOS Coll.
Phys. Rev. Lett. 83 (1999) 1295

E877 – all charged particles

P. Braun-Munzinger et al.,
Nucl. Phys. A 638 (1998) 3c

CERES – all charged particles

H. Appelshauser et al., *Nucl. Phys. A* 698 (2002) 253c

NA49 – pions

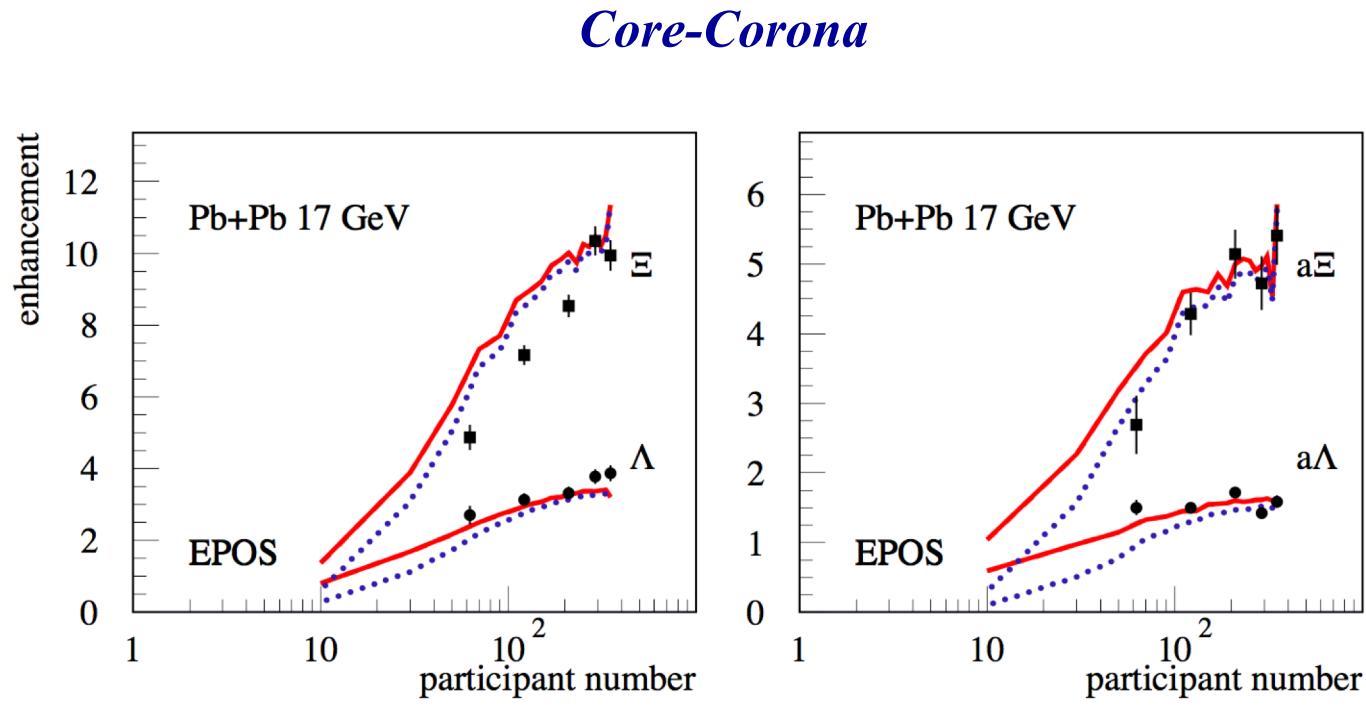
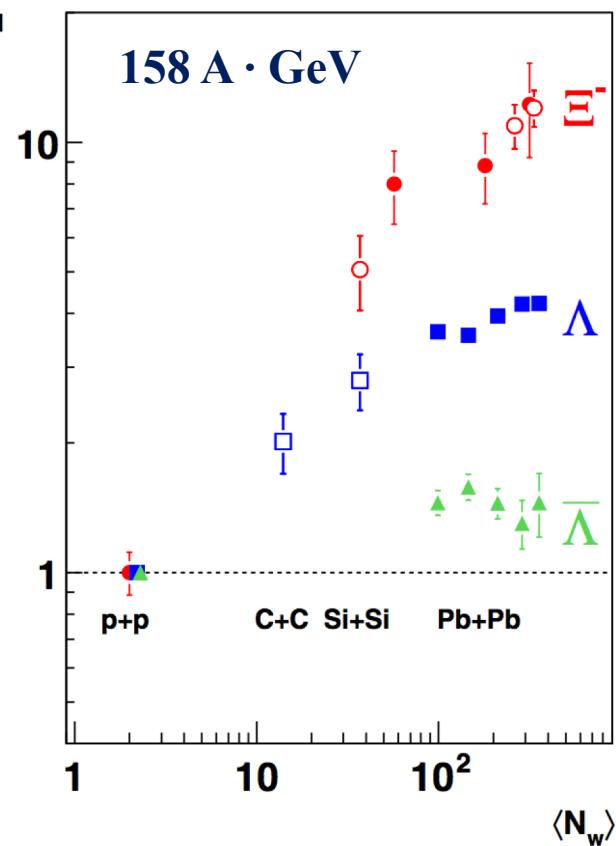
C. Alt et al., *Phys. Rev. C* 68 (2003) 034903

$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} \left(1 + \sum_{n=1}^{\infty} 2v_n \cos(n(\phi - \Psi_r)) \right)$$

$$v_2 = \langle \cos 2(\phi - \Psi_r) \rangle, \quad \phi = \tan^{-1}\left(\frac{p_y}{p_x}\right)$$

Strangeness enhancement - SPS

Exp.



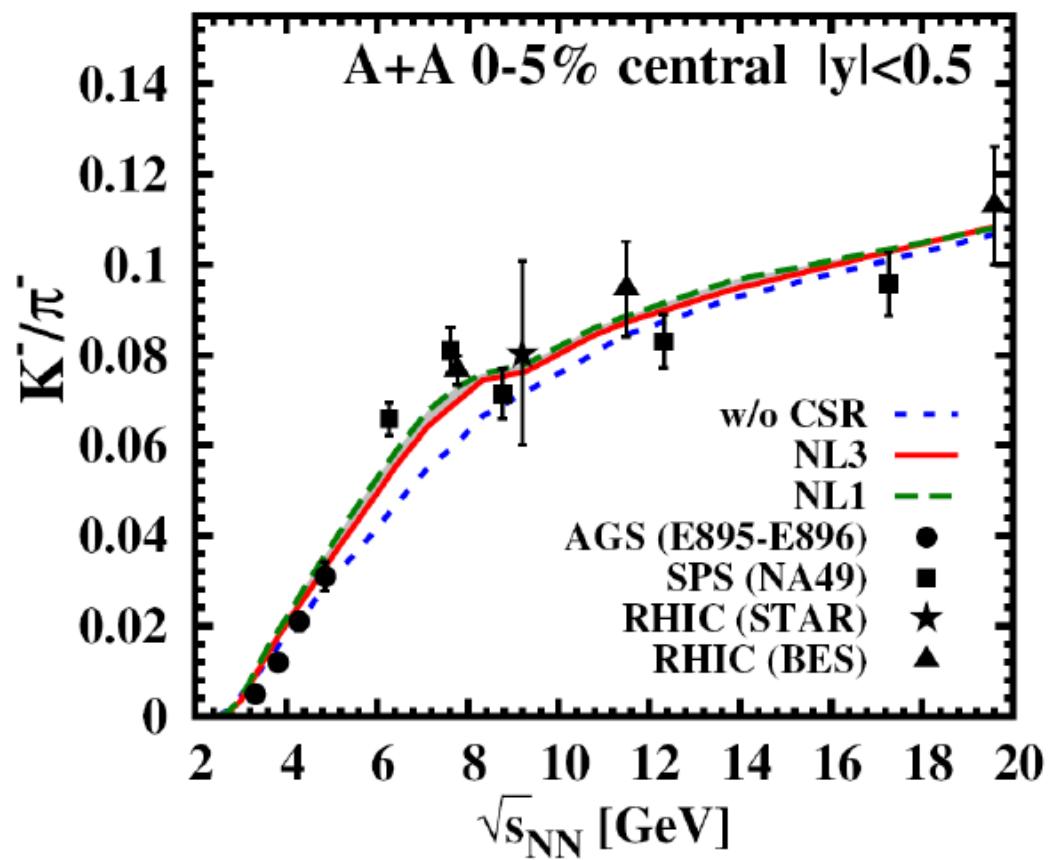
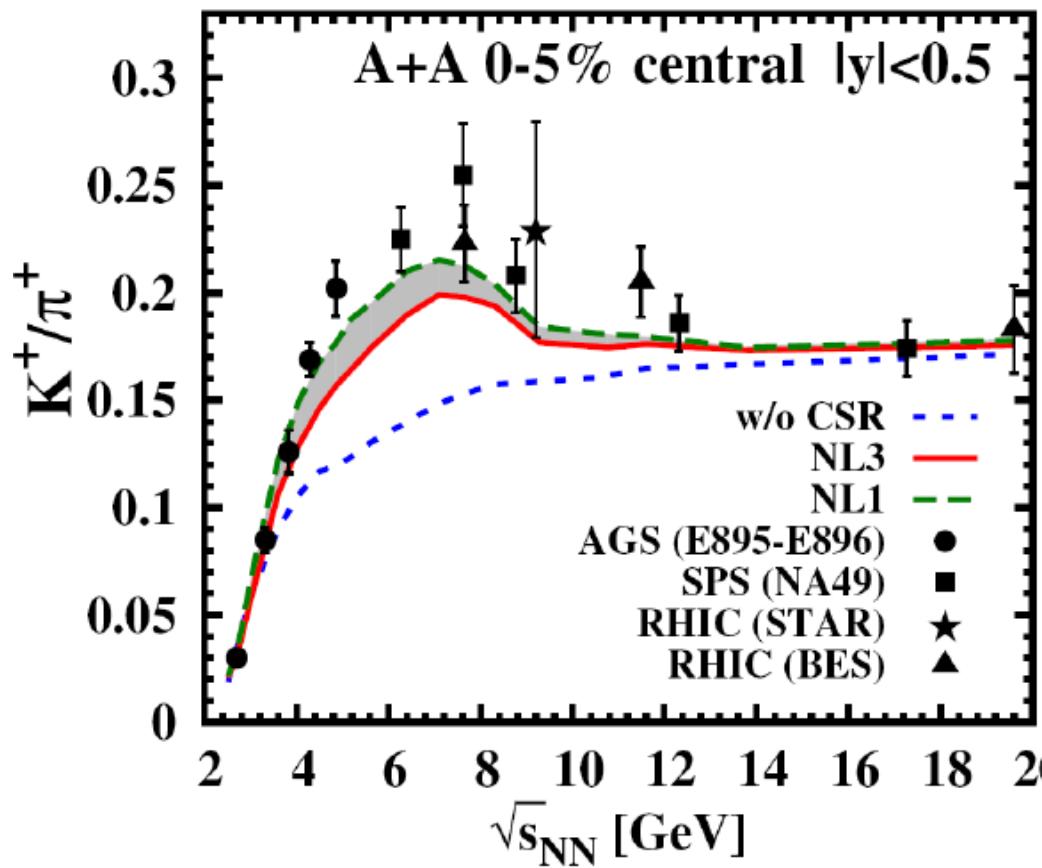
$$E = \left(\frac{1}{\langle N_w \rangle} \left. \frac{dN(Pb+Pb)}{dy} \right|_{y=0} \right) \Bigg/ \left(\frac{1}{2} \left. \frac{dN(p+p)}{dy} \right|_{y=0} \right)$$

$$M^i(N_{part}) = N_{part} [f(N_{core}) \cdot M^i_{core} + (1-f(N_{core})) \cdot M^i_{corona}]$$

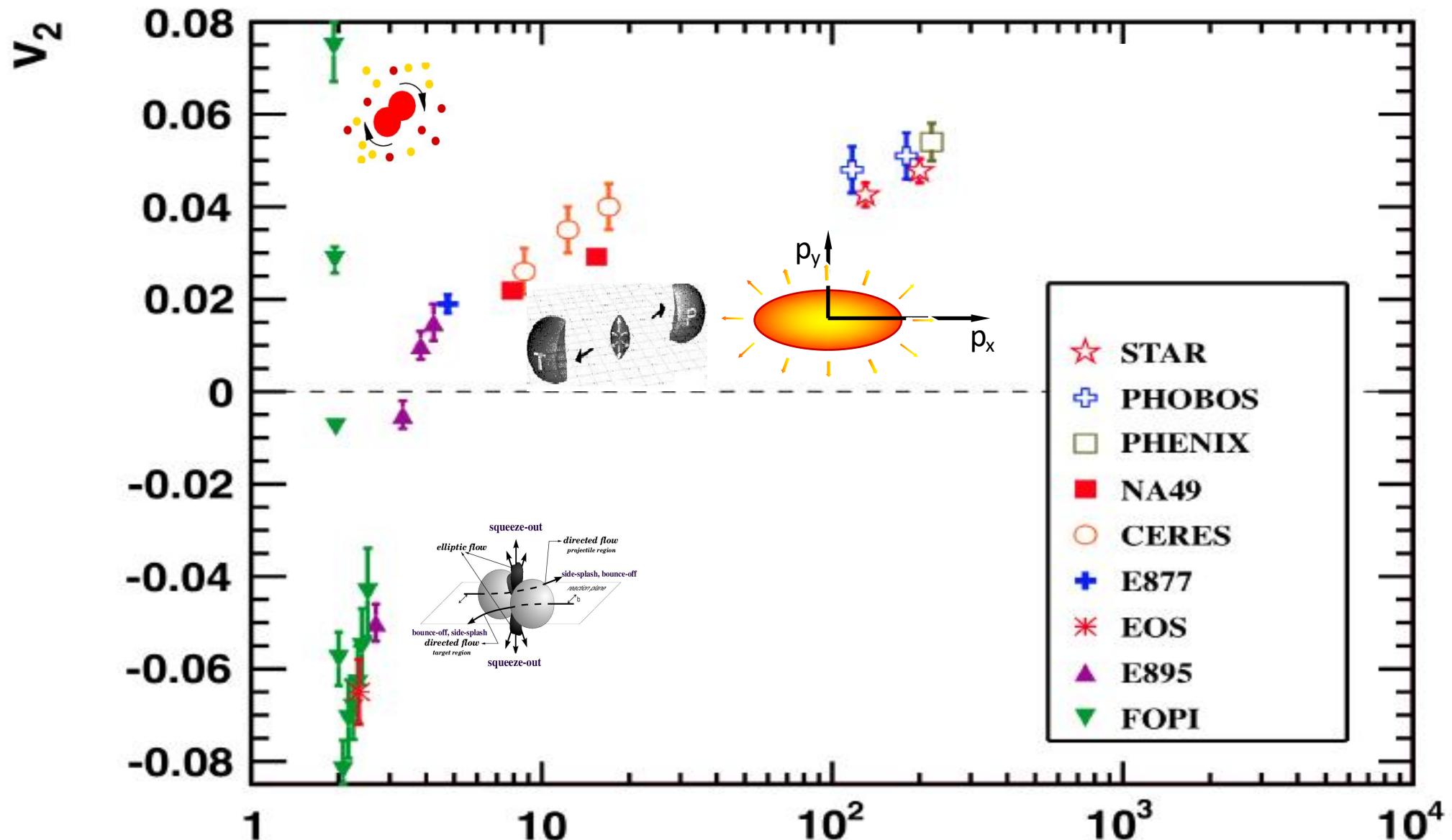
C. Blume et al., NA49 Collaboration,
J. Phys. G: Nucl. Part. Phys. 34 (2007) S951

J. Aichelin et al., Phys. Rev. C79 (2009) 064907

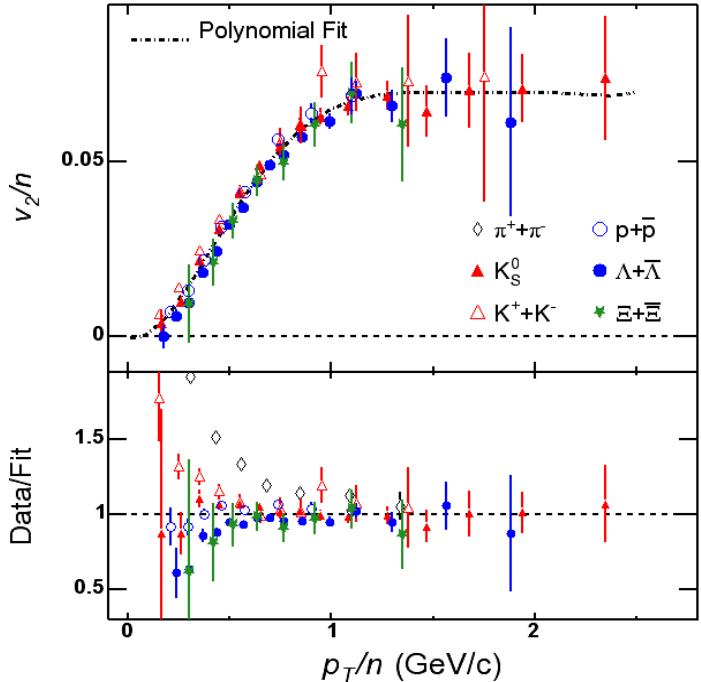
K/π “horn” - SPS



Elliptic flow (v_2) - excitation function including RHIC results



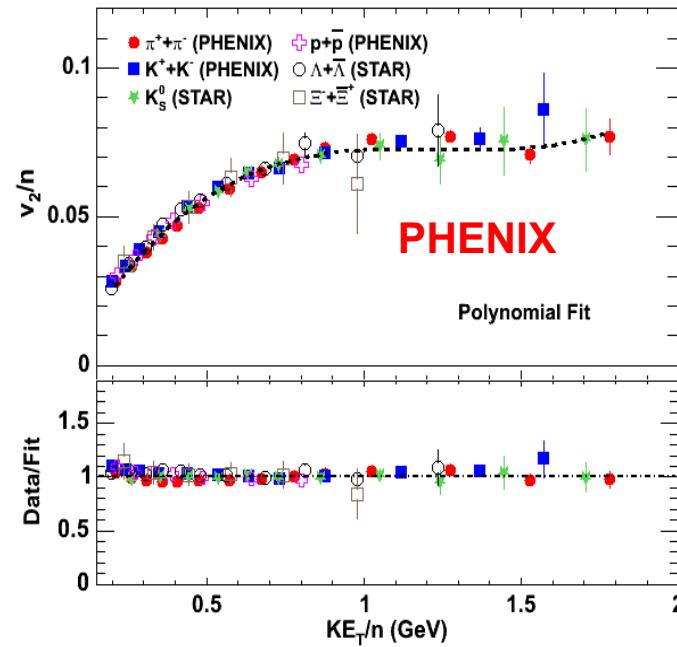
Elliptic Flow - Quark Number Scaling



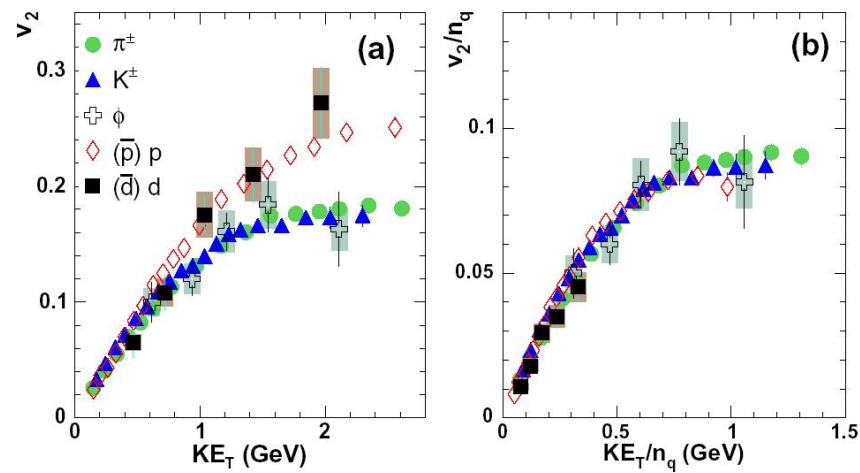
S.S.Adler *et al.*, PHENIX Coll., Phys.Rev.Lett. 91 (2003) 182301

J.Adams *et al.*, STAR Coll., Phys.Rev.Lett. 92 (2004) 052302

- At the moment of hadronization in nucleus-nucleus collisions at RHIC the dominant degree of freedom is related to number of constituent (valence) quarks
- These ‘constituent quarks’ exhibit an angular anisotropy resulting from collective interactions
- Hadrons seem to be formed from coalescence or recombination of the ‘constituent quarks’



A.Adare *et al.*, PHENIX Coll., Phys.Rev.Lett. 98(2007)162301



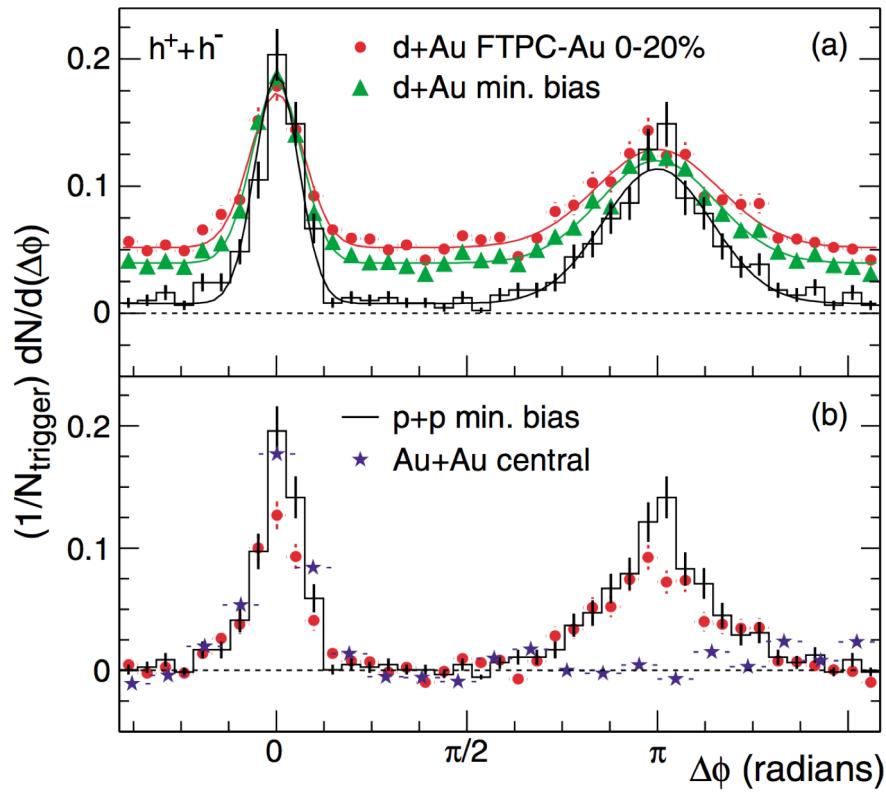
S.Afanasiev *et al.*, PHENIX Coll., Phys.Rev.Lett. 99(2007)052301

Final-state suppression of high- p_T hadrons

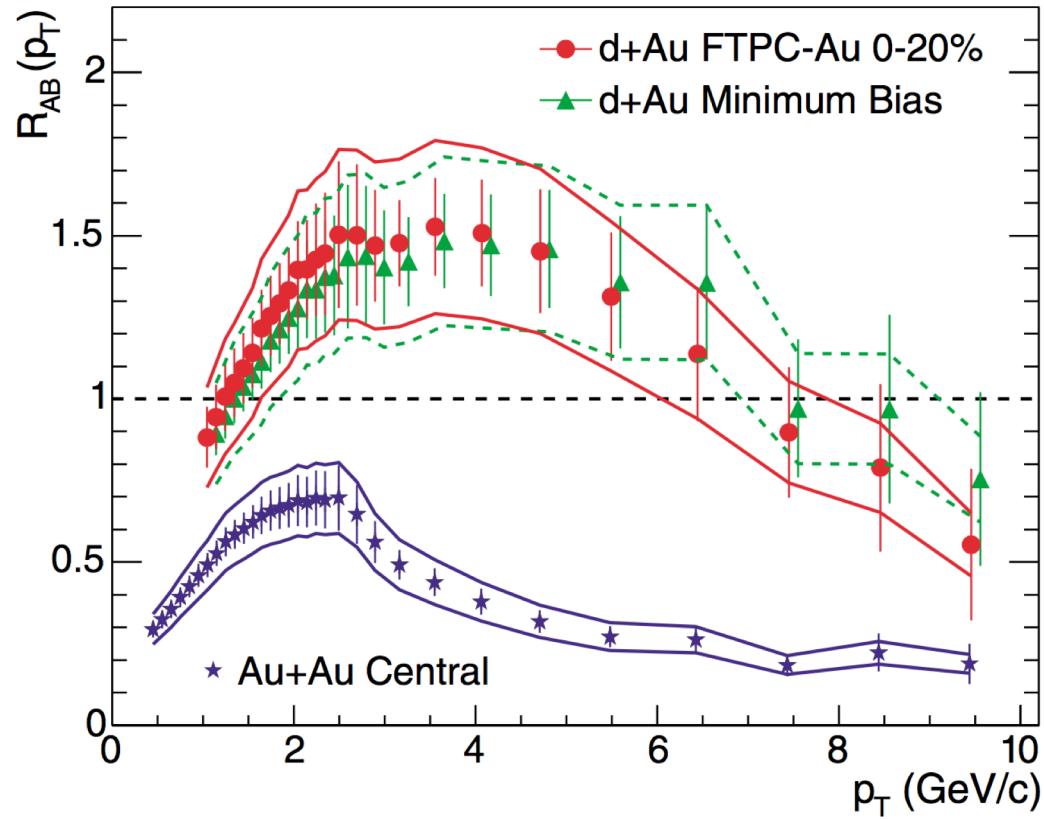
Au-Au, d-Au and pp collisions at $\sqrt{s_{NN}} = 200 \text{ GeV}$

$$4 < p_T(\text{trig}) < 6 \text{ GeV}/c$$

$$2 < p_T < p_T(\text{trig})$$



$$D(\Delta\phi) = A_N \frac{e^{-(\Delta\phi)^2/2\sigma_N^2}}{\sqrt{2\pi}\sigma_N} + A_B \frac{e^{-(|\Delta\phi|-\pi)^2/2\sigma_B^2}}{\sqrt{2\pi}\sigma_B} + P$$

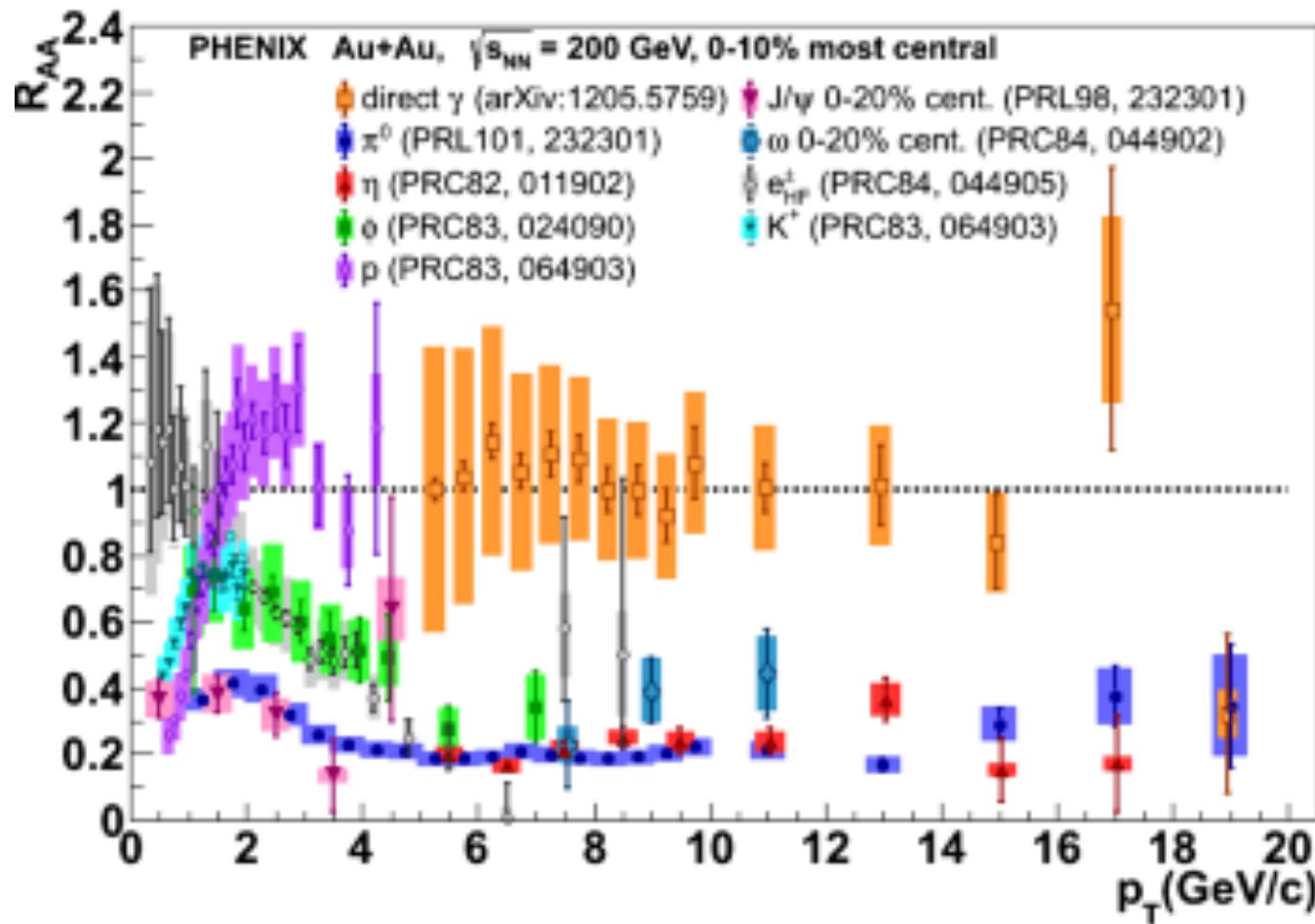


$$R_{AB}(p_T) = \frac{d^2N/dp_T d\eta}{T_{AB} d^2\sigma^{pp}/dp_T d\eta}$$

$$T_{AB} = \langle N_{\text{bin}} \rangle / \sigma_{\text{inel}}^{pp}$$

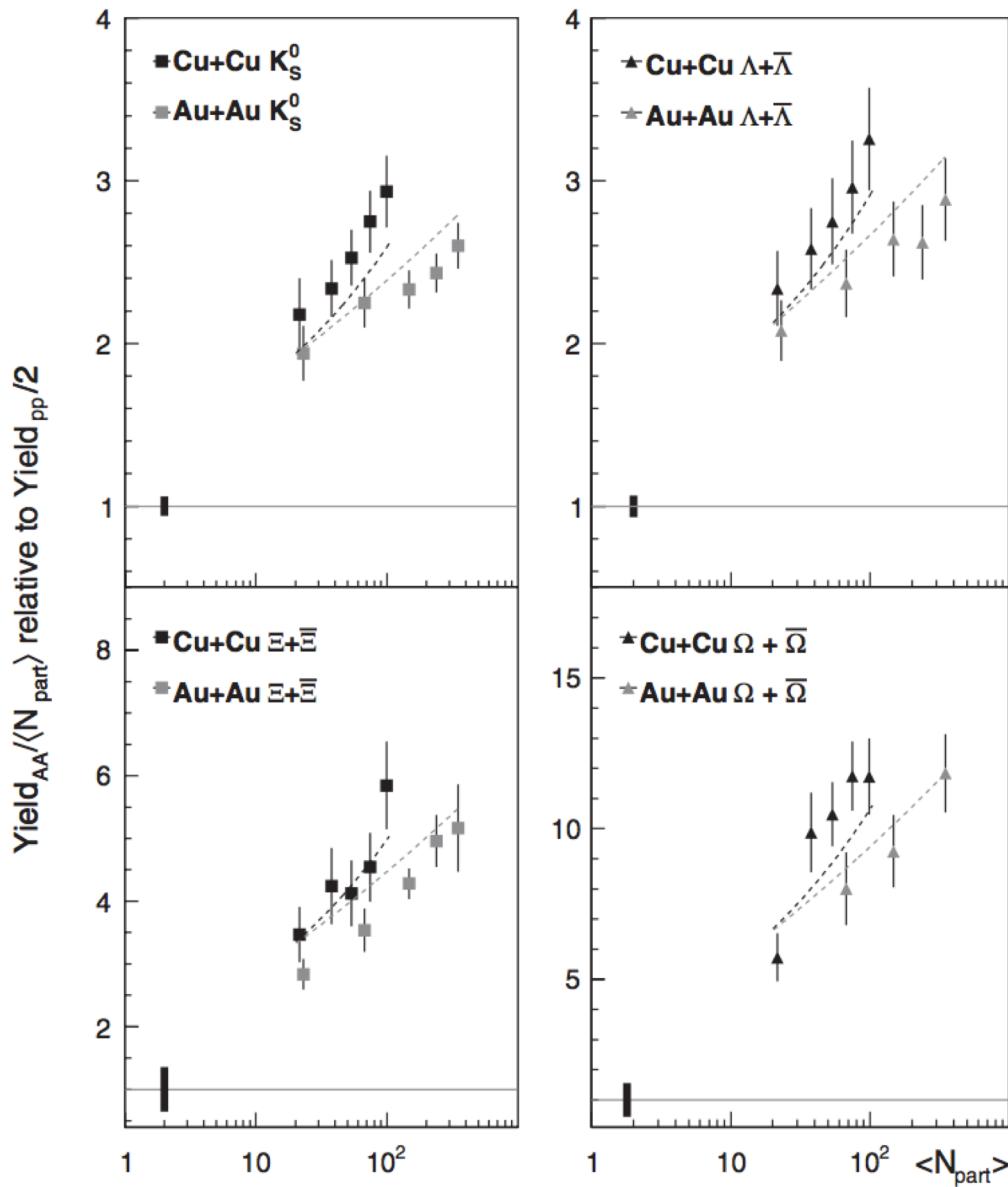
Final-state suppression of high- p_T hadrons

Au-Au, d-Au and pp collisions at $\sqrt{s_{NN}} = 200 \text{ GeV}$

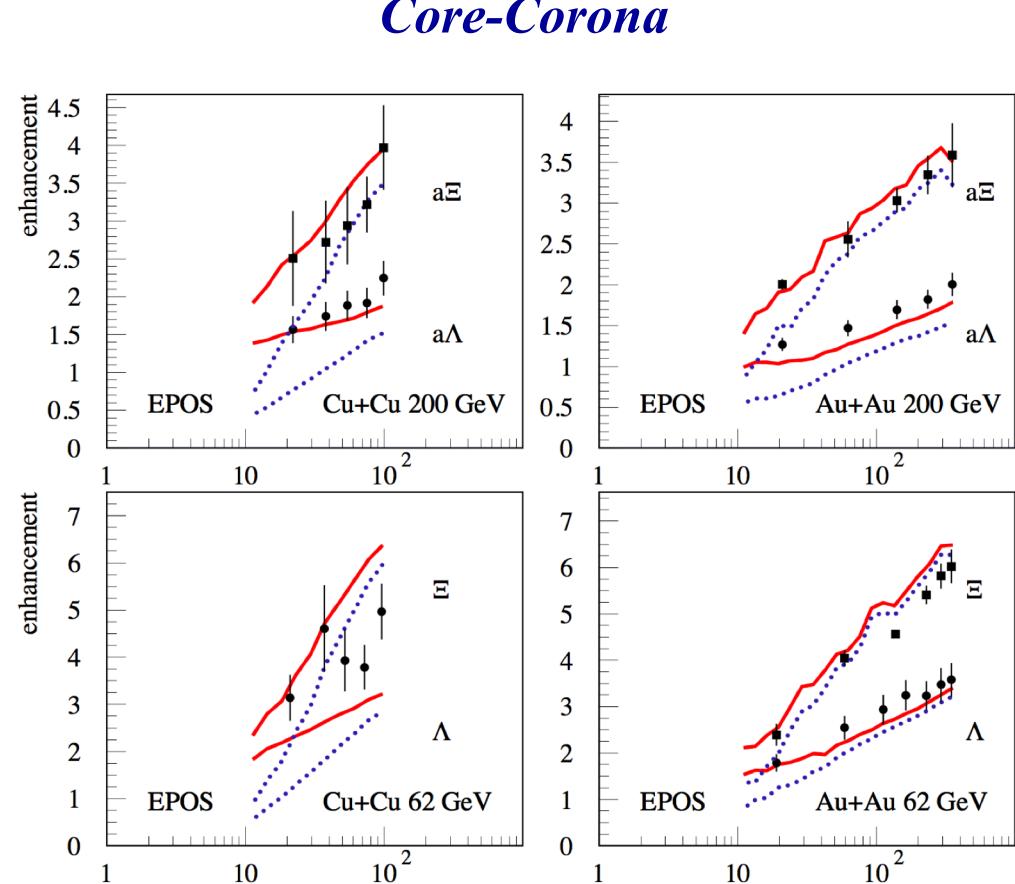


Strangeness enhancement at RHIC

Cu-Cu and Au-Au at $\sqrt{s_{NN}} = 200 \text{ GeV}$

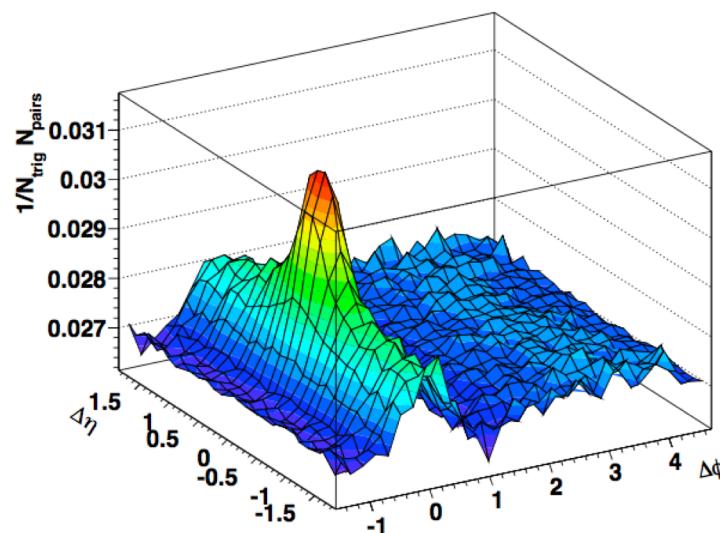
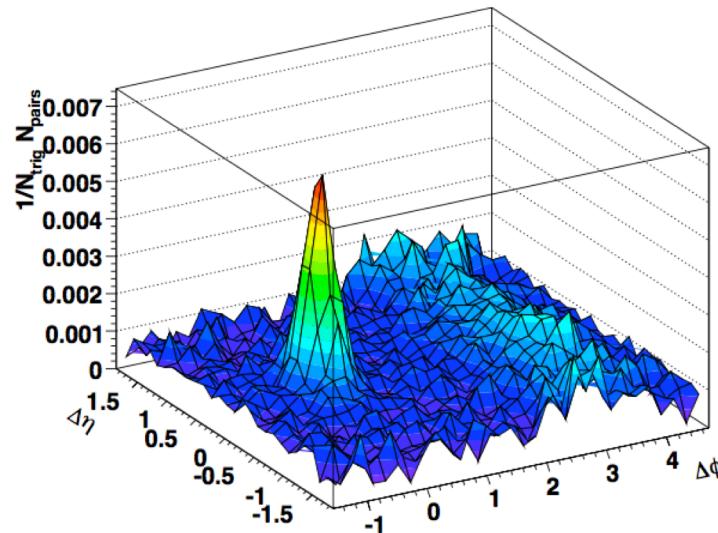


Core-Corona



J.Aichelin et al., Phys.Rev.C81(2001)029902

Two-particle correlations at RHIC

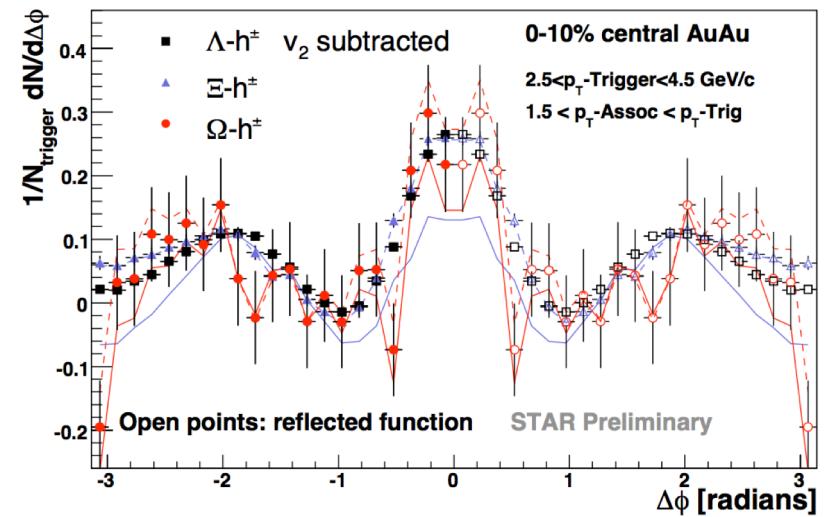
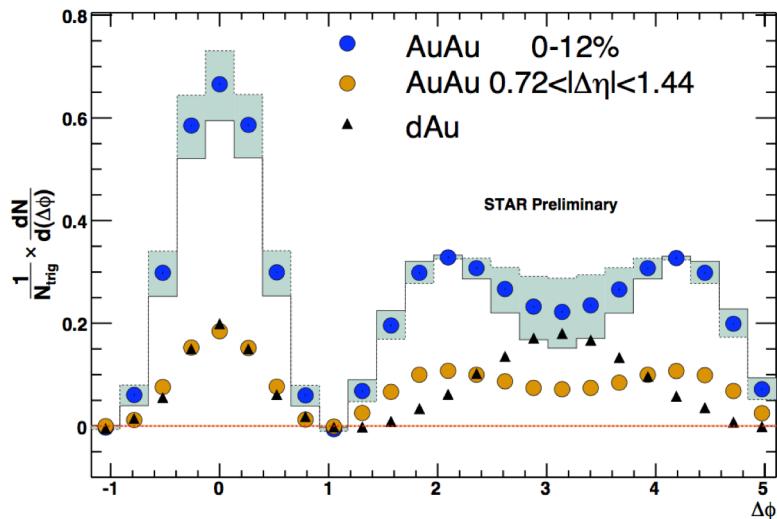


(a)

(b)

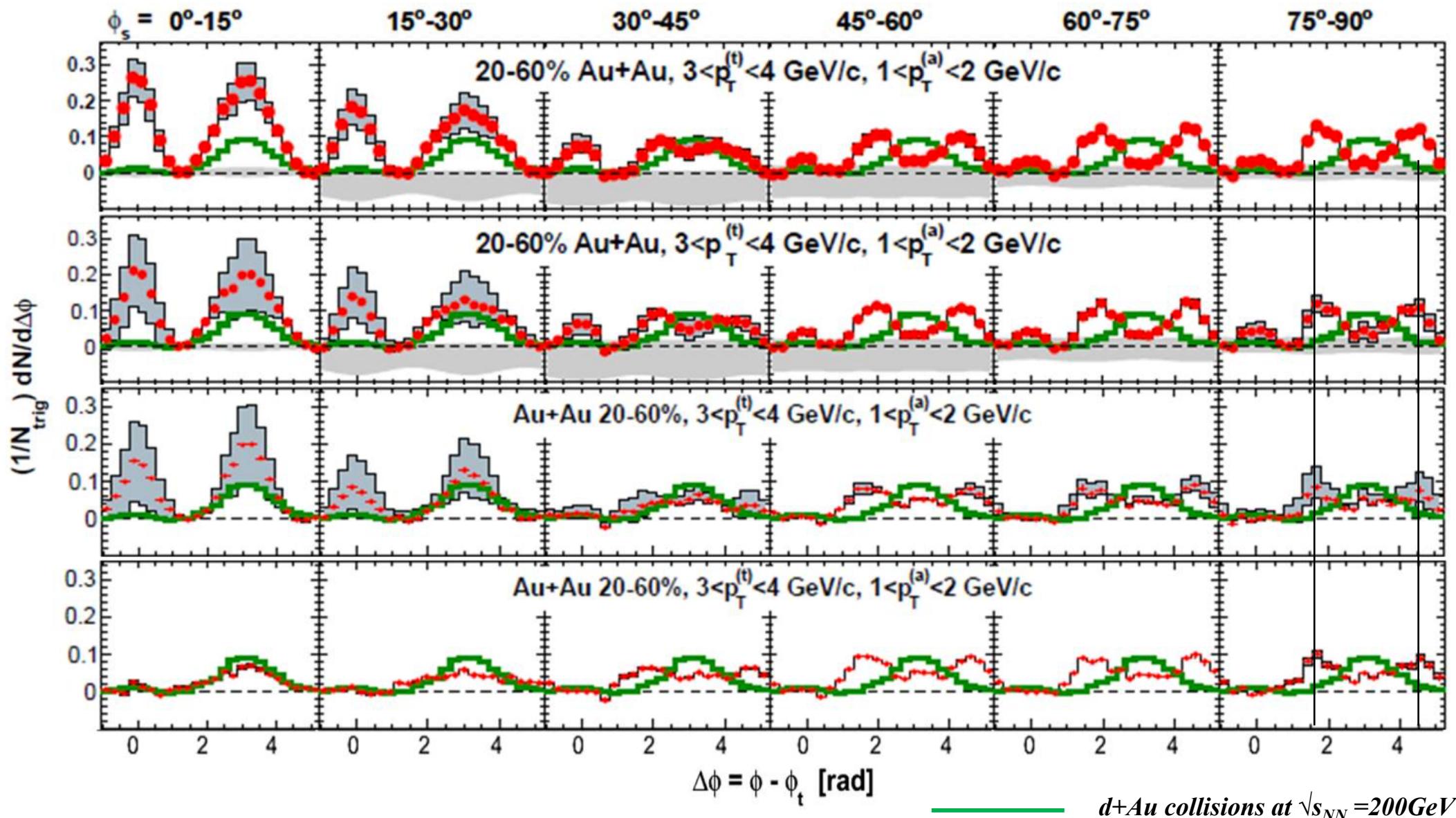
Two-particle angular correlations ($\Delta\phi, \Delta\eta$): a) $d+Au$ and b) central (0-10%) $Au+Au$ collisions at $\sqrt{s_{NN}} = 200 GeV$ for $3 < p_{trig} < 6 GeV/c$ and $2 GeV/c < p_{asso} < p_{trig}$

$2.5 < p_{trig} < 4.0 GeV/c$ and $1.0 < p_{asso} < 2.5 GeV/c$

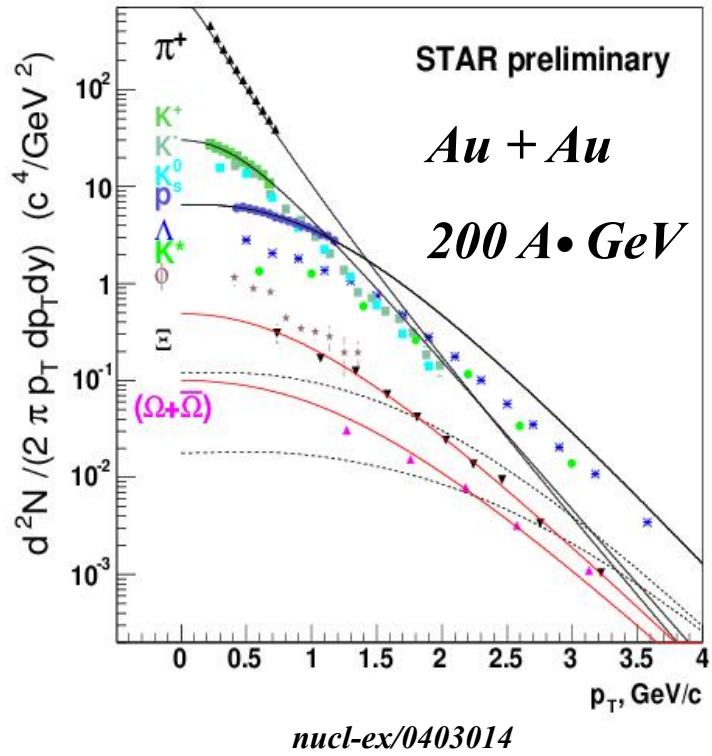


Two particle correlations at RHIC

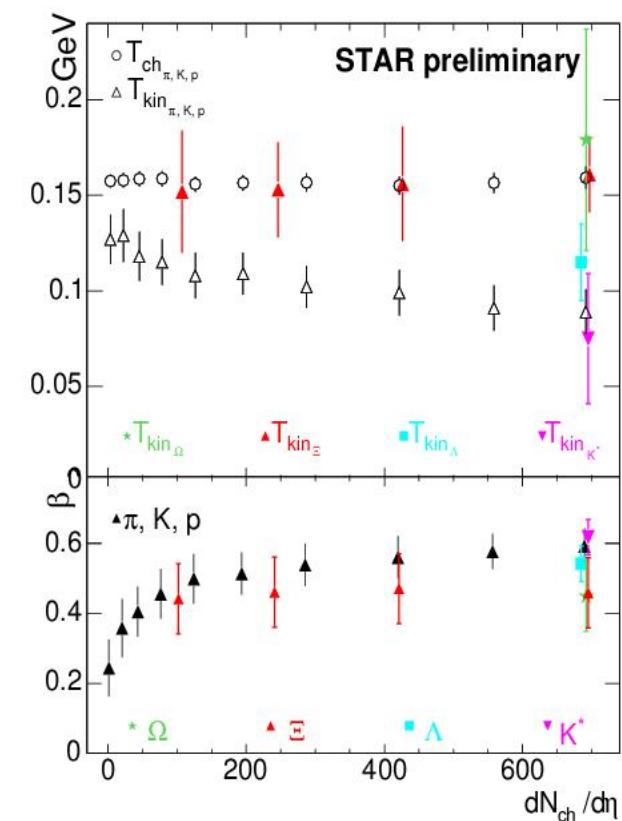
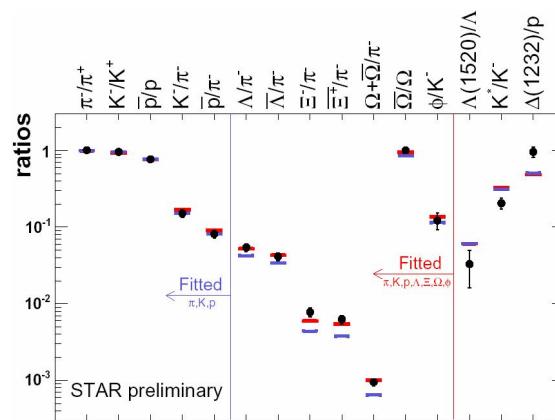
Two-particle angular correlations Au+Au collisions at $\sqrt{s_{NN}} = 200\text{GeV}$



Transverse Flow at RHIC



Particle	T_{kin} (MeV)	$\langle \beta \rangle (c)$
π, K, p	89 ± 10	0.59 ± 0.05
K^*	75 ± 35	0.62 ± 0.05
$\Lambda, \bar{\Lambda}$	115 ± 20	0.54 ± 0.05
Ξ^-, Ξ^+	161 ± 20	0.46 ± 0.10
$\Omega, \bar{\Omega}$	179 ± 60	0.45 ± 0.10



$$\frac{dN}{m_T dm_T} \propto \int_0^R r dr m_T K_1 \left(\frac{m_T \cosh \rho}{T_{fo}} \right) I_0 \left(\frac{p_T \sinh \rho}{T_{fo}} \right)$$

$$\rho = \tanh^{-1} \beta_r \quad \beta_r = \beta_s \left(\frac{r}{R} \right)^\alpha \quad \alpha = 0.5, 0.7, 1, 2$$

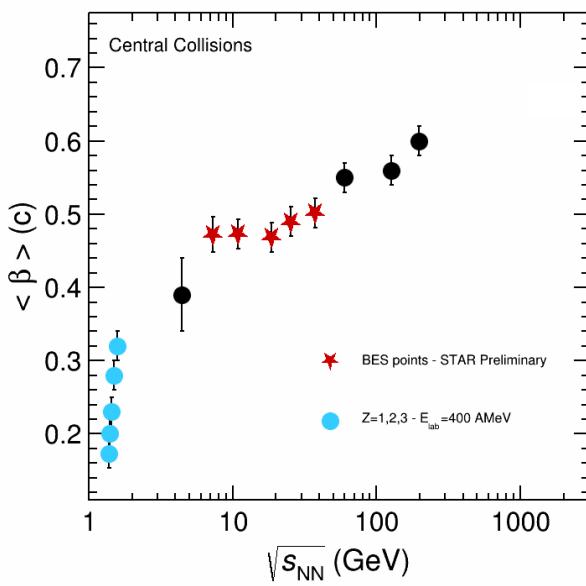
Shnedermann, Sollfrank, Heinz, nucl-th/9307020

Compilation including SIS18, SPS and RHIC central collisions

$$E \frac{d^3N}{dp^3} \sim f(p_t) = \int_0^R m_T K_1(m_T \cosh \rho / T_{fo}) I_0(p_T \sinh \rho / T_{fo}) r dr$$

$$n = \frac{1}{V} \frac{\partial(T \ln Z)}{\partial \mu} = \frac{VTm_i^2 g_i}{2\pi^2} \sum_{k=1}^{\infty} \frac{(\pm 1)^{k+1}}{k} \left(e^{\beta k \mu_i} \right) K_2 \left(\frac{km_i}{T} \right)$$

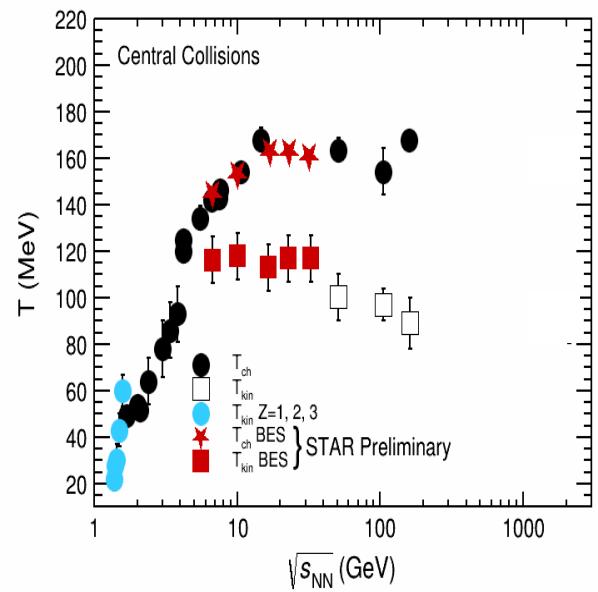
where $m_T = \sqrt{m^2 + p_T^2}$; $\beta_r(r) = \beta_s \left(\frac{r}{R} \right)^n$; $\rho = \tanh^{-1} \beta_r$.



π^+, K^+, p – simultaneous fits

FOPI
E866
STAR

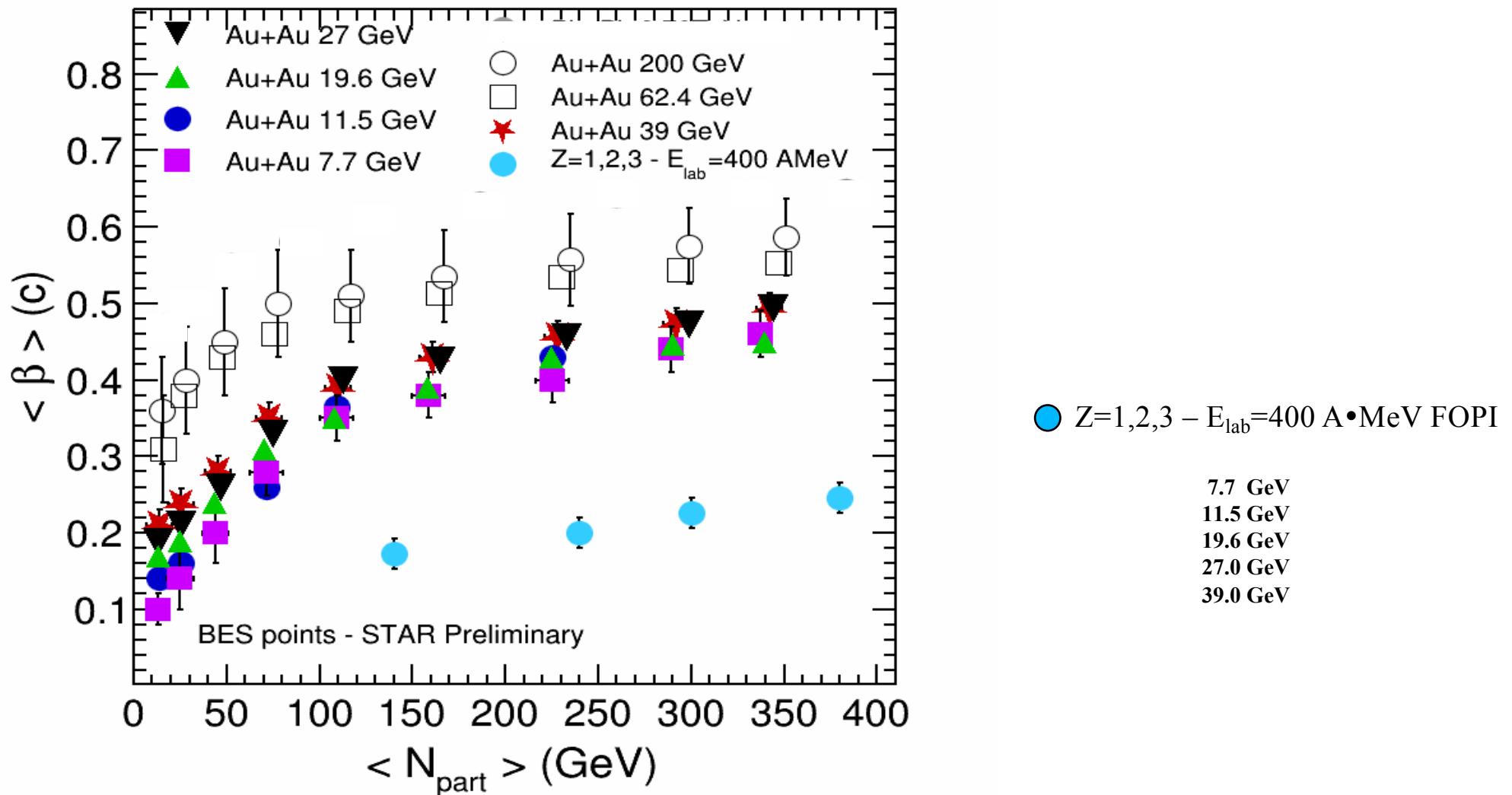
7.7 GeV
11.5 GeV
19.6 GeV
27.0 GeV
39.0 GeV



L. Kumar, STAR Coll., QM2014

M.Petrovici, Carpathian Summer School of Physics
July 23, 2014 - Sinaia, Romania

Compilation of SIS and RHIC $\langle \beta \rangle - N_{part}$ dependence

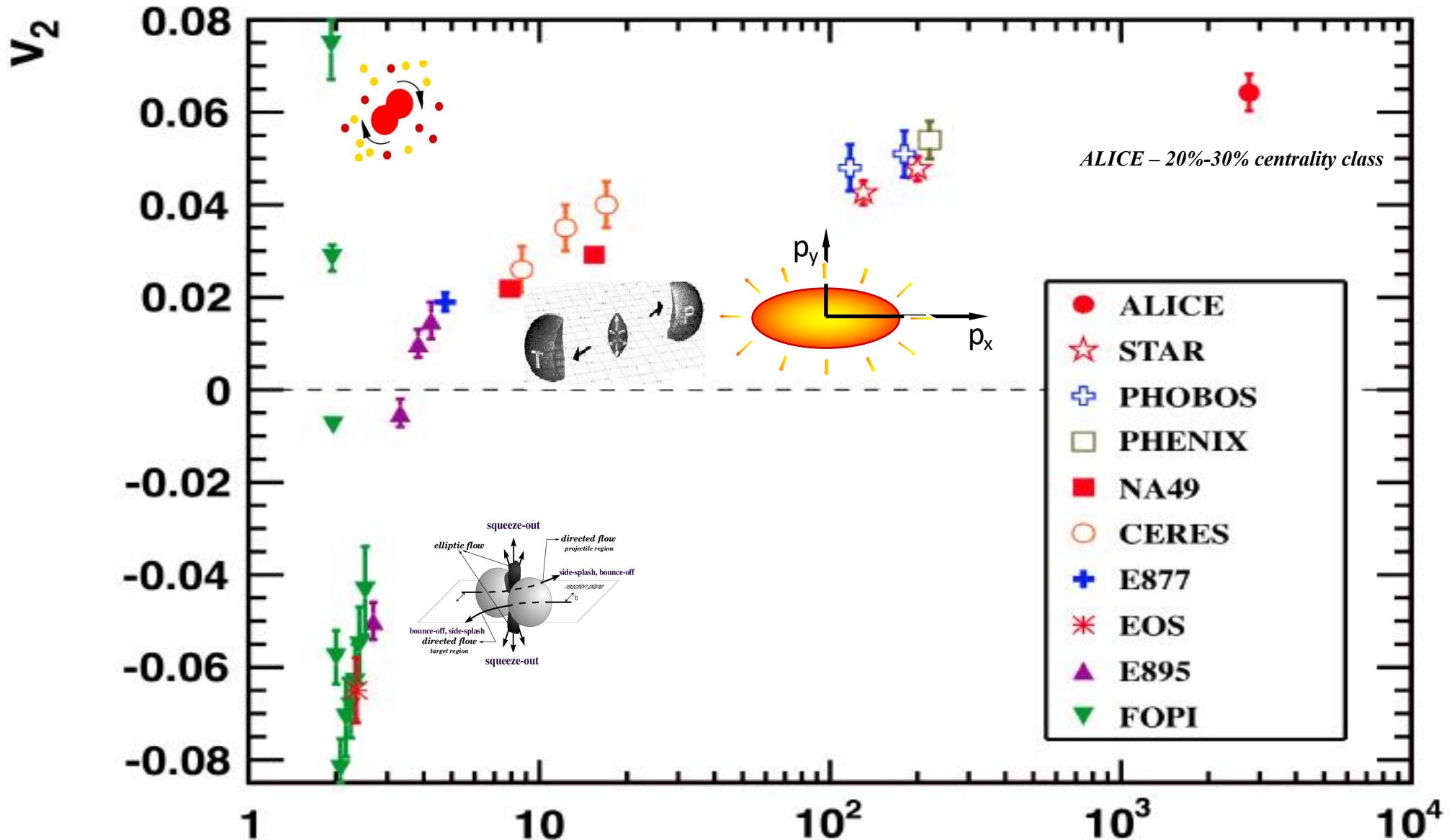


L. Kumar, STAR Coll., QM2014

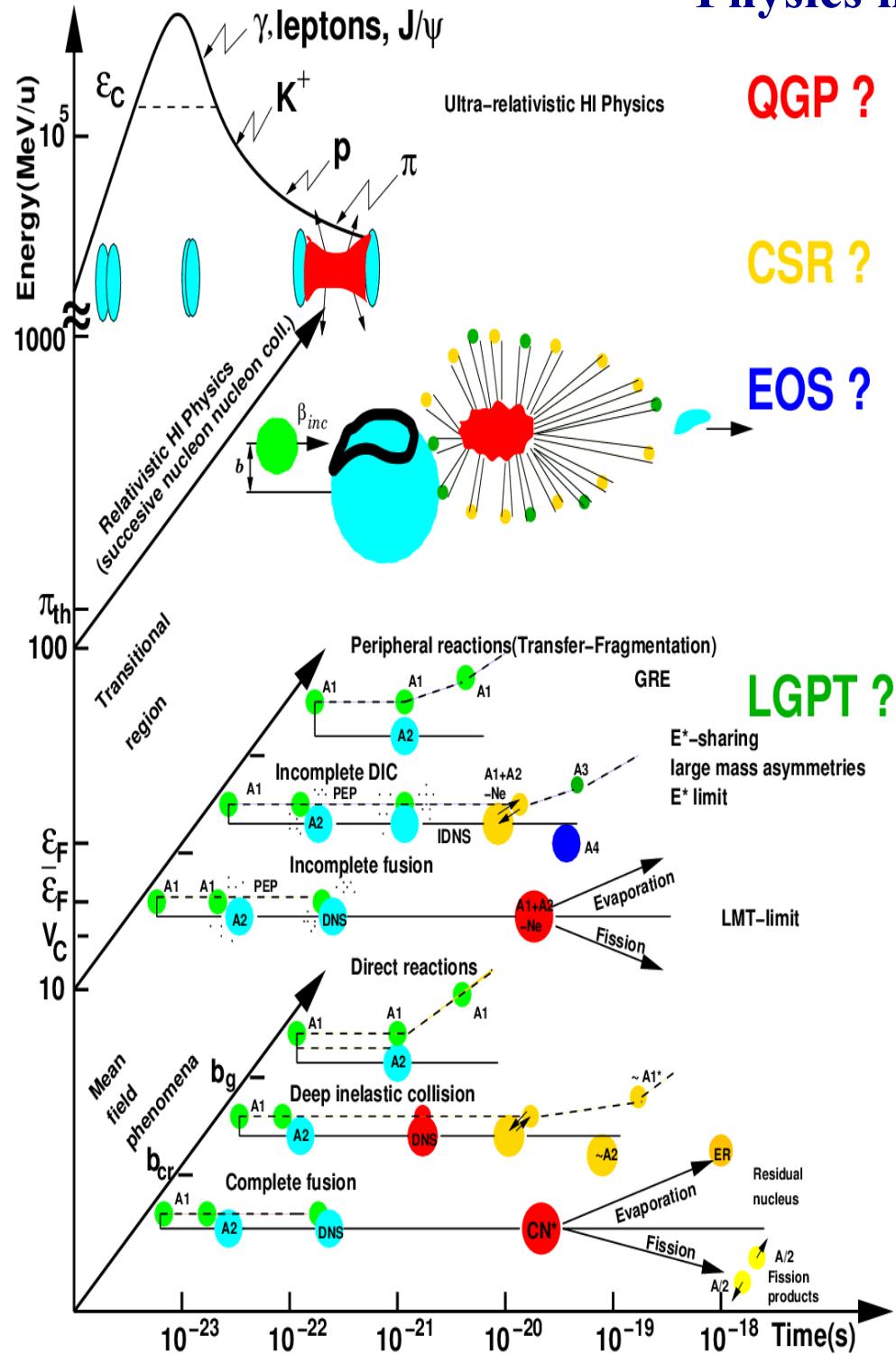
M.Petrovici, Carpathian Summer School of Physics

July 23, 2014 - Sinaia, Romania

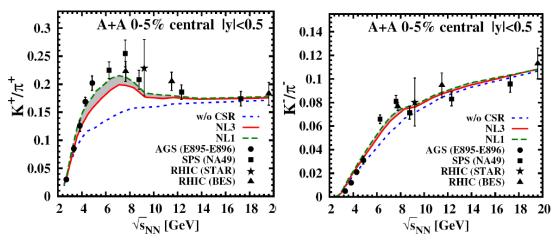
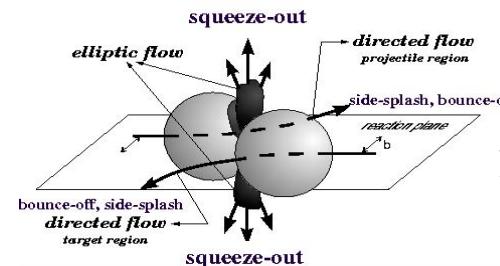
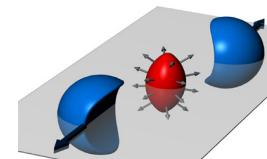
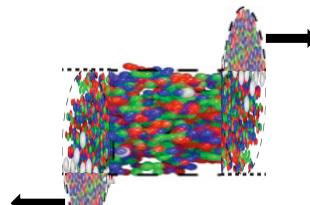
Elliptic flow (v_2) – excitation function including LHC results



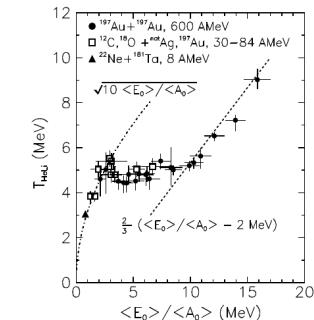
Physics motivation



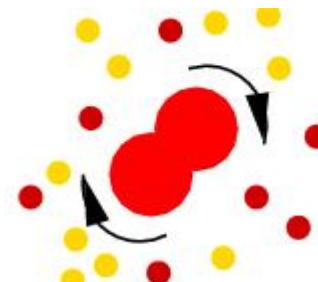
QGP ?



100 A•MeV - ~600 A•MeV

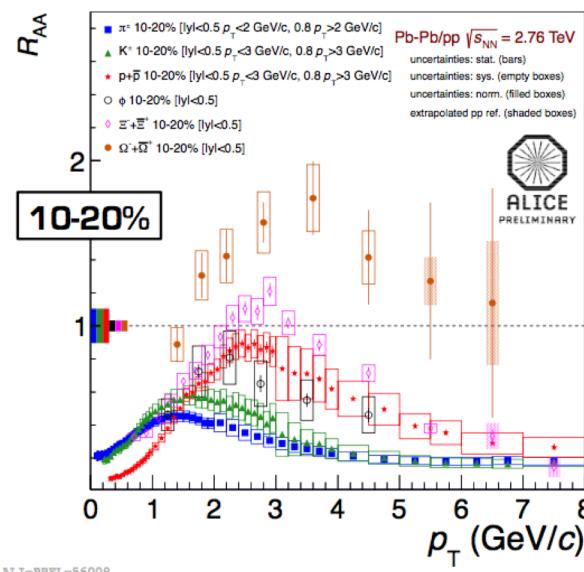
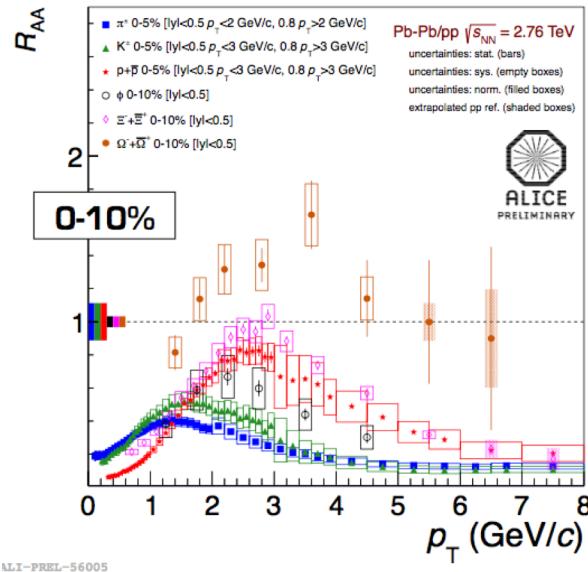


< 100 A•MeV

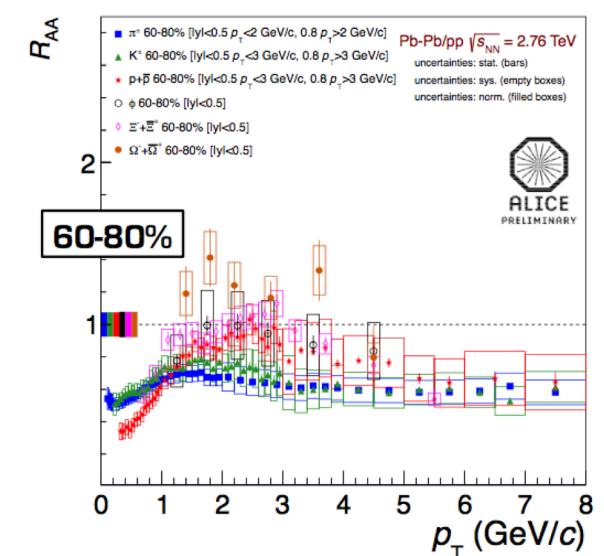
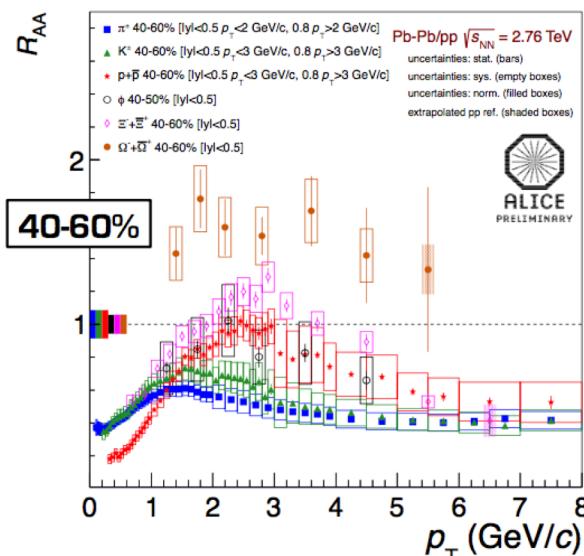
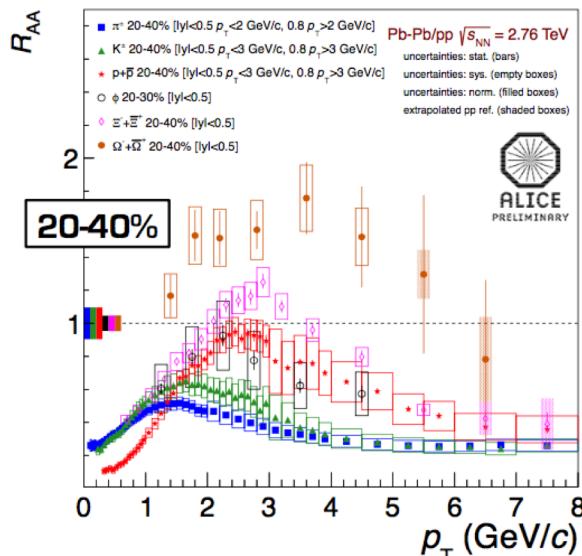


Suppression of high- p_T hadrons at LHC

Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76 \text{ GeV}$

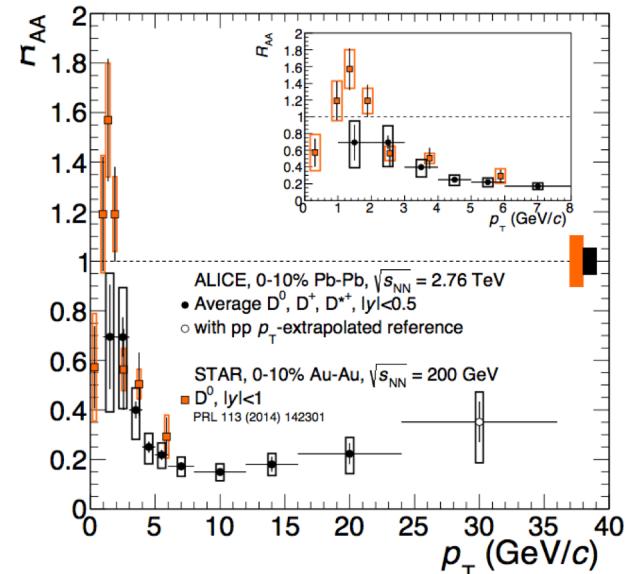
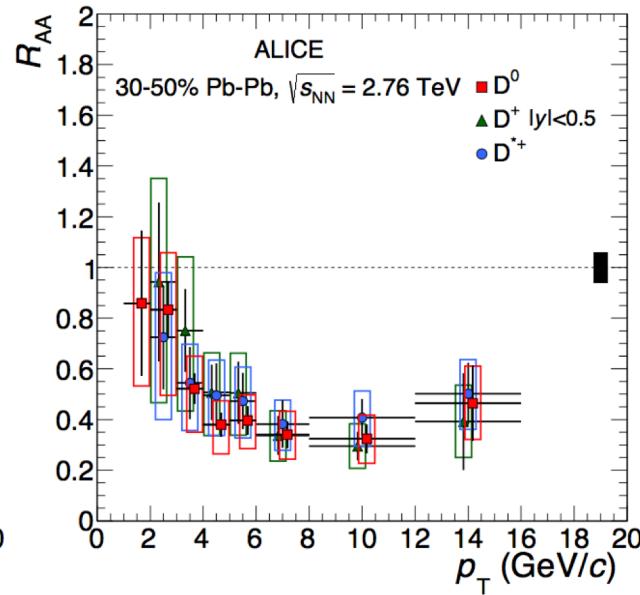
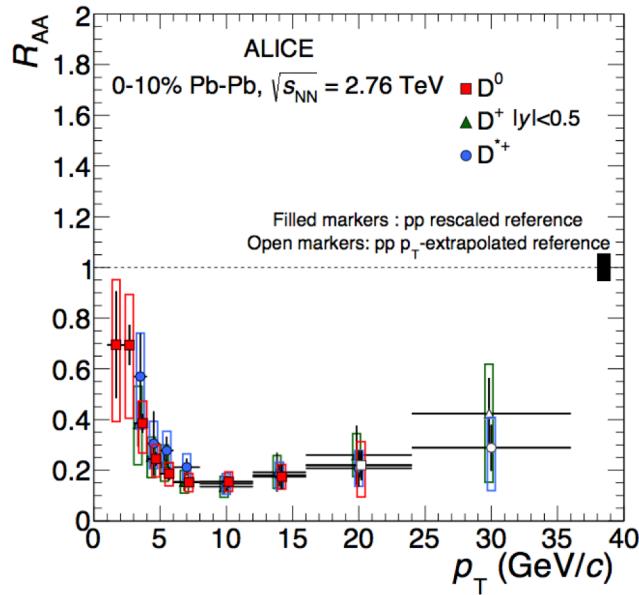


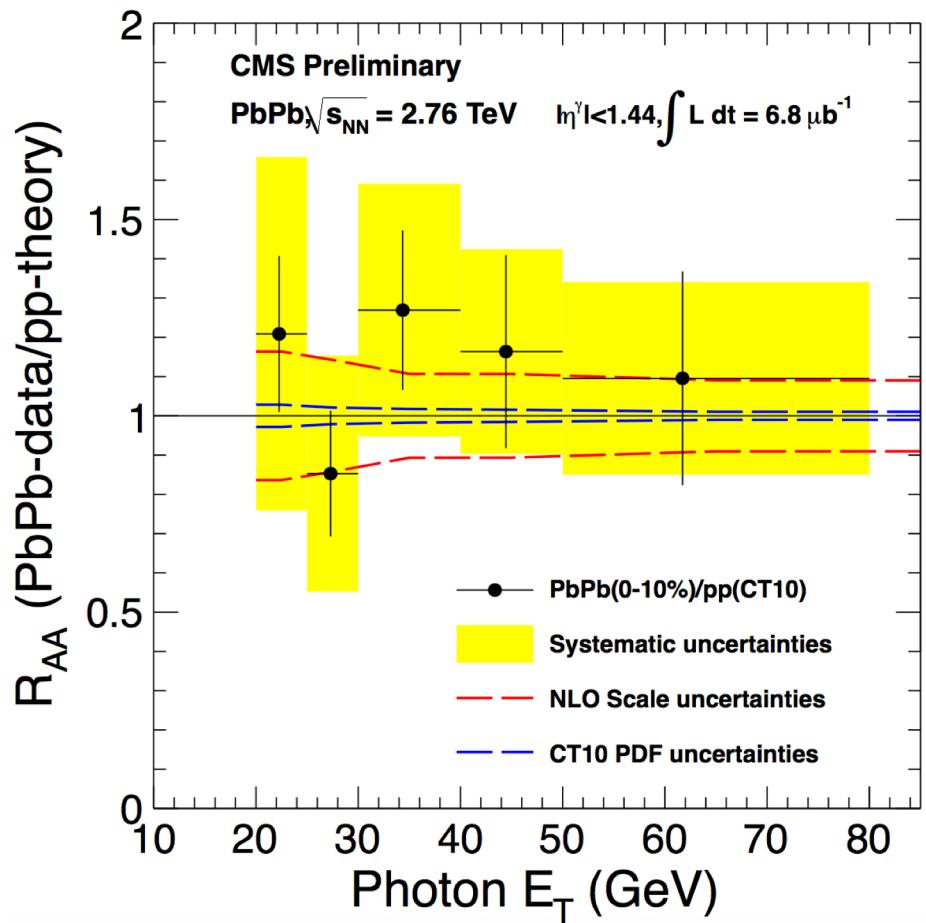
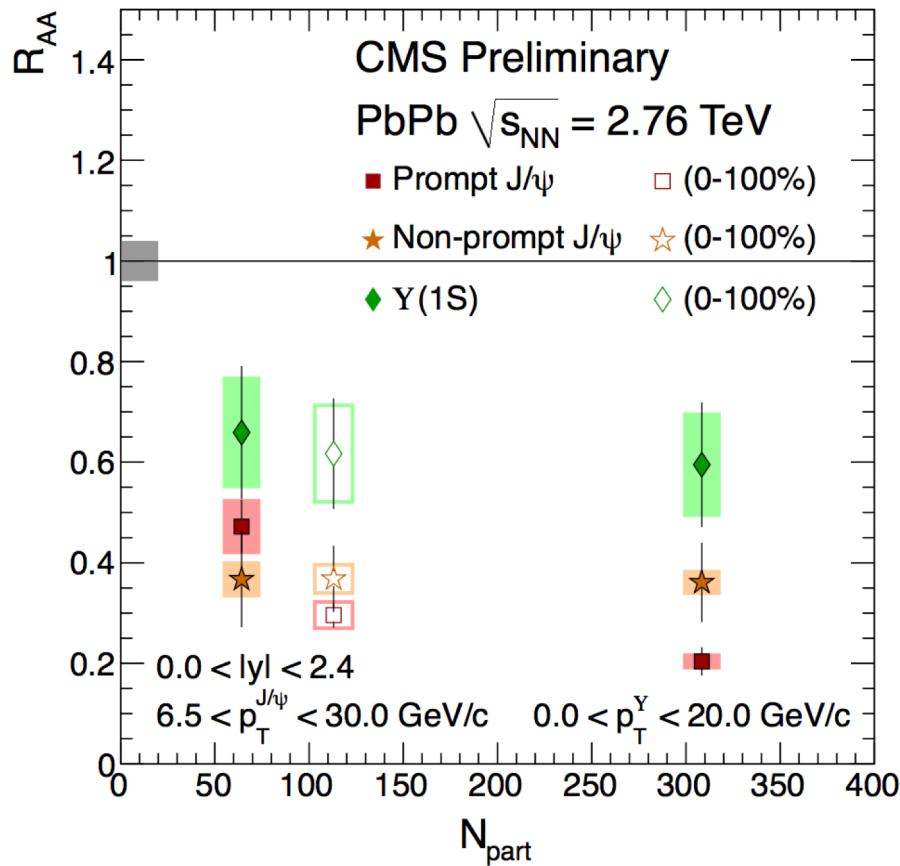
ALI-PREL-56005



Suppression of high- p_T hadrons at LHC

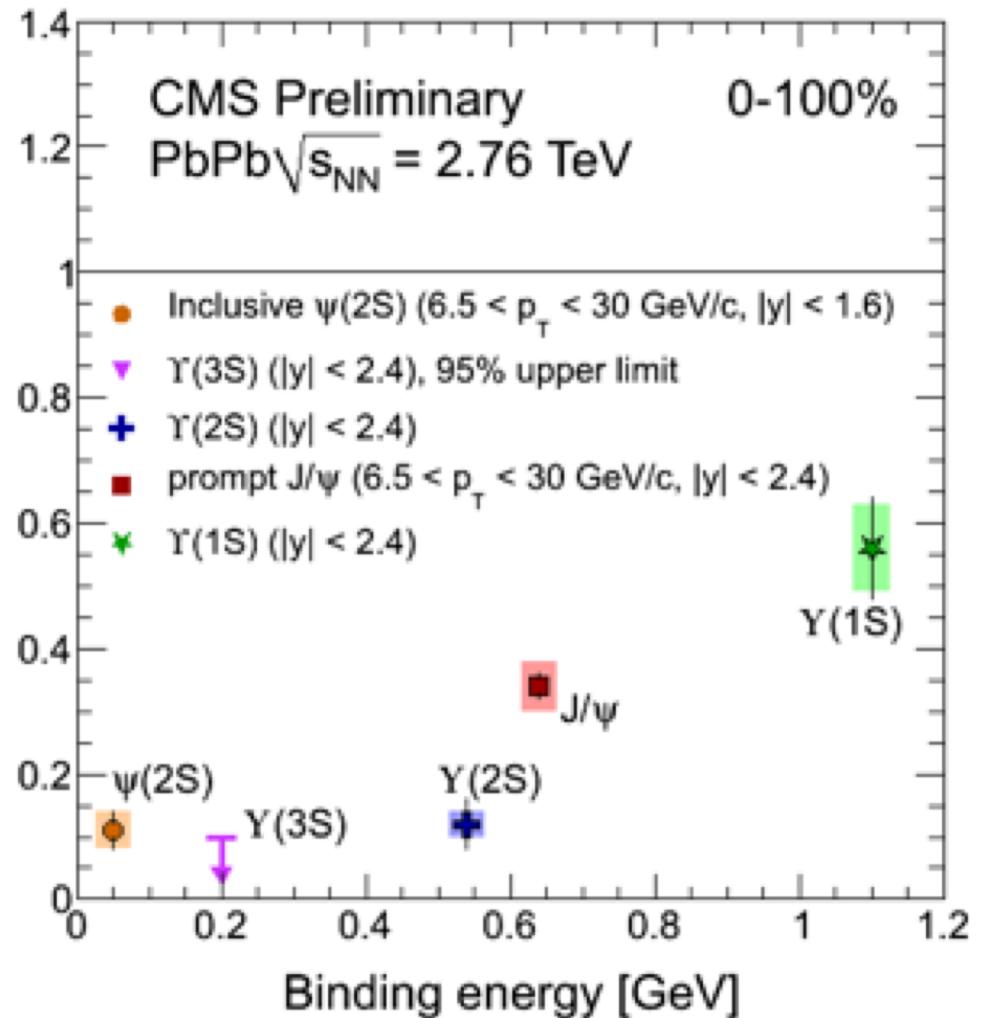
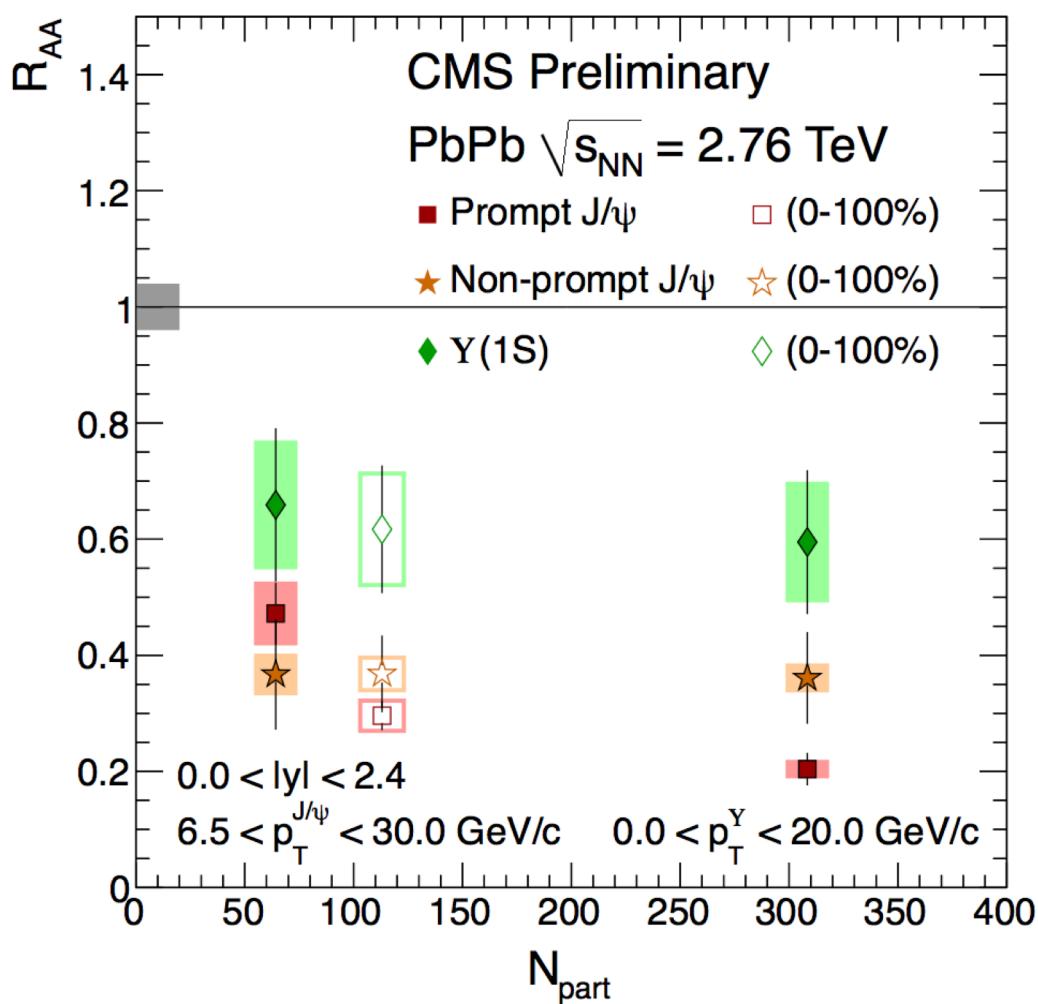
Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76 \text{ GeV}$



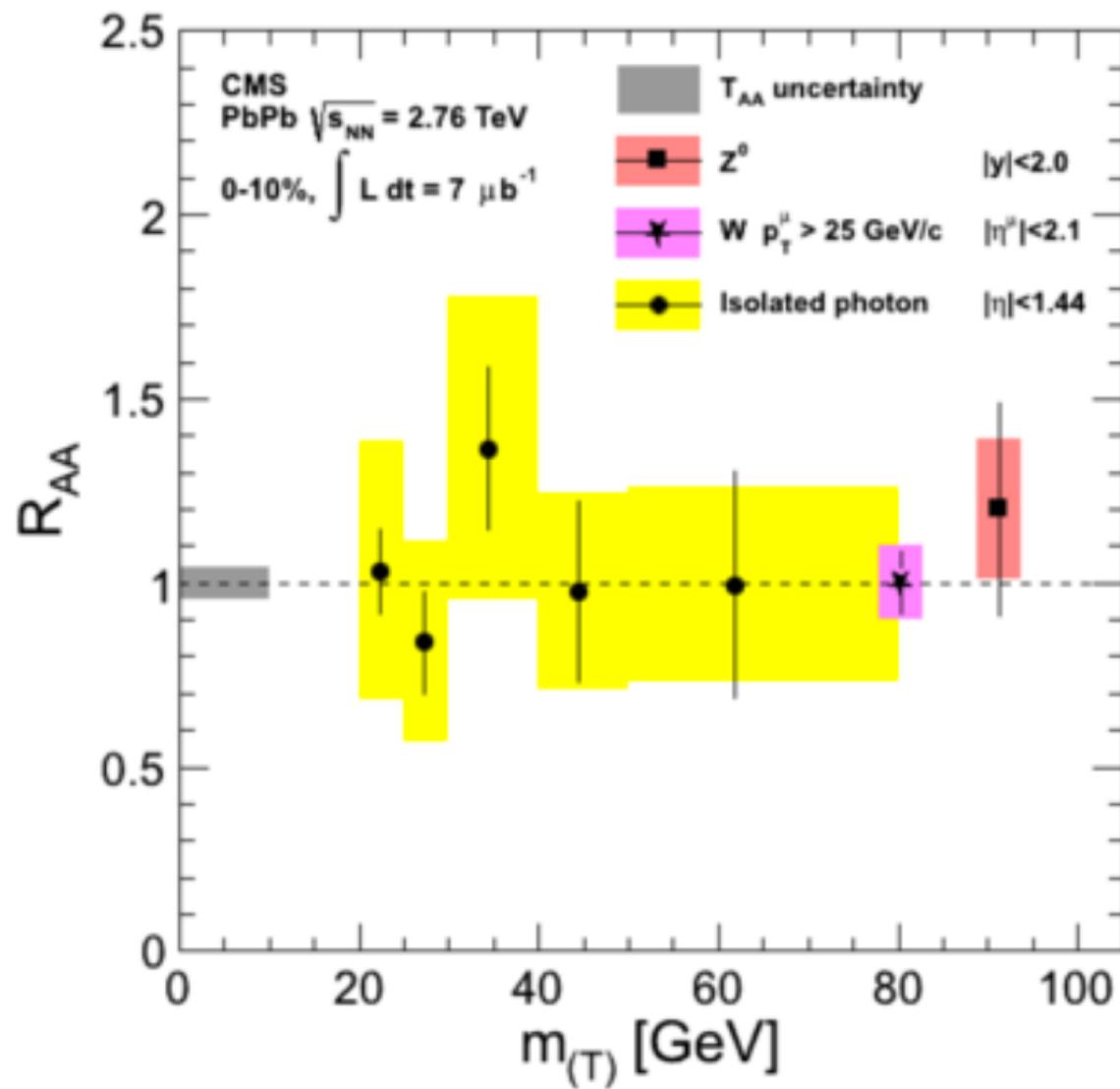


Suppression of high- p_T hadrons at LHC

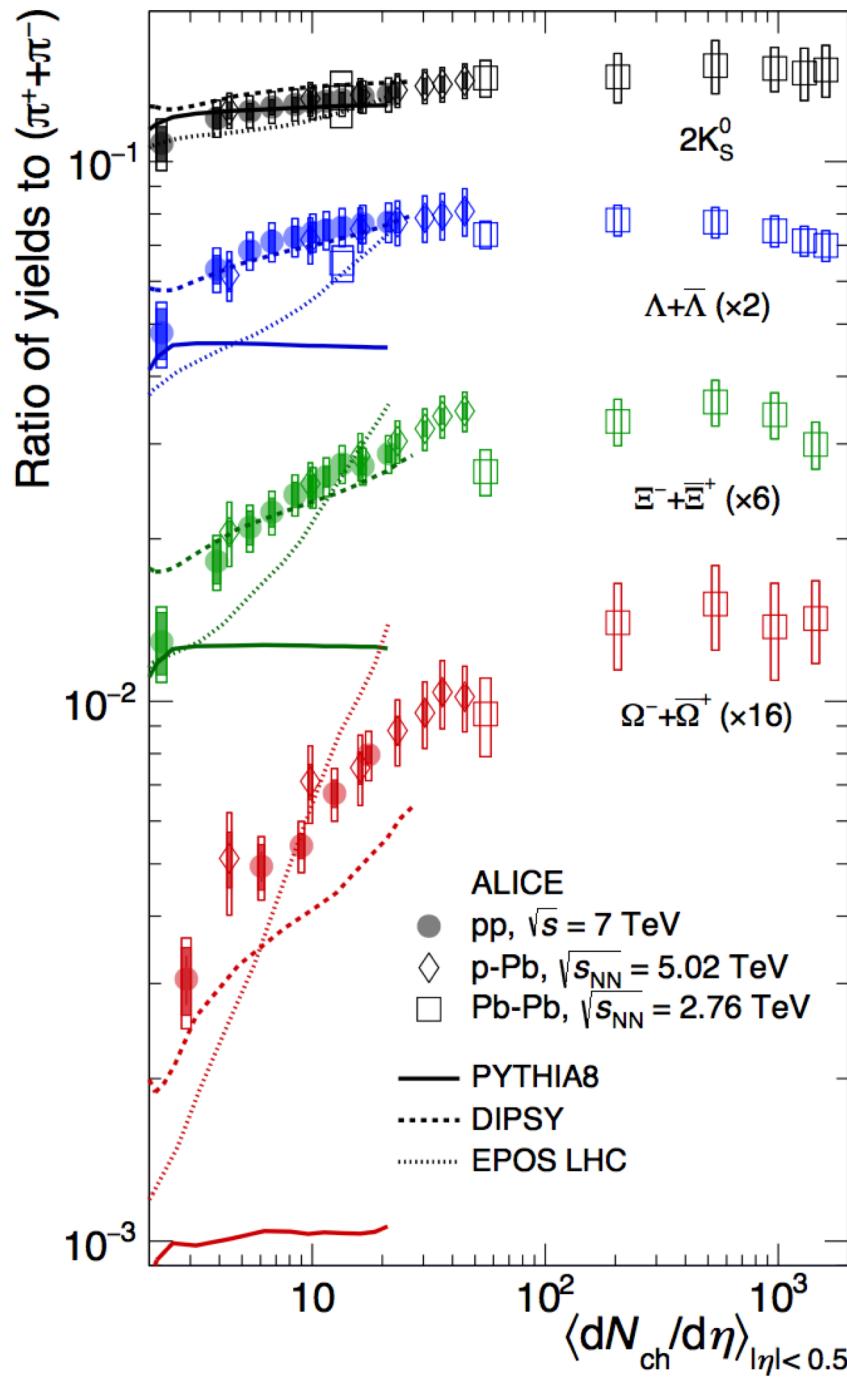
The suppression factors, as a function of the binding energy of the respective quarkonium state



Suppression of high- p_T hadrons at LHC



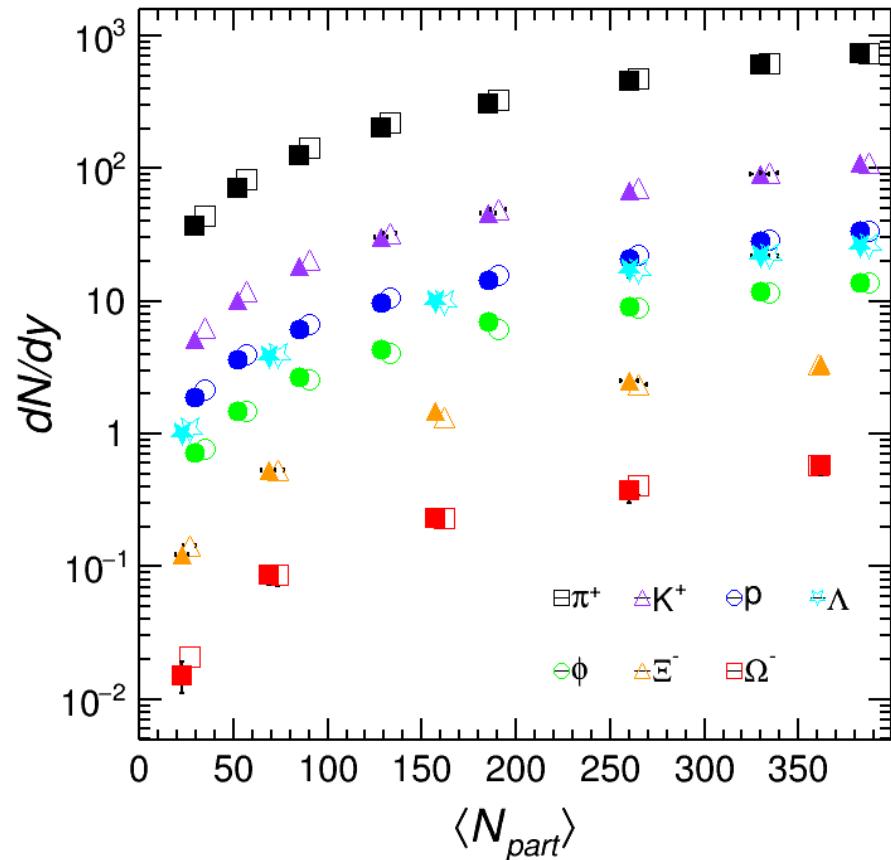
Strangeness enhancement at LHC



Core-Corona effect

$$\left(\frac{dN}{dy} \right)_i^{cen} = N_{part} [(1 - f_{core}) M_i^{ppMB} + f_{core} M_i^{core}]$$

$$M_i^{ppMB} = \frac{1}{2} (dN/dy)_i^{ppMB}$$



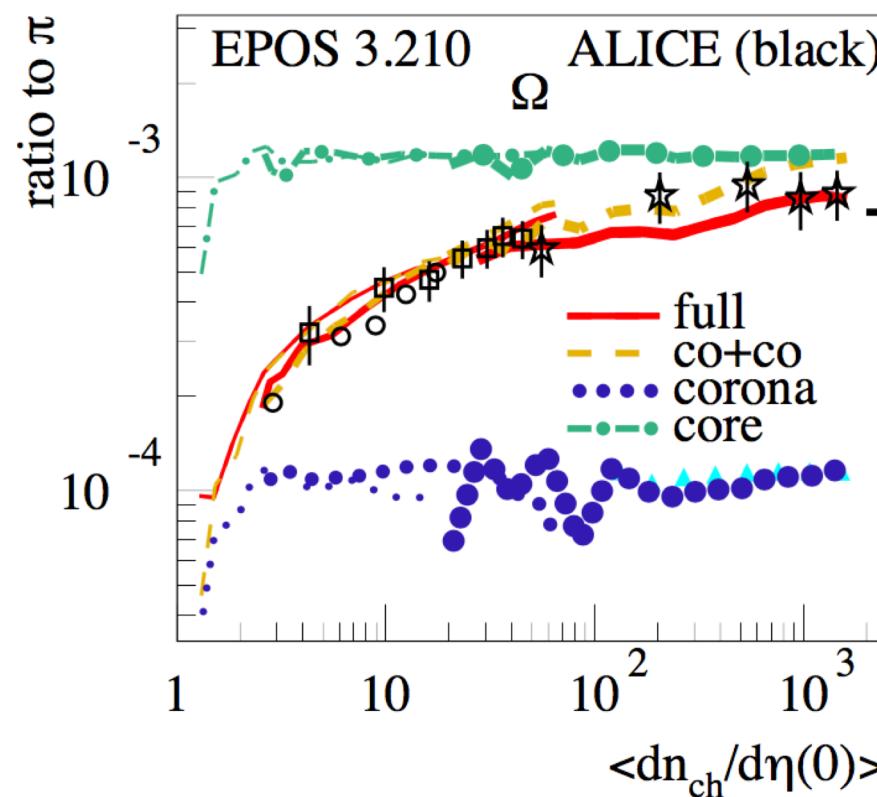
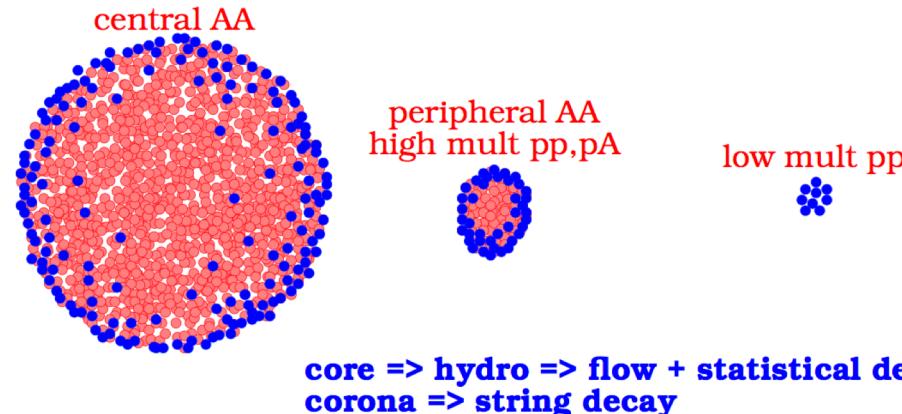
Core-corona in pp

Core-corona picture in EPOS

Phys.Rev.Lett. 98 (2007) 152301, Phys.Rev. C89 (2014) 6, 064903

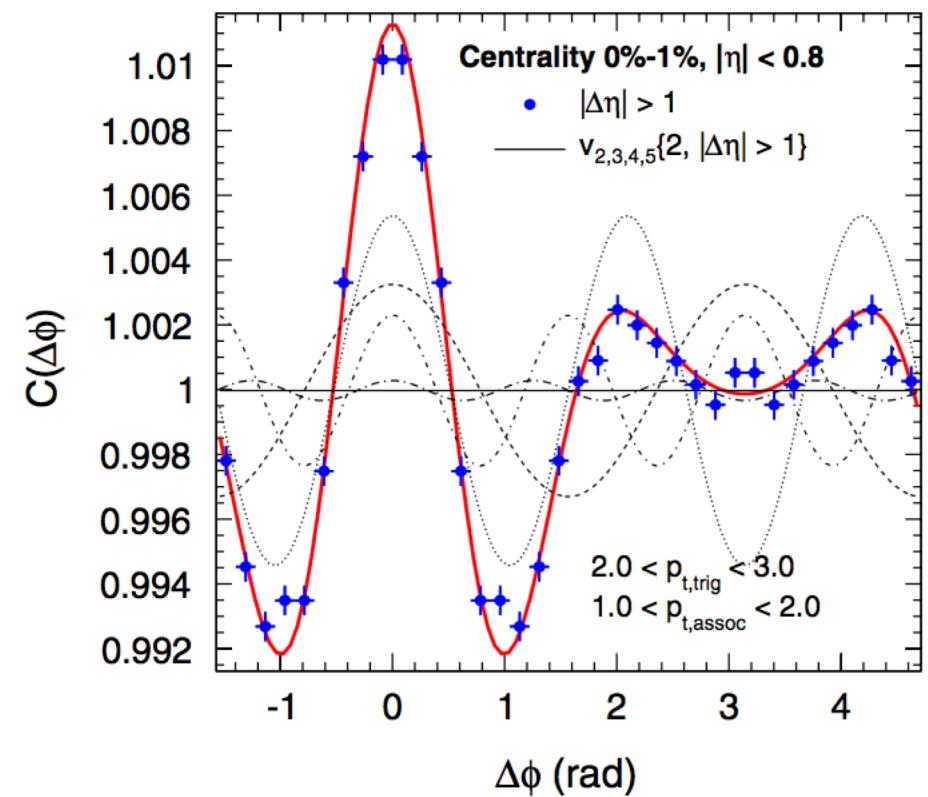
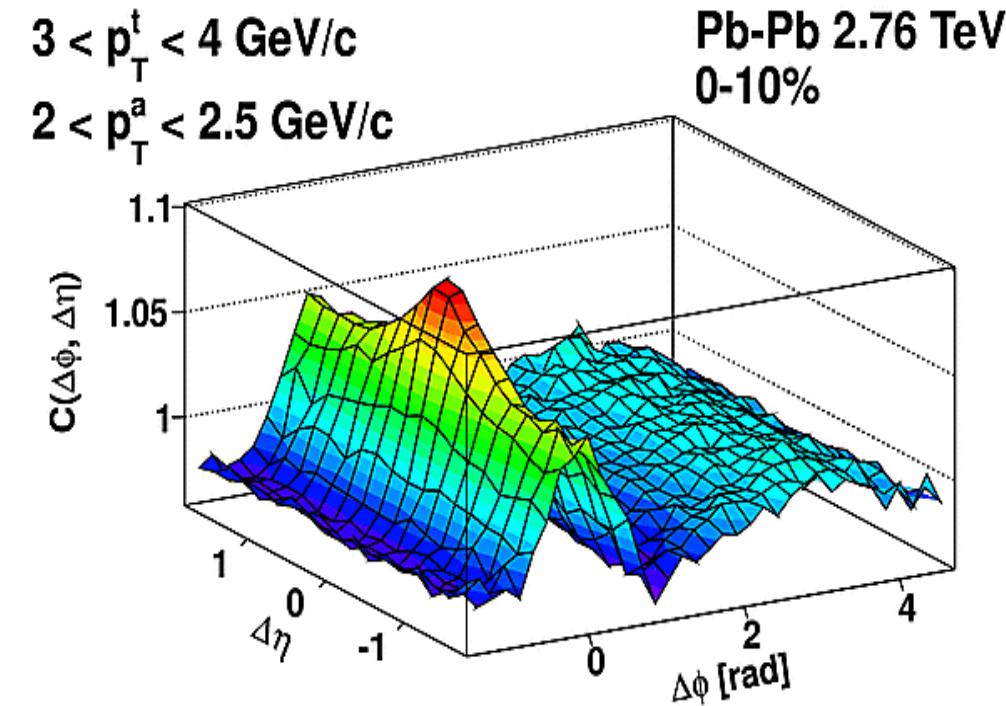
K. Werner, SQM 2017, July 10-15 2017, Utrecht

Gribov-Regge approach => (Many) kinky strings
=> core/corona separation (based on string segments)



thin lines = pp (7TeV)
intermediate lines = pPb (5TeV)
thick lines = PbPb (2.76TeV)
circles = pp (7TeV)
squares = pPb (5TeV)
stars = PbPb (2.76TeV)

Two-particle correlations at LHC

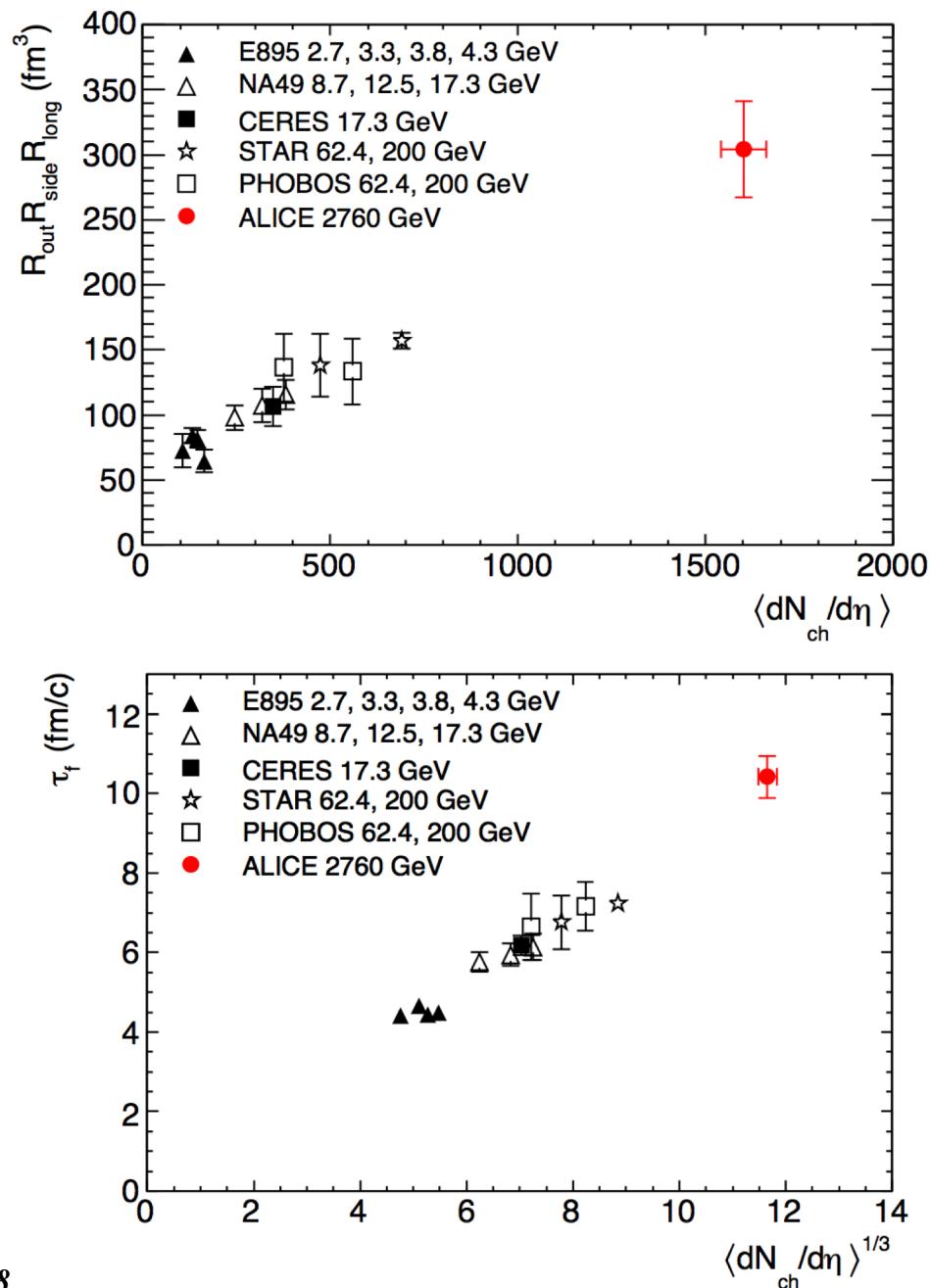
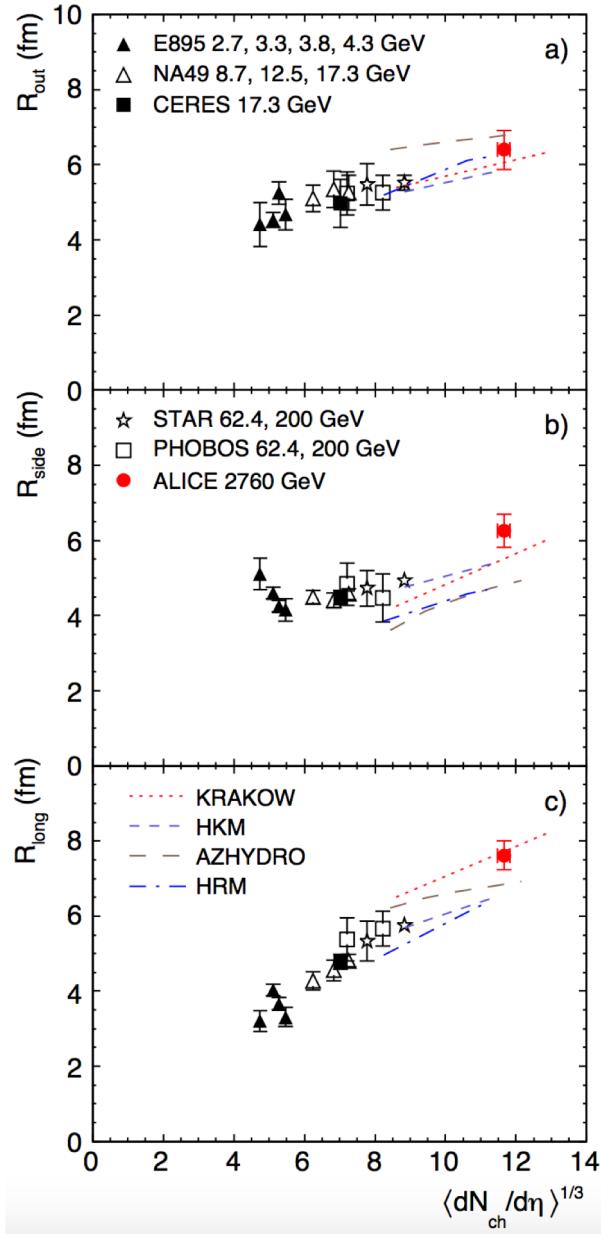


ALI-PUB-14107

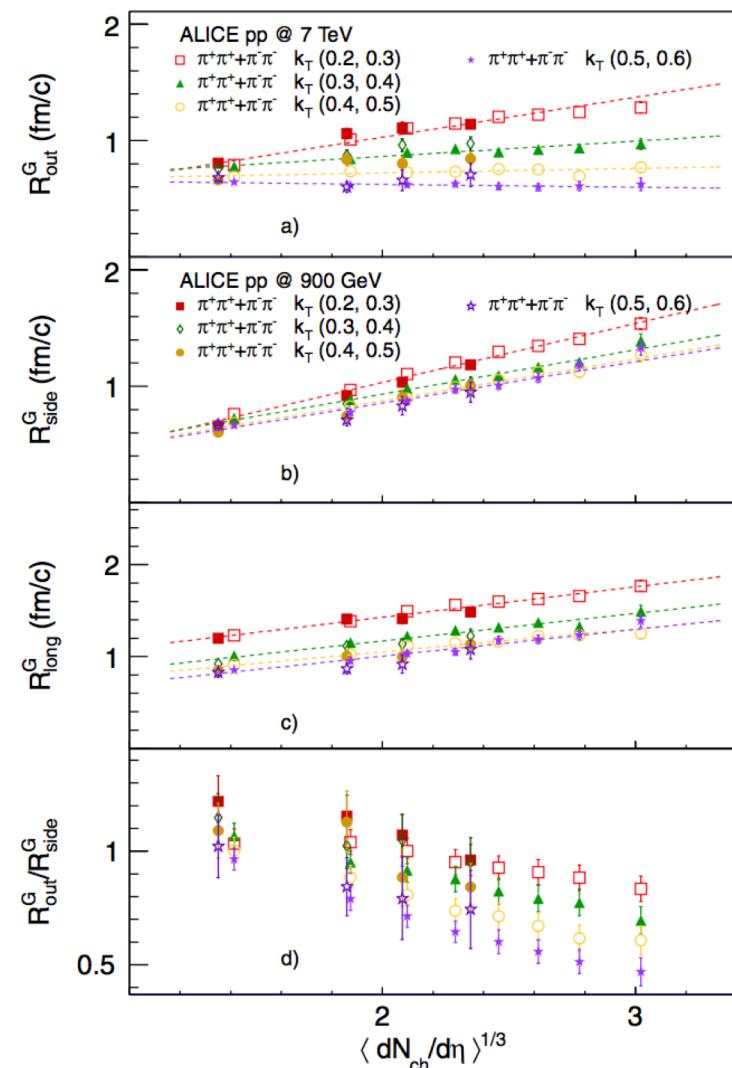
I.G.Altsybeev et al., ALICE Collaboration, arXiv:[nucl-ex]1611.10090

K.Aamodt et al., ALICE Collaboration Phys.Rev.Lett. 107(2011)032301

Bose-Einstein correlations at AGS, SPS, RHIC and LHC



Bose-Einstein correlations for pp collisions at LHC



$$C(\mathbf{q}) = A(\mathbf{q})/B(\mathbf{q})$$

- $A(\mathbf{q})$ measured two-particle distribution of a pair momentum difference

$$\mathbf{q} = \mathbf{p}_2 - \mathbf{p}_1$$

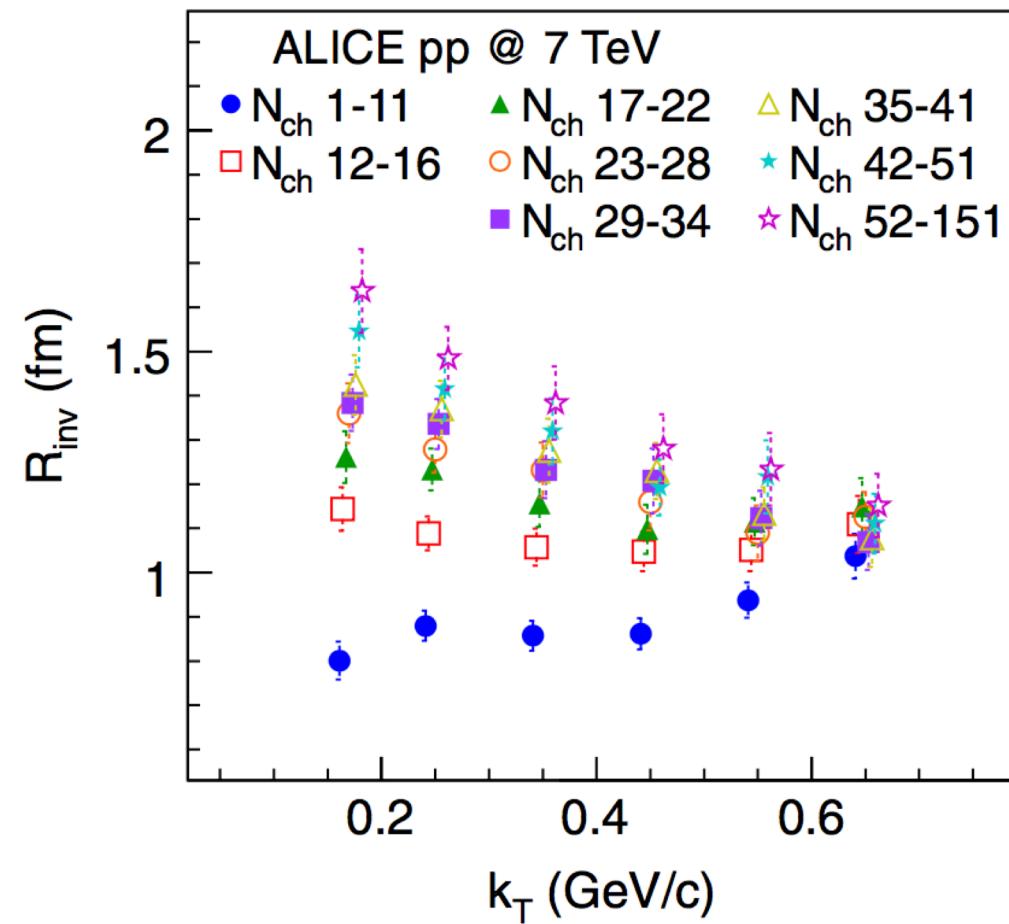
- $B(\mathbf{q})$ similar with $A(\mathbf{q})$ but for pairs from different event

$$k_T = |\mathbf{p}_{T,1} + \mathbf{p}_{T,2}|/2$$

q_{long} is parallel to

the beam, q_{out} is parallel to the pair transverse momentum,

and q_{side} is perpendicular to q_{long} and q_{out}



$$C(q_{inv}) = [((1-\lambda)+\lambda K(q_{inv})(1+\exp(-R_{inv}^2 q_{inv}^2))] B(q_{inv})$$

Bjorken energy density

$$\epsilon_{Bj} = \frac{dE_T}{dy} \frac{1}{S_T \tau}$$

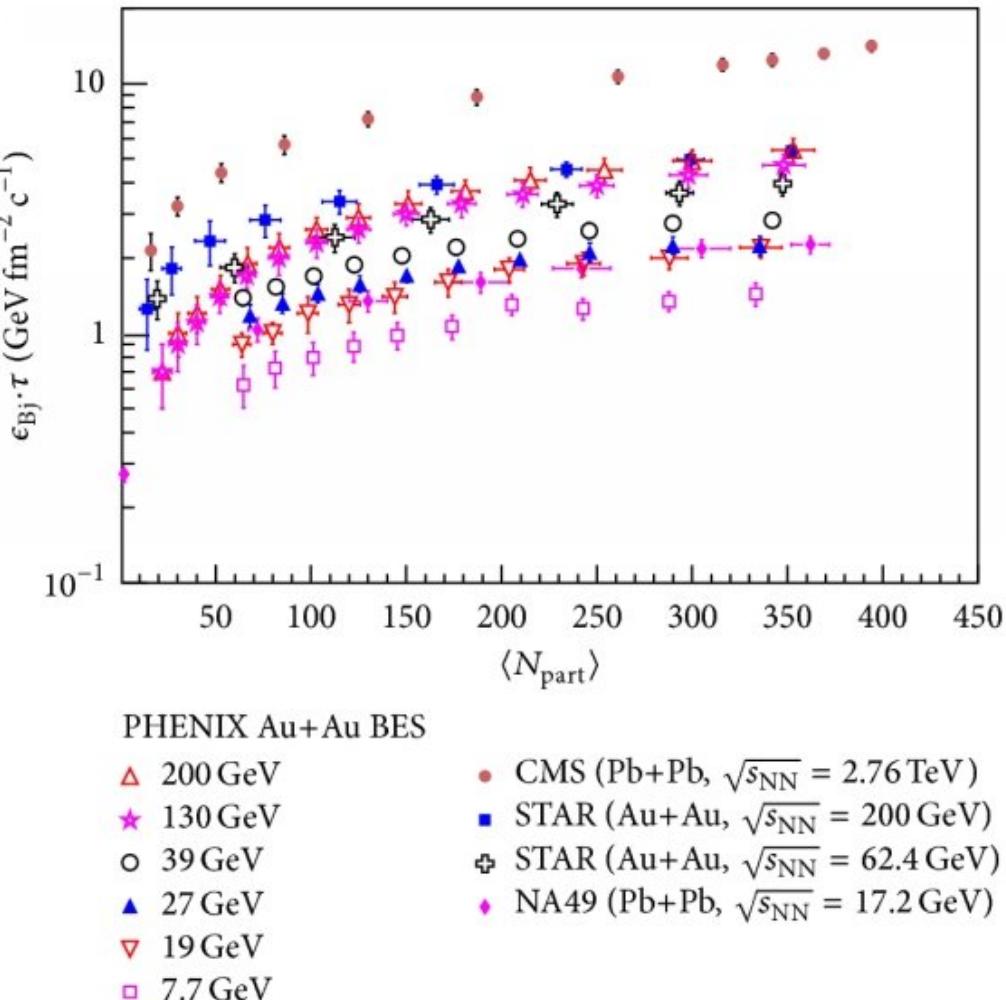
$$\frac{dE_T}{dy} \approx \frac{3}{2} (\langle m_T \rangle \frac{dN}{dy})_{\pi^\pm} + 2 (\langle m_T \rangle \frac{dN}{dy})_{K^\pm, p, \bar{p}}$$

$$\langle m_T \rangle = \sqrt{\langle p_T \rangle^2 + m_0^2}$$

$$\frac{dN}{dy} \simeq \frac{3}{2} \frac{dN^{(\pi^+ + \pi^-)}}{dy} + 2 \frac{dN^{(K^+ + K^-, p + \bar{p}, \Xi^- + \bar{\Xi}^+)}}{dy} + \frac{dN^{(\Lambda + \bar{\Lambda})}}{dy}$$

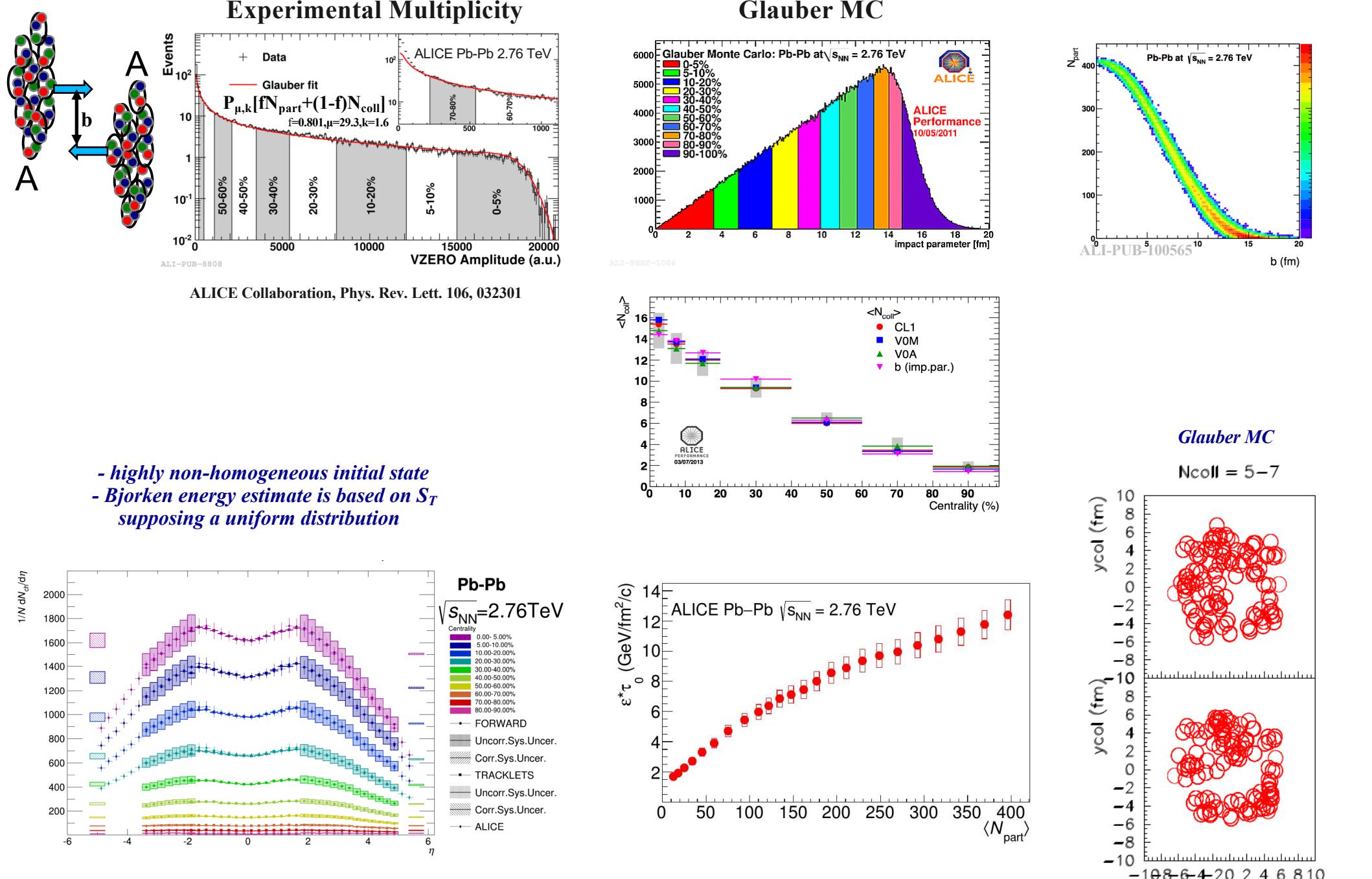
$$\frac{dN}{dy} \simeq \frac{3}{2} \frac{dN^{(\pi^+ + \pi^-)}}{dy} + 2 \frac{dN^{(K^+ + K^-, p + \bar{p}, \Xi^- + \bar{\Xi}^+)}}{dy} + \frac{dN^{(\Lambda + \bar{\Lambda}, \Omega^- + \bar{\Omega}^+)}}{dy}$$

$$\frac{dN}{dy} \simeq \frac{3}{2} \frac{dN^{(\pi^+ + \pi^-)}}{dy} + 2 \frac{dN^{(p + \bar{p}, \Xi^- + \bar{\Xi}^+)}}{dy} + \frac{dN^{(K^+ + K^-, K_S^0 + \bar{K}_S^0, \Lambda + \bar{\Lambda}, \Omega^- + \bar{\Omega}^+)}}{dy}$$



A few considerations

Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76 \text{ GeV}$



A few considerations

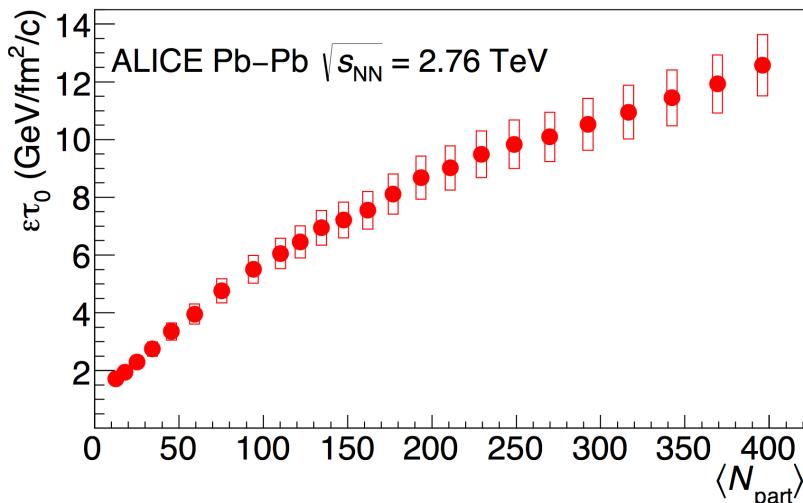
$$\varepsilon_{Bj} = \frac{dE_T}{dy} \frac{1}{S_T \tau}$$

Bjorken energy density - Pb+Pb

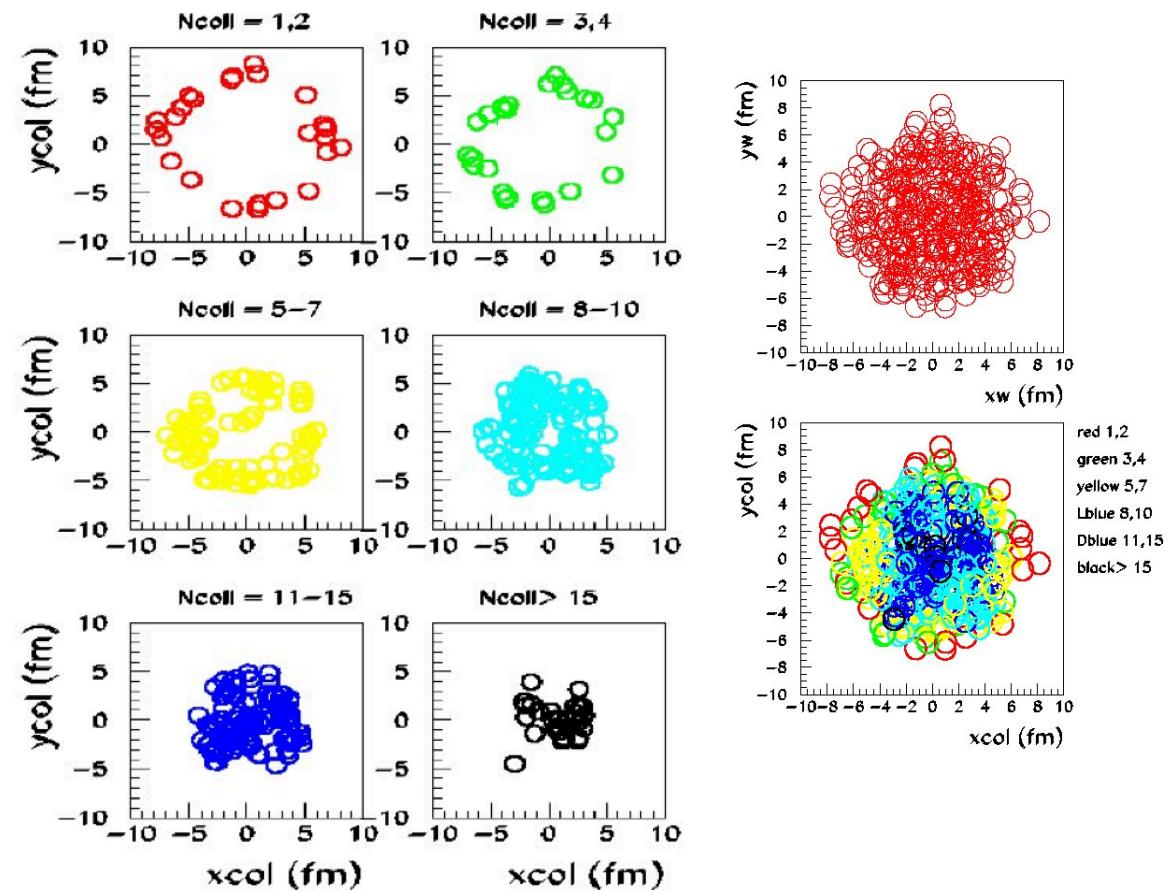
$$\frac{dE_T}{dy} \approx \frac{3}{2} (\langle m_T \rangle \frac{dN}{dy})_{\pi^\pm} + 2 (\langle m_T \rangle \frac{dN}{dy})_{K^\pm, p, \bar{p}} \quad \langle m_T \rangle = \sqrt{\langle p_T \rangle^2 + m_0^2}$$

Pb+Pb $\sqrt{s_{NN}} = 2.76 \text{ TeV}$

Glauber MC, b=0

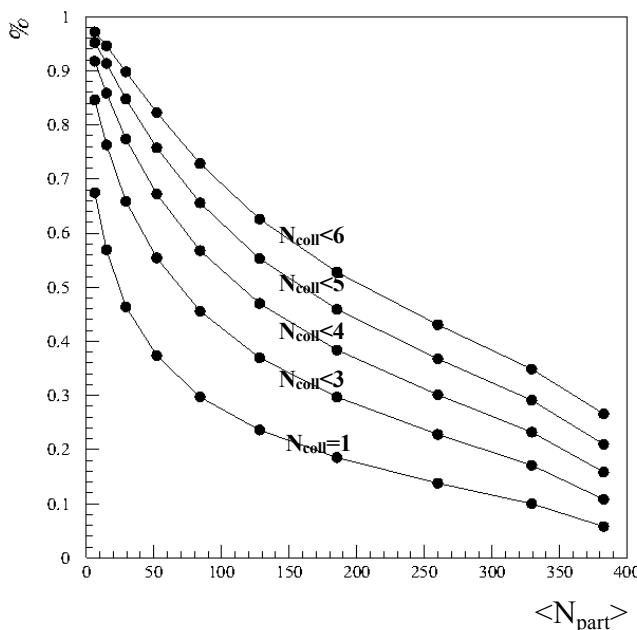
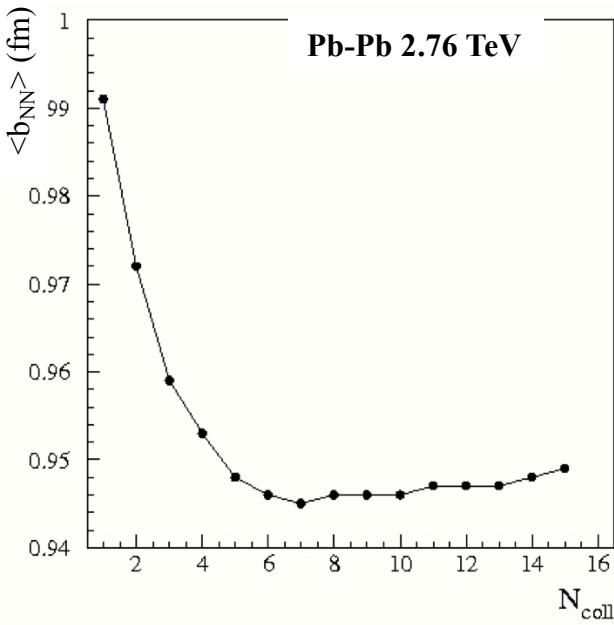


J.Adam et al., ALICE Coll., CERN-EP-2016-071 11 March 2016



A few considerations Core-Corona effect

Glauber MC



How should we define “Corona”?

F.Becattini, J.Manninen, J.Phys.G 35 (2008) 104013, Phys.Lett.B 673(2009)19

J.Aichelin, K.Werner, Phys.Rev.C 79(2009)064907,

J.Phys.G 37(2010)094006,

Phys.Rev.C 82(2010)034906

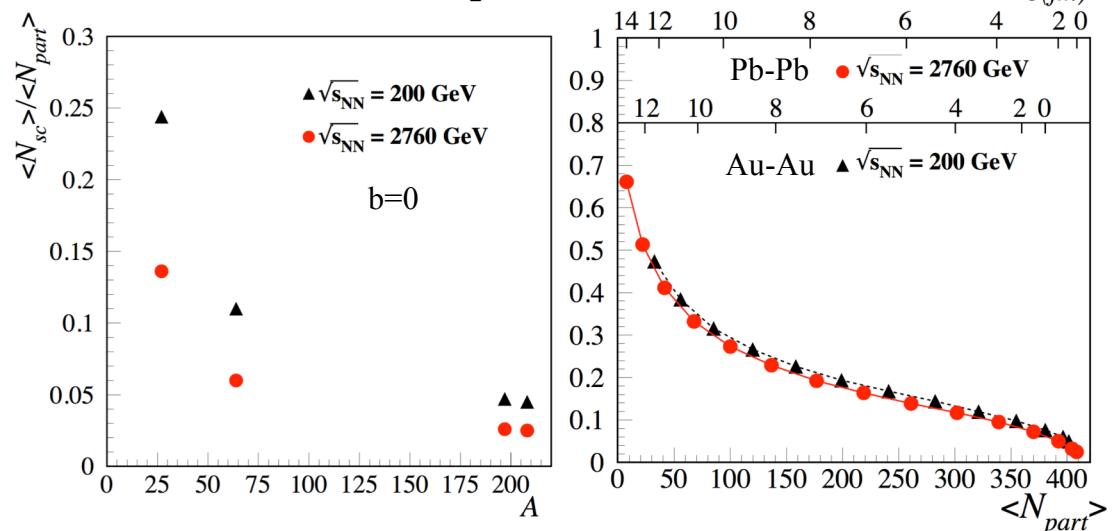
P.Bozek, Phys.Rev.C 79 (2009) 054901

C.Schreiber, K.Werner, J.Aichelin, Phys.Atom.Nucl. 75(2012)640

M.Gemard and J.Aichelin, Astron.Nachr. 335(2014)660

$$\left(\frac{dN}{dy} \right)_i^{cen} = N_{part} [(1 - f_{core}) M_i^{ppMB} + f_{core} M_i^{core}]$$

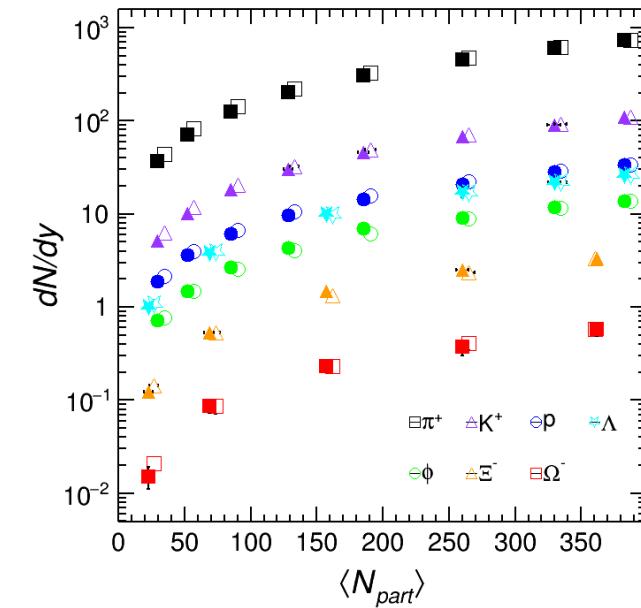
$$M_i^{ppMB} = \frac{1}{2} (dN/dy)_i^{ppMB}$$



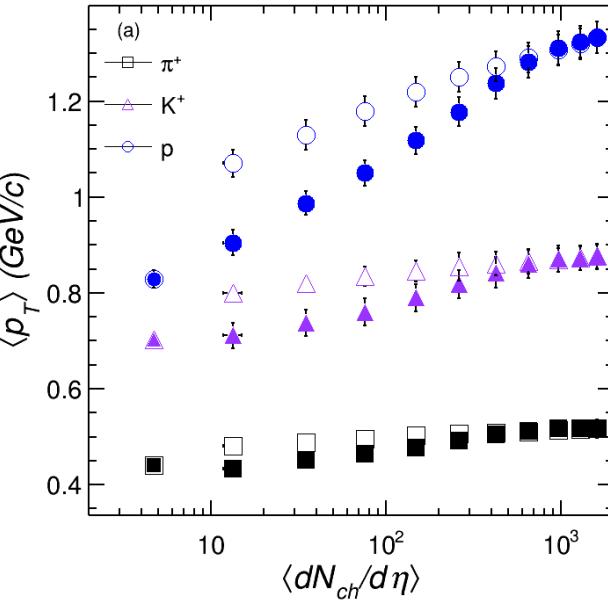
A few considerations Core-Corona effect

$$\left(\frac{dN}{dy}\right)_i^{cen} = N_{part}[(1 - f_{core})M_i^{ppMB} + f_{core}M_i^{core}] \quad (1)$$

$$M_i^{ppMB} = \frac{1}{2}(dN/dy)_i^{ppMB} \quad (2)$$

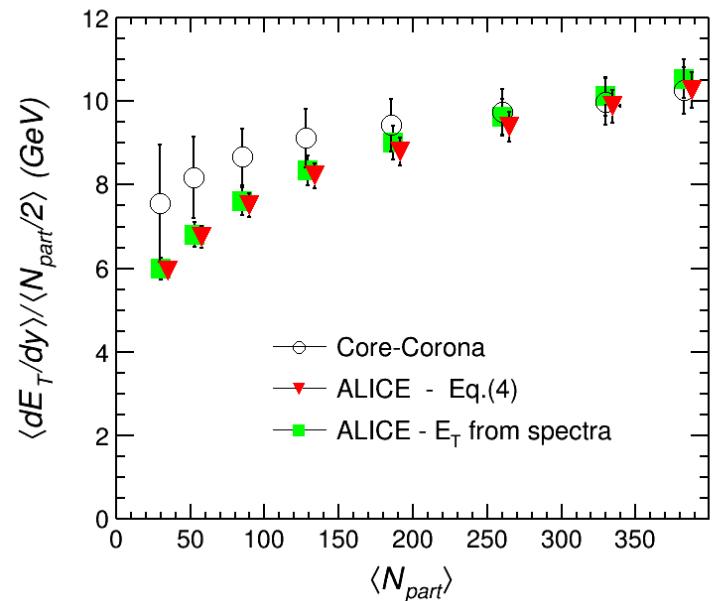


$$\langle p_T \rangle_i^{cen} = \frac{f_{core} \langle p_T \rangle_i^{core} M_i^{core} + (1 - f_{core}) \langle p_T \rangle_i^{ppMB} M_i^{ppMB}}{f_{core} M_i^{core} + (1 - f_{core}) M_i^{ppMB}} \quad (3)$$



$$\frac{dE_T}{dy} \approx 3 \left(\frac{dE_T}{dy} \right)_{\pi^+} + 4 \left(\frac{dE_T}{dy} \right)_{K^+, p, \Xi^-} + 2 \left(\frac{dE_T}{dy} \right)_{\Lambda, \Omega^-} \quad (4)$$

$$\frac{dE_T}{dy} = \langle m_T \rangle \frac{dN}{dy} \quad \langle m_T \rangle = \sqrt{\langle p_T \rangle^2 + m^2}$$



ALICE Coll., Phys.Rev. C88(2013)044910

ALICE Coll., Phys.Rev.Lett 111(2013)222301

ALICE Coll., Phys.Lett. B728(2014)216

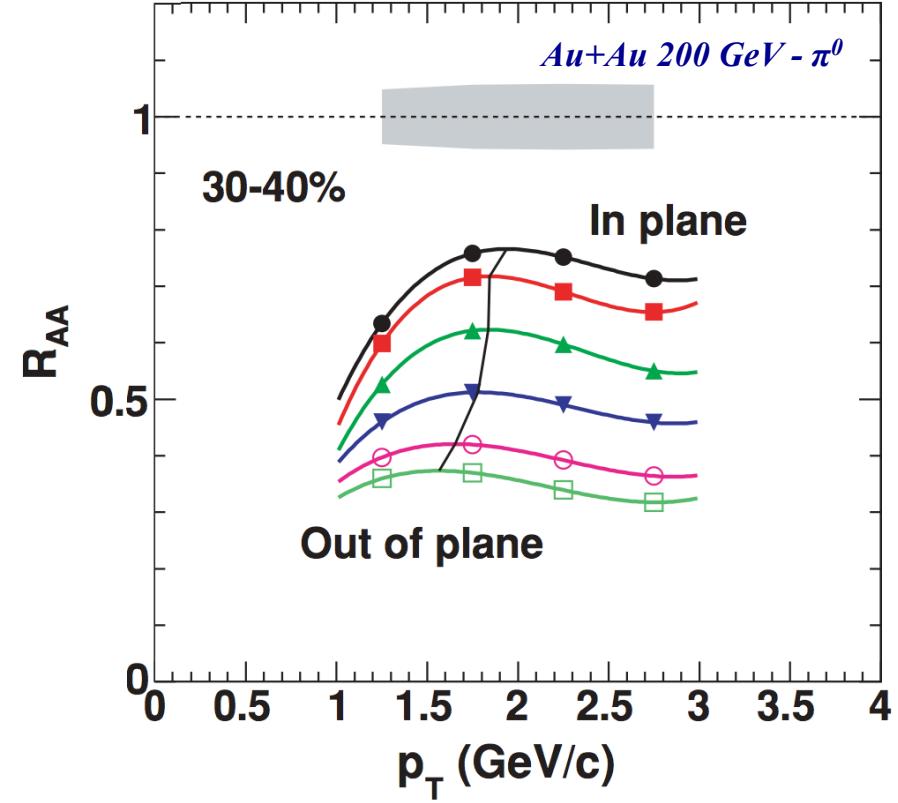
ALICE Coll., Phys.Rev. C91(2015)024609

M. Petrovici, I. Berceanu, A. Pop, M. Târzila, and C. Andrei, Phys.Rev. C96(2017)014908

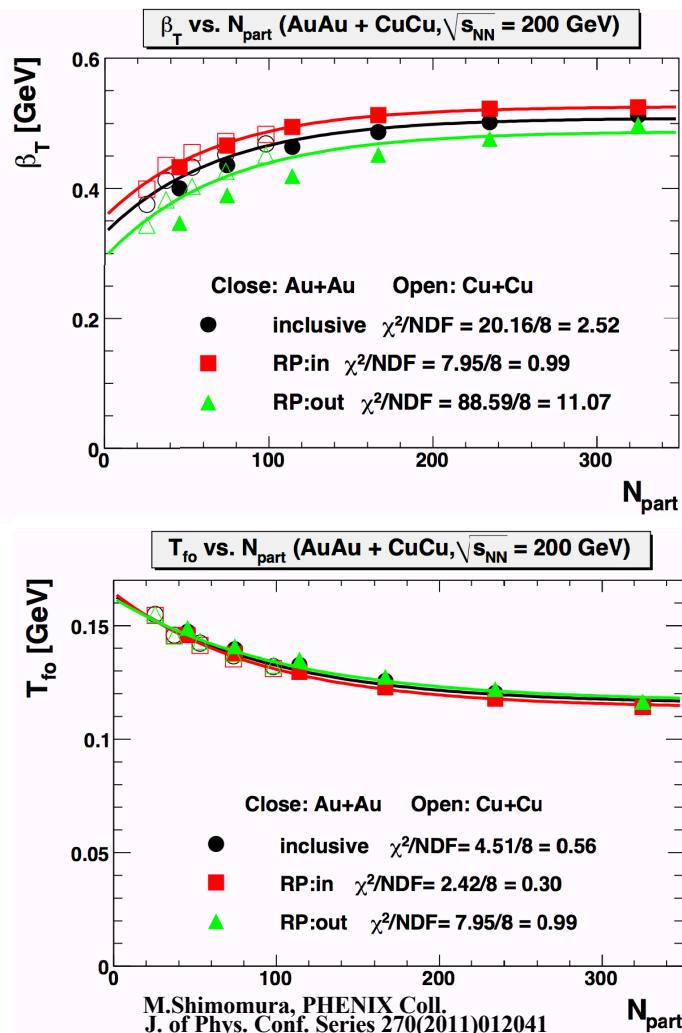
*Which is the source of difference between
Core-Corona in $\langle p_T \rangle$ and ratio of normalized p_T distributions
relative to*

Core-Corona in yields ?

*Core $\langle p_T \rangle$ and ratio of normalized p_T distributions is fireball shape dependent
Which is not included in the simple anzatz used up to now !!!*

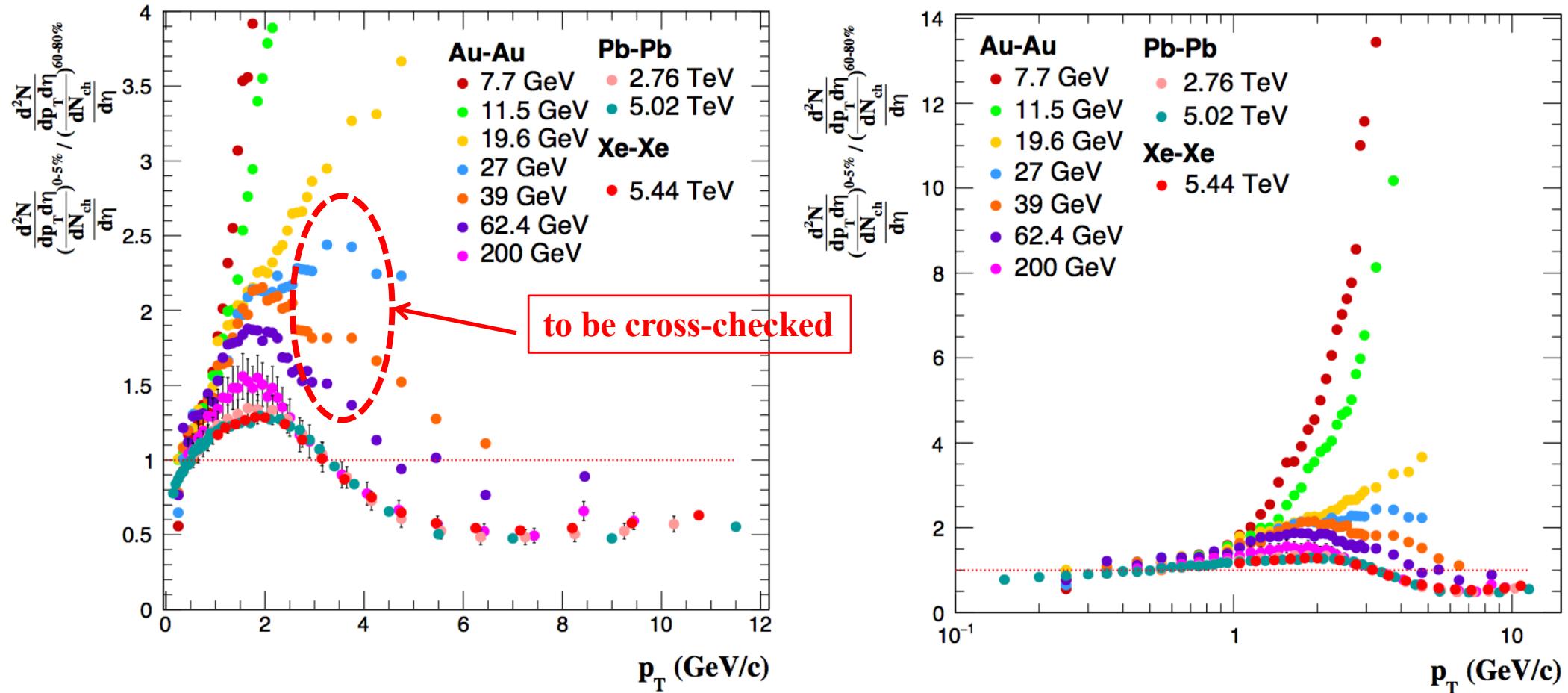


PHENIX Coll. Phys.Rev. C80(2009)054907



Could we extract something similar
using v2 analysis in Pb-Pb @ LHC ???

$(0\text{-}5\%)/(60\text{-}80\%)$ - collision energy dependence



- at $p_T > \sim 2\text{-}2.5 \text{ GeV}/c$ - no difference between 200 GeV - 2.76(5.02)TeV
- at $\sim 27 \text{ GeV}$ at $p_T \sim 3\text{-}4 \text{ GeV}/c$ - a leveling off sets in
- >39 GeV a maximum appears at p_T values decreasing with the collision energy expansion - “suppression” competition ? - it stays at the same p_T value starting from 200 GeV

A few considerations

Geometrical scaling

**Local parton-hadron duality picture
and dimensionality argument**

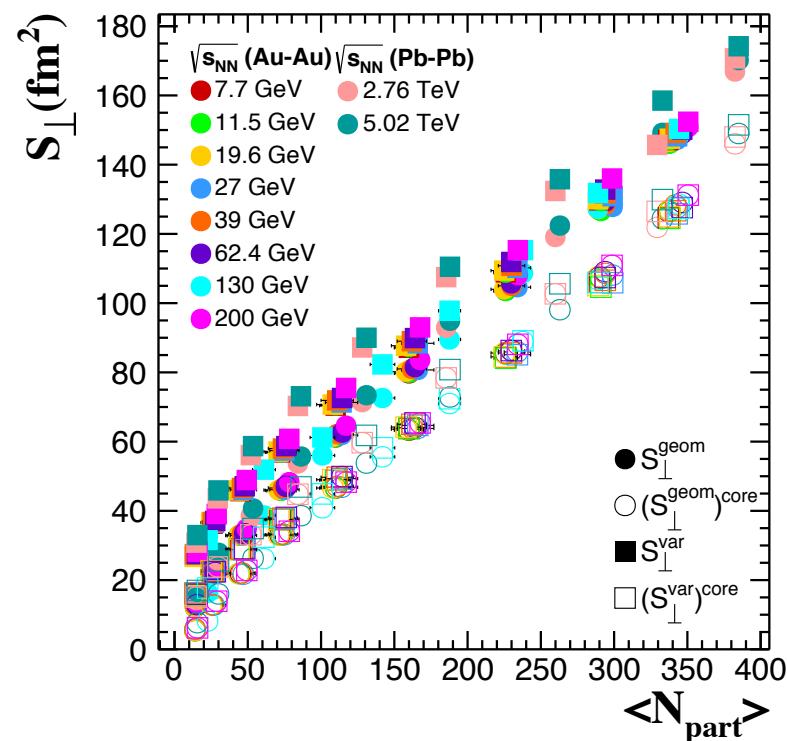
$$\langle p_T \rangle / \sqrt{\frac{dN}{dy} / S_\perp} \sim \frac{1}{n\sqrt{n}}$$

n - no. of charged
part. from a
gluon fragmentation

- Y.L.Dokshitzer, V.A.Khoze and S.Trojan, J.Phys.G 17 (1991) 1585
- T. Lappi, Eur.Phys.J. C71 (2011) 1699
- E. Levin and A.H. Rezaeian, Phys.Rev.D 83 (2011) 114001

S_{perp} & dN/dy estimates

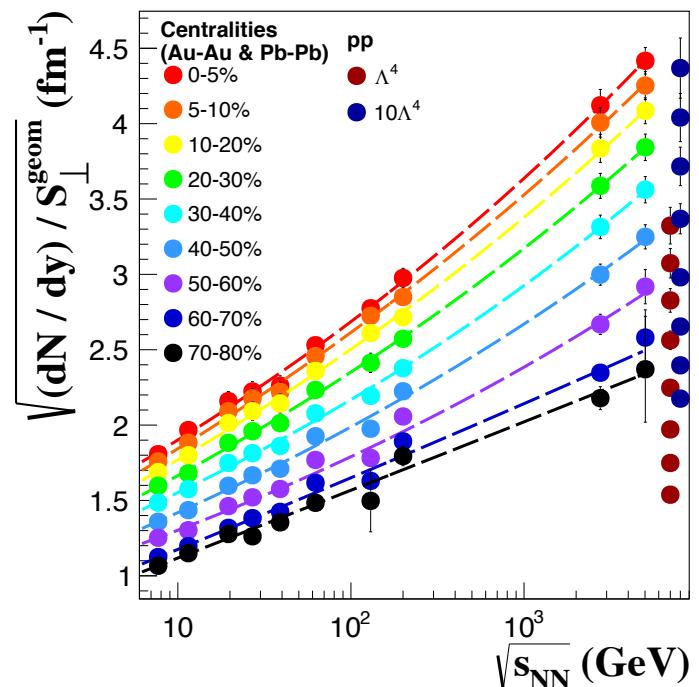
Glauber Monte Carlo approach



$$S_\perp^{\text{var}} \sim \pi \sqrt{\sigma_x^2 \sigma_y^2 - \sigma_{xy}^2}$$

BES
RHIC
62.4; 130; 200 GeV
LHC

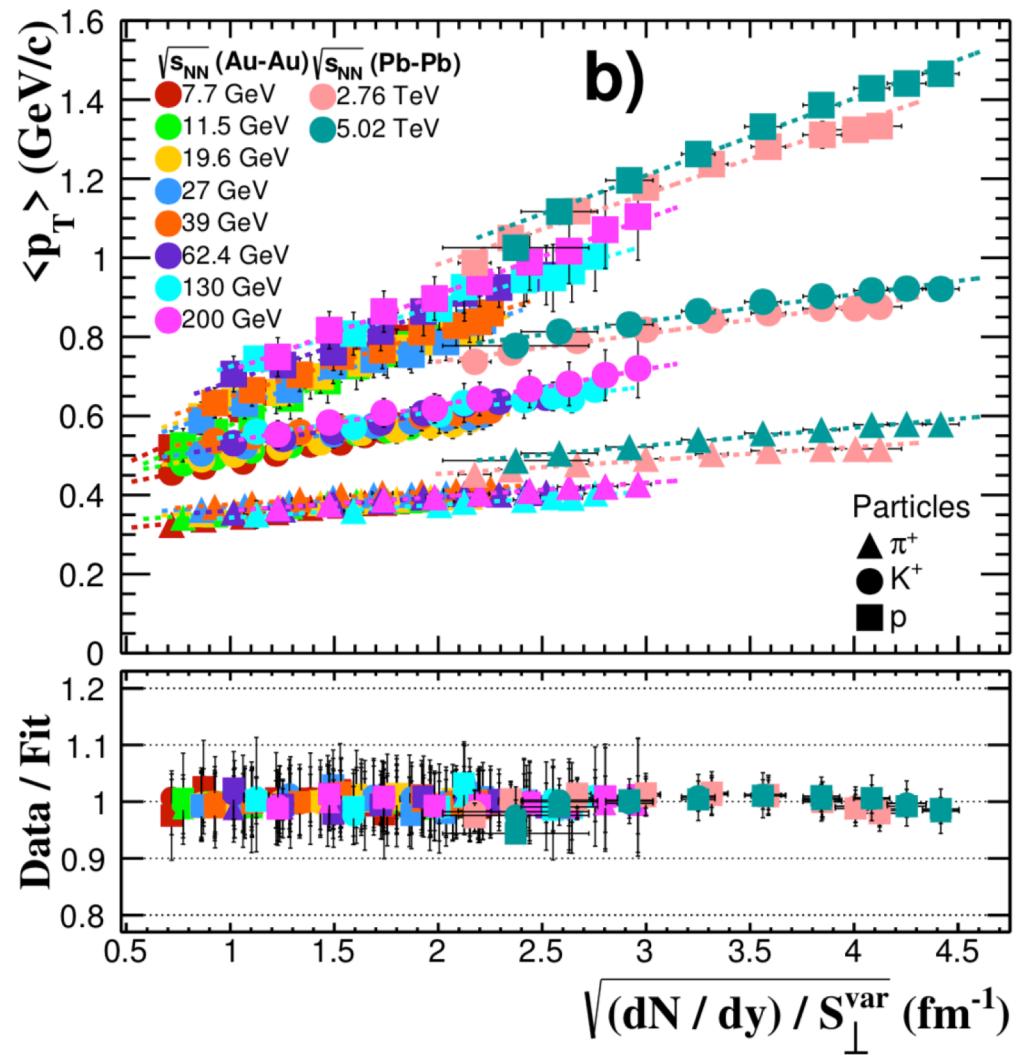
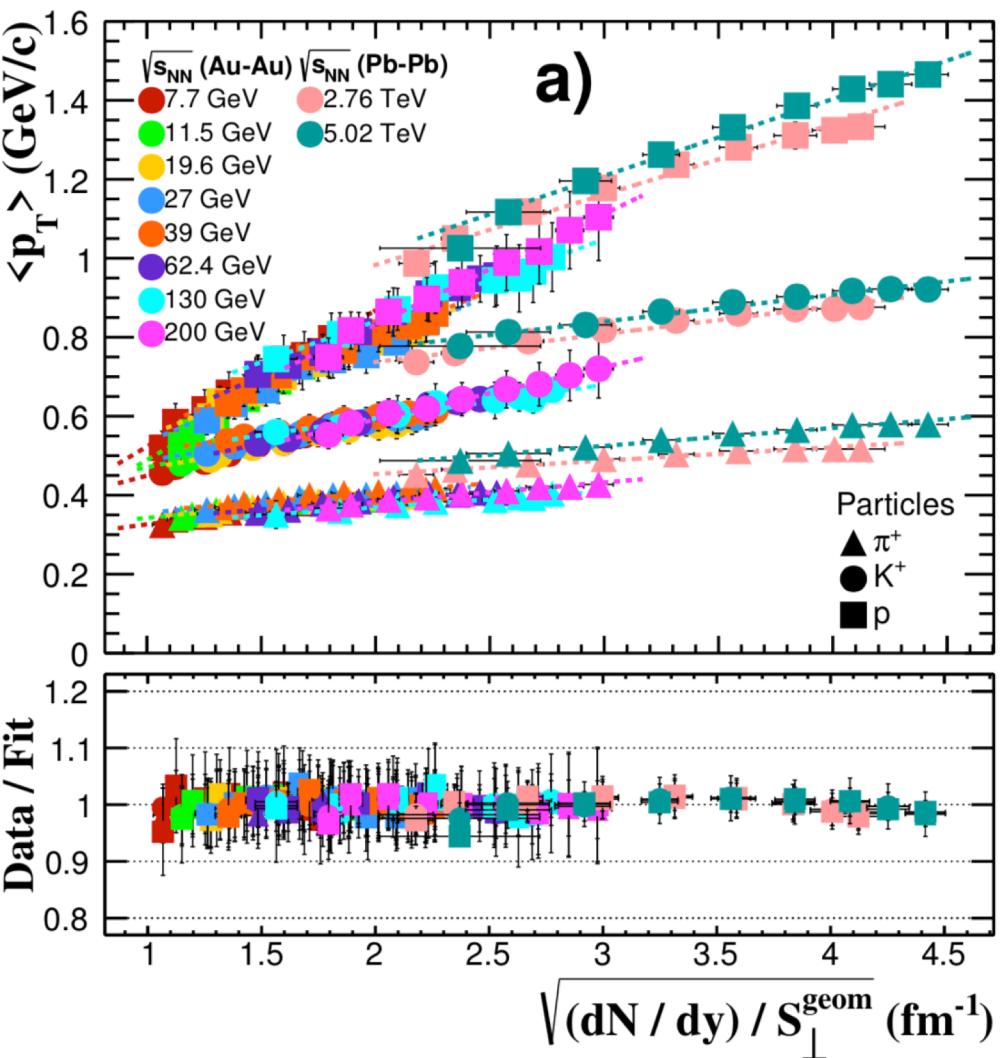
$$\begin{aligned} \frac{dN}{dy} &\simeq \frac{3}{2} \frac{dN^{(\pi^+ + \pi^-)}}{dy} + 2 \frac{dN^{(K^+ + K^-, p + \bar{p}, \Xi^- + \bar{\Xi}^+)}}{dy} + \frac{dN^{(\Lambda + \bar{\Lambda})}}{dy} \\ \frac{dN}{dy} &\simeq \frac{3}{2} \frac{dN^{(\pi^+ + \pi^-)}}{dy} + 2 \frac{dN^{(K^+ + K^-, p + \bar{p}, \Xi^- + \bar{\Xi}^+)}}{dy} + \frac{dN^{(\Lambda + \bar{\Lambda}, \Omega^- + \bar{\Omega}^+)}}{dy} \\ \frac{dN}{dy} &\simeq \frac{3}{2} \frac{dN^{(\pi^+ + \pi^-)}}{dy} + 2 \frac{dN^{(p + \bar{p}, \Xi^- + \bar{\Xi}^+)}}{dy} + \frac{dN^{(K^+ + K^-, K_S^0 + \bar{K}_S^0, \Lambda + \bar{\Lambda}, \Omega^- + \bar{\Omega}^+)}}{dy} \end{aligned}$$



A few considerations

Geometrical scaling

$\langle p_T \rangle$ vs. $[(dN/dy)/S_{\perp}^{\text{geom}}]^{1/2}$



STAR Collaboration, Phys.Rev. C96(2017)044904

STAR Collaboration, Phys.Rev. C79(2009)034909

ALICE Collaboration, Phys.Rev. C 88 (2013) 044910

ALICE Collaboration, Phys.Rev.Lett. 116(2016)222302

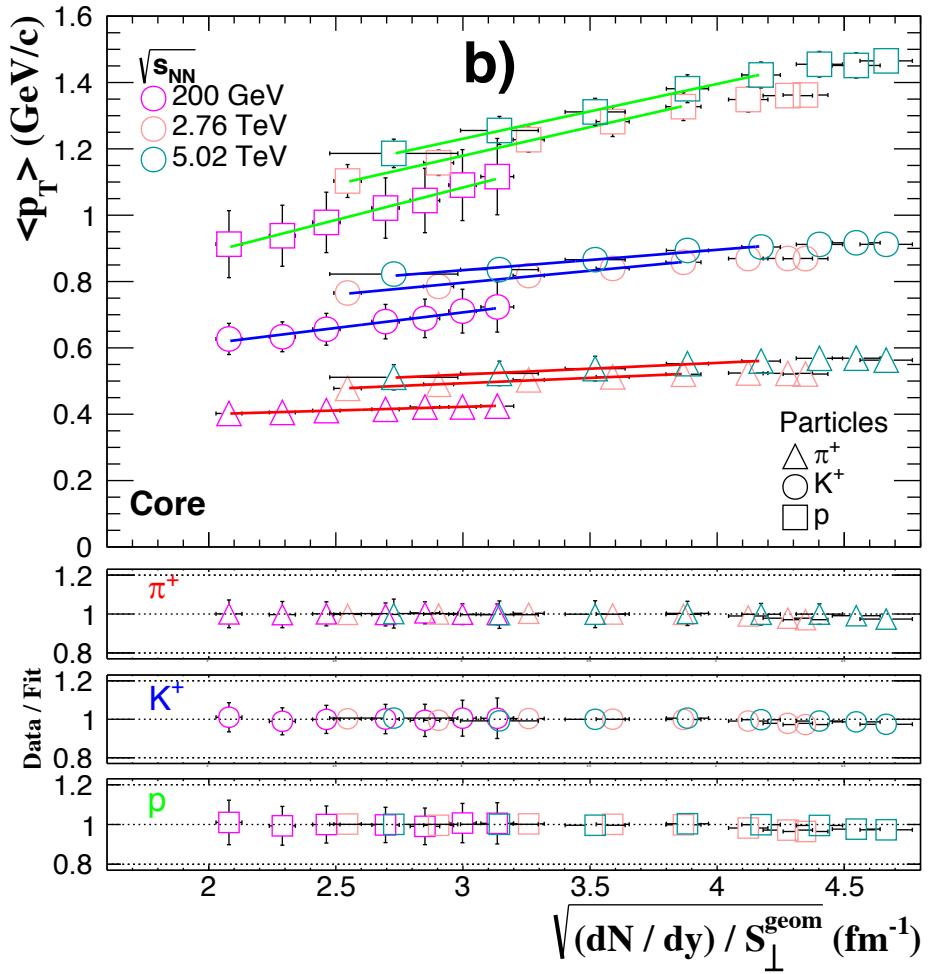
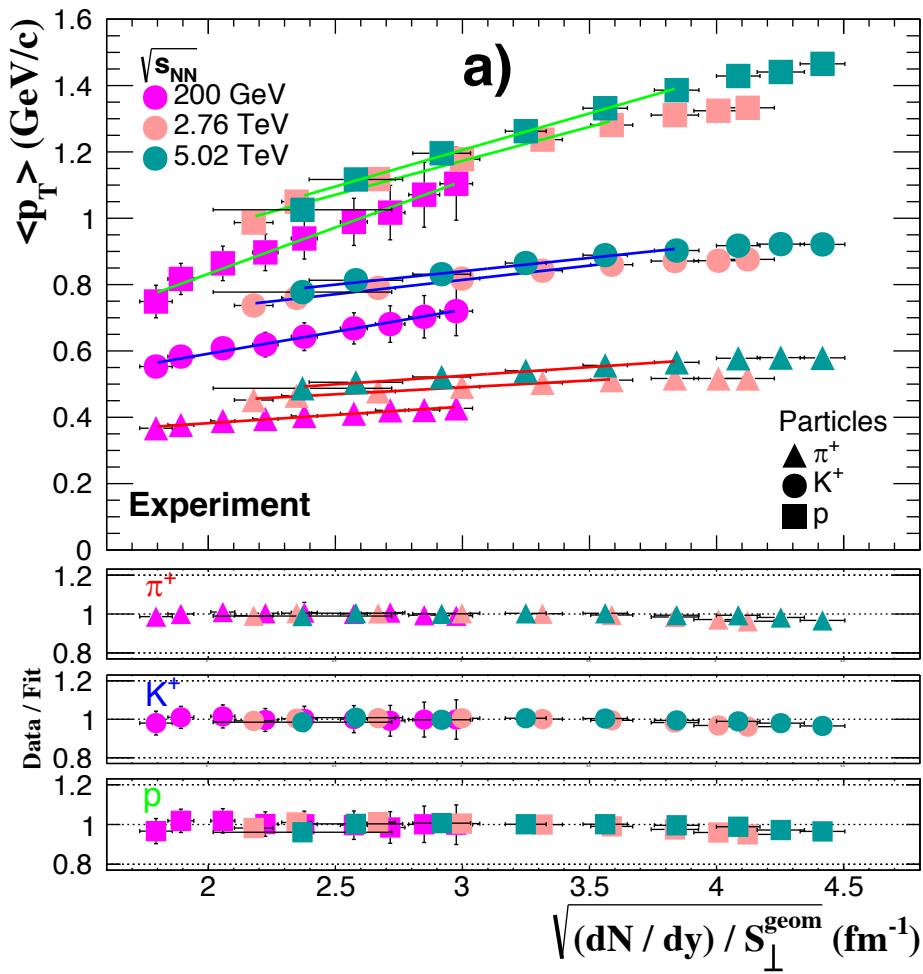
ALICE Collaboration, Eur.Phys.J. C75(2015)226

A.K.Dash, ALICE Collaboration , 9th Int. Workshop on MPI at LHC, Dec. 11-15, 2017

A few considerations

Geometrical scaling $\langle p_T \rangle$ vs. $[(dN/dy)/S_{\perp}^{\text{geom}}]^{1/2}$

Core-Corona effect



$\sqrt{s_{NN}}$ (GeV)	Slope			Offset		
	π^+	K^+	p	π^+	K^+	p
200	0.05 ± 0.02	0.13 ± 0.04	0.28 ± 0.06	0.28 ± 0.04	0.33 ± 0.09	0.27 ± 0.13
2760	0.04 ± 0.01	0.09 ± 0.02	0.20 ± 0.03	0.37 ± 0.04	0.56 ± 0.07	0.56 ± 0.08
5020	0.05 ± 0.02	0.08 ± 0.02	0.22 ± 0.03	0.37 ± 0.06	0.60 ± 0.07	0.54 ± 0.10

$\sqrt{s_{NN}}$ (GeV)	Slope			Offset		
	π^+	K^+	p	π^+	K^+	p
200	0.02 ± 0.03	0.09 ± 0.06	0.20 ± 0.11	0.36 ± 0.07	0.43 ± 0.15	0.50 ± 0.29
2760	-0.03 ± 0.02	0.07 ± 0.03	0.17 ± 0.04	0.40 ± 0.06	0.58 ± 0.10	0.66 ± 0.14
5020	0.03 ± 0.03	0.06 ± 0.02	0.17 ± 0.04	0.41 ± 0.11	0.65 ± 0.08	0.73 ± 0.16

$$\langle p_T \rangle_i^{cen} = \frac{f_{core} \langle p_T \rangle_i^{core} M_i^{core} + (1 - f_{core}) \langle p_T \rangle_i^{ppMB} M_i^{ppMB}}{f_{core} M_i^{core} + (1 - f_{core}) M_i^{ppMB}}$$

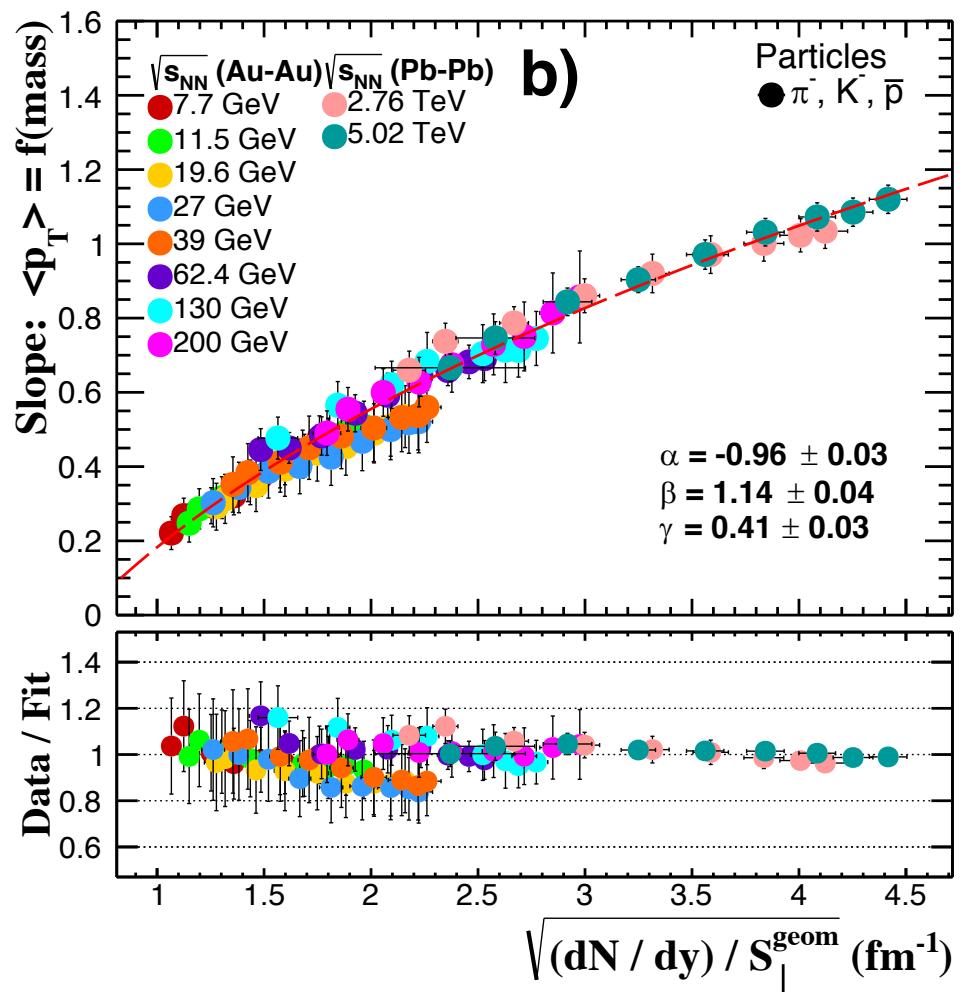
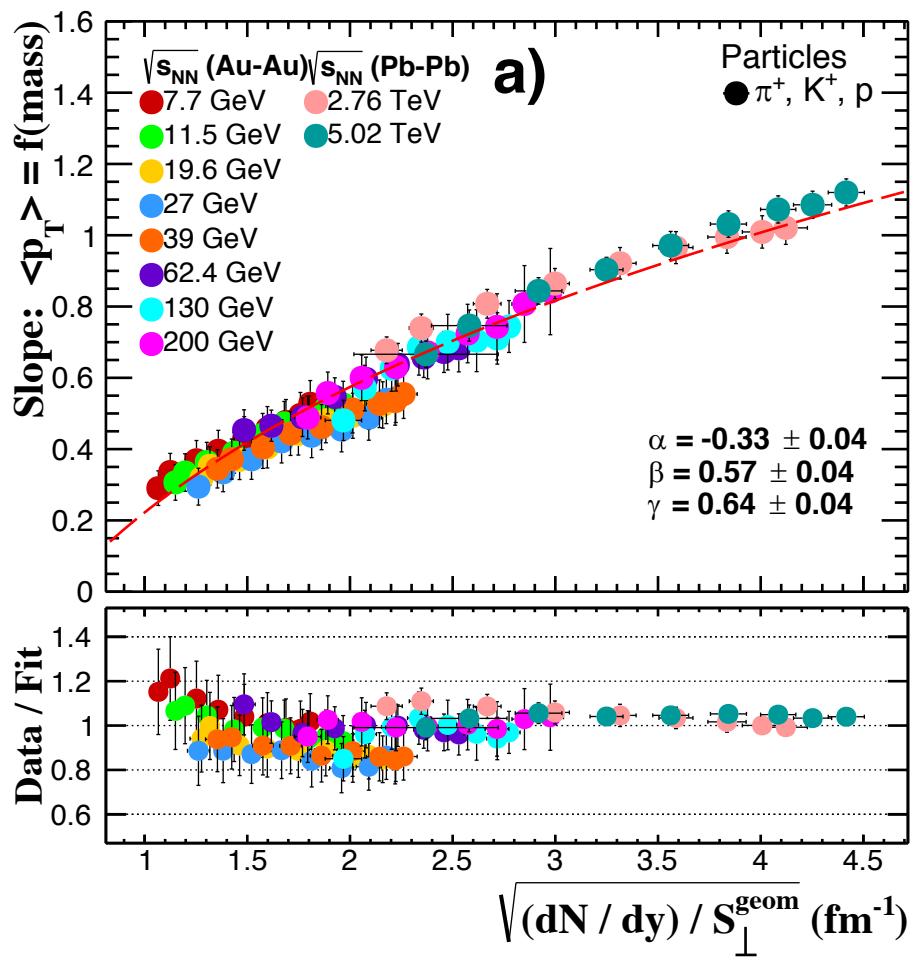
$$\left(\frac{dN}{dy} \right)_i^{cen} = \langle N_{part} \rangle [(1 - f_{core}) M_i^{ppMB} + f_{core} M_i^{core}]$$

$$M_i^{ppMB} = \frac{1}{2} (dN/dy)_i^{ppMB}$$

A few considerations

Geometrical scaling

The slope of $\langle p_T \rangle = f(\text{mass})$ vs. $[(dN/dy)/S_{\perp}^{\text{geom}}]^{1/2}$

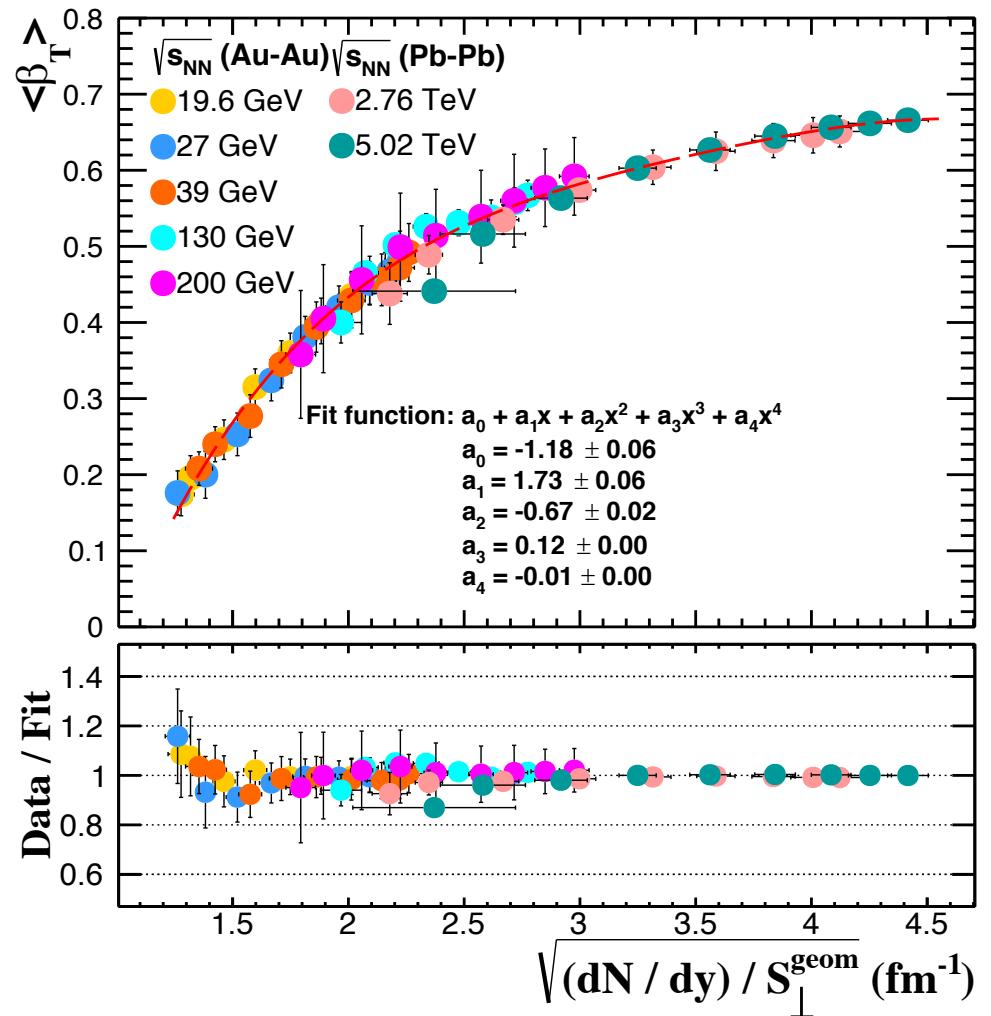
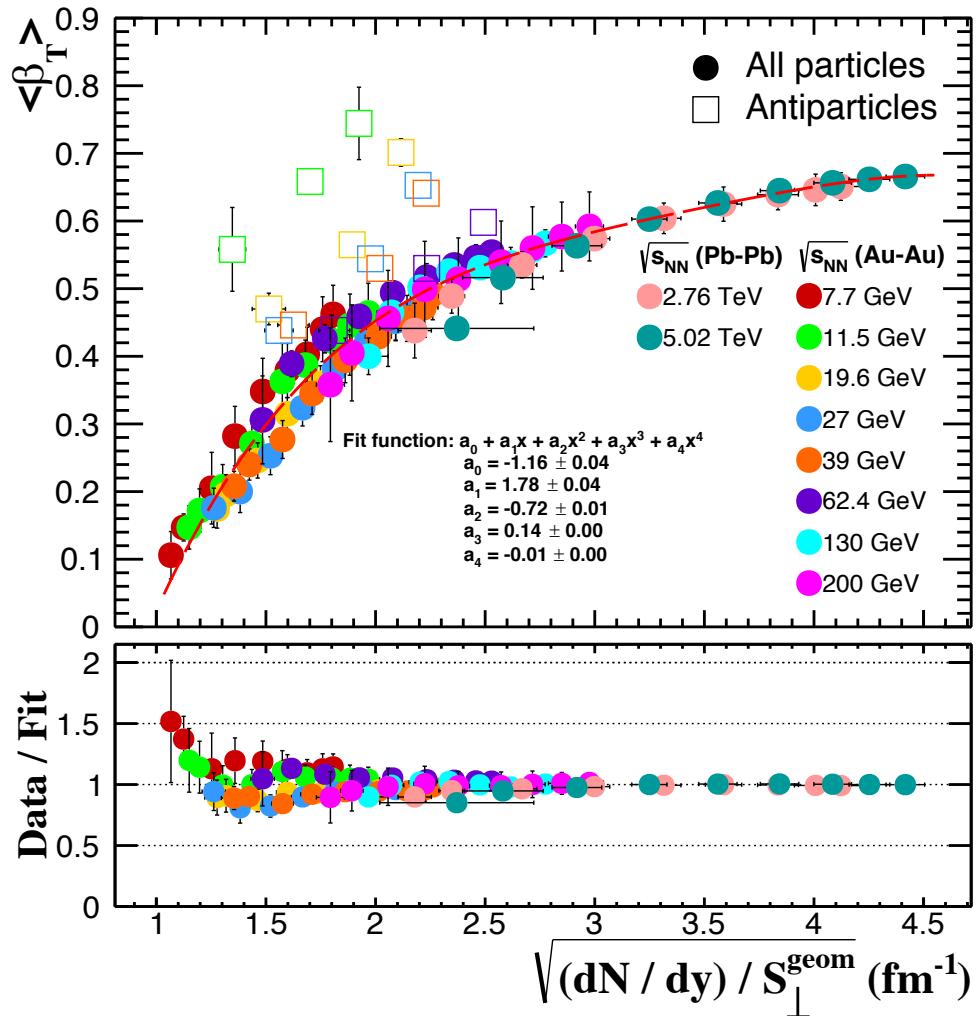


$$Slope_{\langle p_T \rangle = f(\text{mass})} = \alpha + \beta \left(\sqrt{\frac{dN}{dy}} / S_{\perp}^{\text{geom}} \right)^{\gamma}$$

A few considerations

Geometrical scaling

$\langle \beta_T \rangle$ from BGBW fits vs. $[(dN/dy)/S_{\perp}^{\text{geom}}]^{1/2}$



**Boltzmann-Gibbs
Blast Wave**

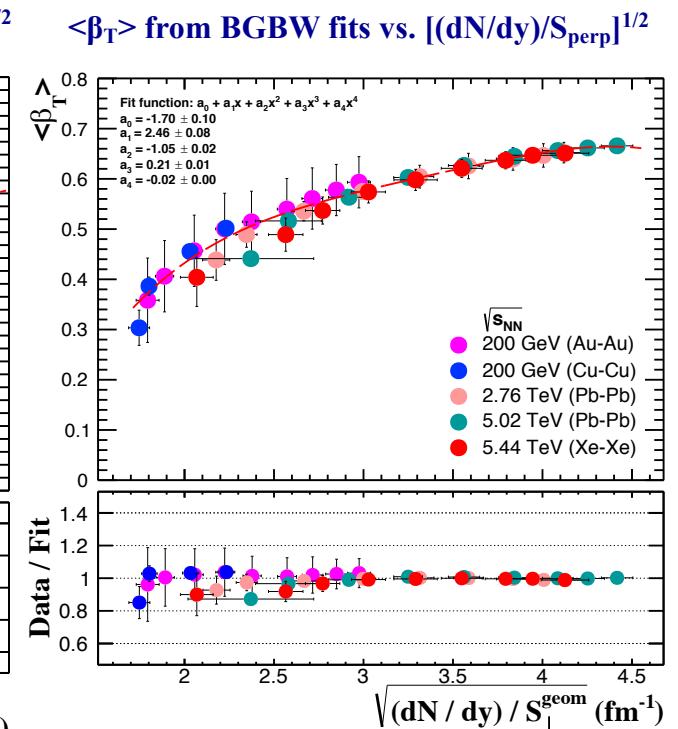
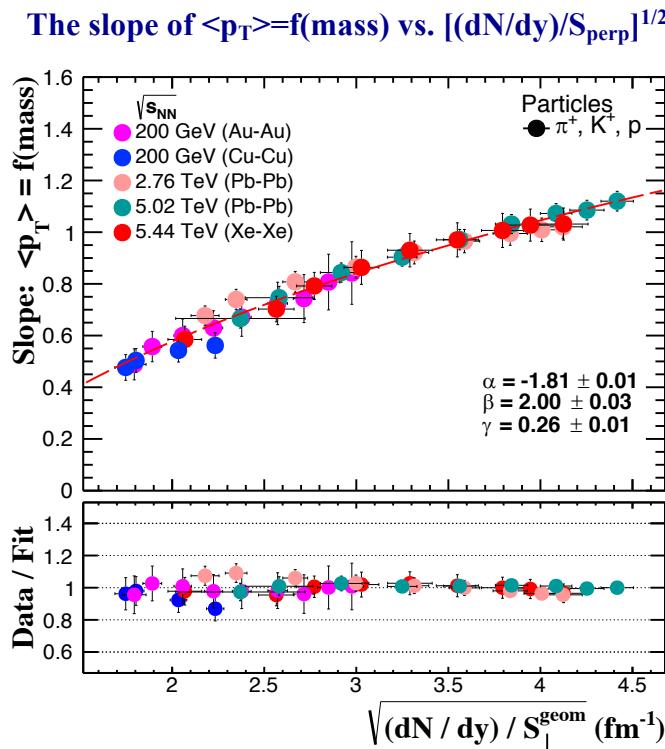
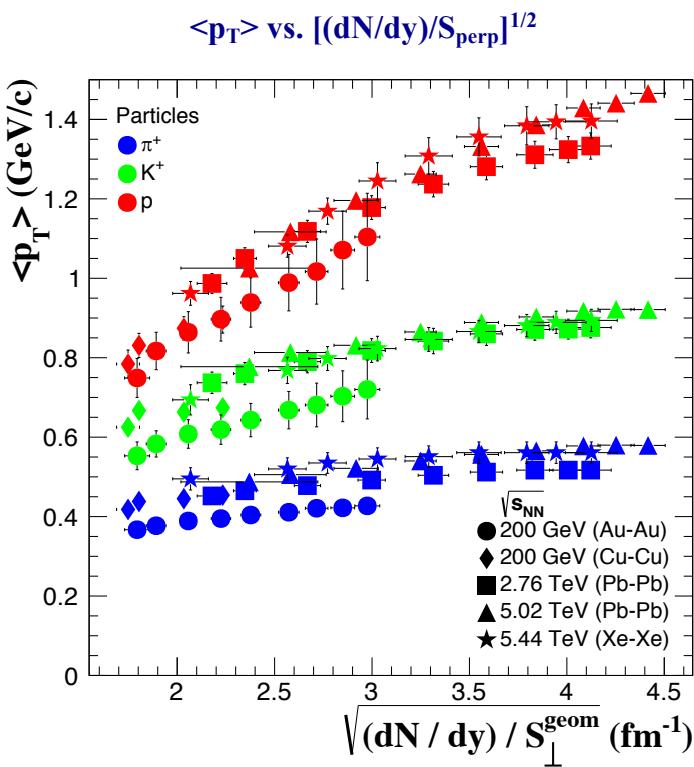
$$\left[\frac{1}{2\pi p_T} \frac{d^2 N}{dy dp_T} \propto \int_0^R r dr m_T I_0 \left(\frac{p_T \sinh \rho}{T_{kin}} \right) K_1 \left(\frac{m_T \cosh \rho}{T_{kin}} \right) \right]$$

$$\rho = \tanh^{-1} \beta_T = \tanh^{-1} \left[\left(\frac{r}{R} \right)^n \beta_s \right]$$

A few considerations

Geometrical scaling

Cu-Cu; Au-Au @ RHIC vs. Xe-Xe and Pb+Pb @ LHC



BRAHMS Collaboration, arXiv:[nucl.ex]1602.01183

F.Bellini, ALICE Collaboration, QM2018

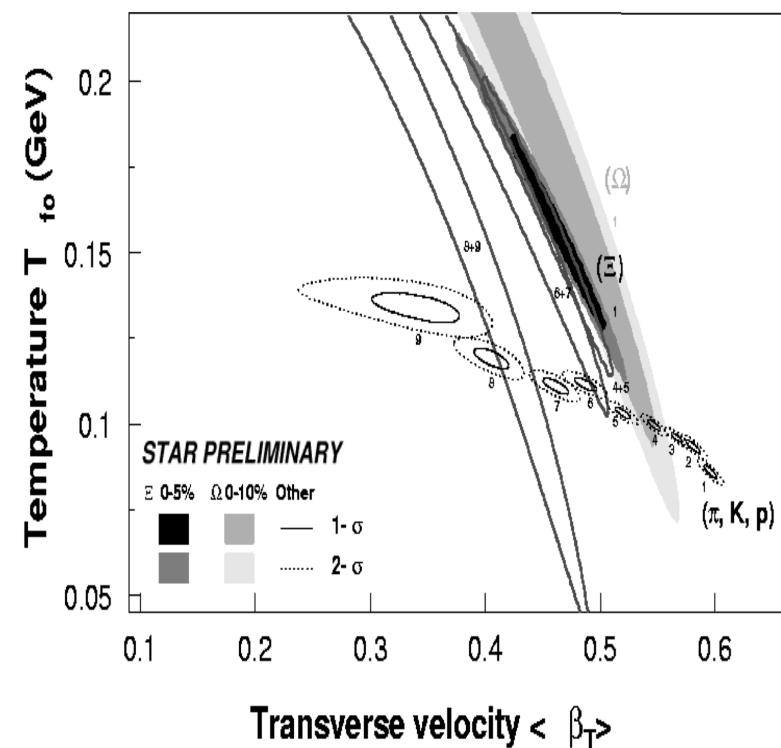
STAR Collaboration, Phys.Rev. C79(2009)034909

ALICE Collaboration, Phys.Rev. C{88}{044910}{2013}

A few considerations

A-A BGBW fits

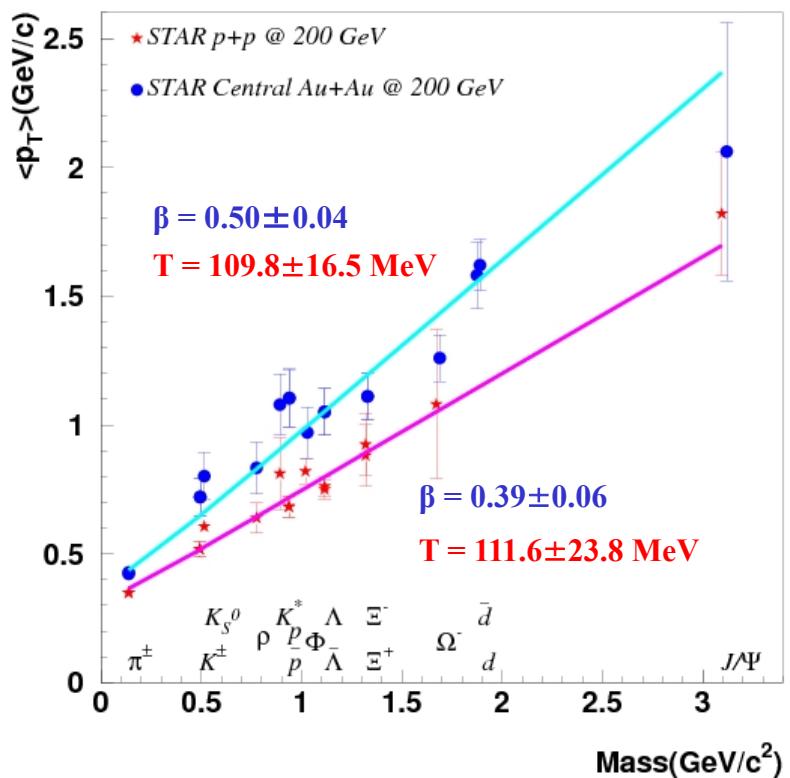
Au-Au 200 GeV



M.Etienne, STAR Coll. arXiv:[nucl-ex/0411034](https://arxiv.org/abs/nucl-ex/0411034)

$$f(p_t) \sim \int_0^R r dr m_t I_0 \left(\frac{p_t \sinh \rho}{T} \right) K_1 \left(\frac{m_t \cosh \rho}{T} \right)$$

$$\langle p_t \rangle = \frac{\int_0^\infty p_t^2 f(p_t) dp_t}{\int_0^\infty p_t f(p_t) dp_t}$$

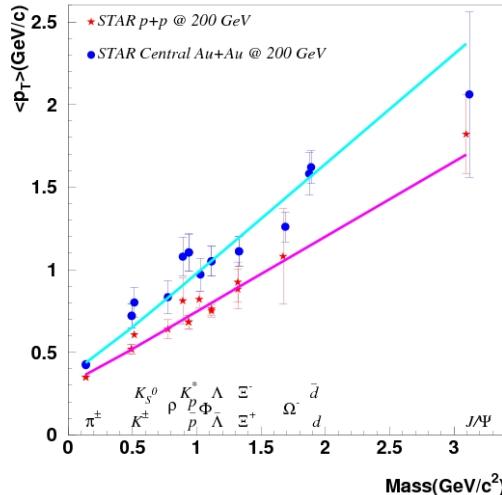


M.Petrovici and Amalia Pop,
AIP Conference Proceedings 972(2008)98

A few considerations

A-A Tsallis BW fits

$$f(p_t) = m_t \int_{-Y}^Y \cosh(y) dy \int_{-\pi}^{\pi} d\phi \int_0^R rdr \left(1 + \frac{q-1}{T} (m_t \cosh(y) \cosh(\rho) - p_t \sinh(\rho) \cos(\phi))\right)^{-1/(q-1)}$$



*A. Lavagno, Phys.Lett. A301(2002)13
Z. Tang et al, arXiv:0812.1609 nucl-ex*

$\pi^\pm, K^\pm, K^*, K_s^0, \bar{p}, \Lambda, \bar{\Lambda}, \Xi^\pm, \Omega^-, d, \bar{d}$,

J/ψ

System	p + p	p + p	Au + Au	Au + Au
Model	BGBW	TBW	BGBW	TBW
T [MeV]	111.6 ± 23.8	78.86 ± 10.13	109.8 ± 16.5	86.8 ± 1.54
β	0.39 ± 0.06	0.027 ± 0.10	0.50 ± 0.04	0.48 ± 0.04
q	1.0	1.0874	1.0	1.0247

$\pi^\pm, K^\pm, K^*, p, \bar{p}, d,$
 \bar{d}

	Au + Au	Au + Au
	BGBW	TBW
T [MeV]	98.7 ± 19.5	79.05 ± 0.04
β	0.54 ± 0.04	0.53 ± 0.0005
q	1.0	1.0175

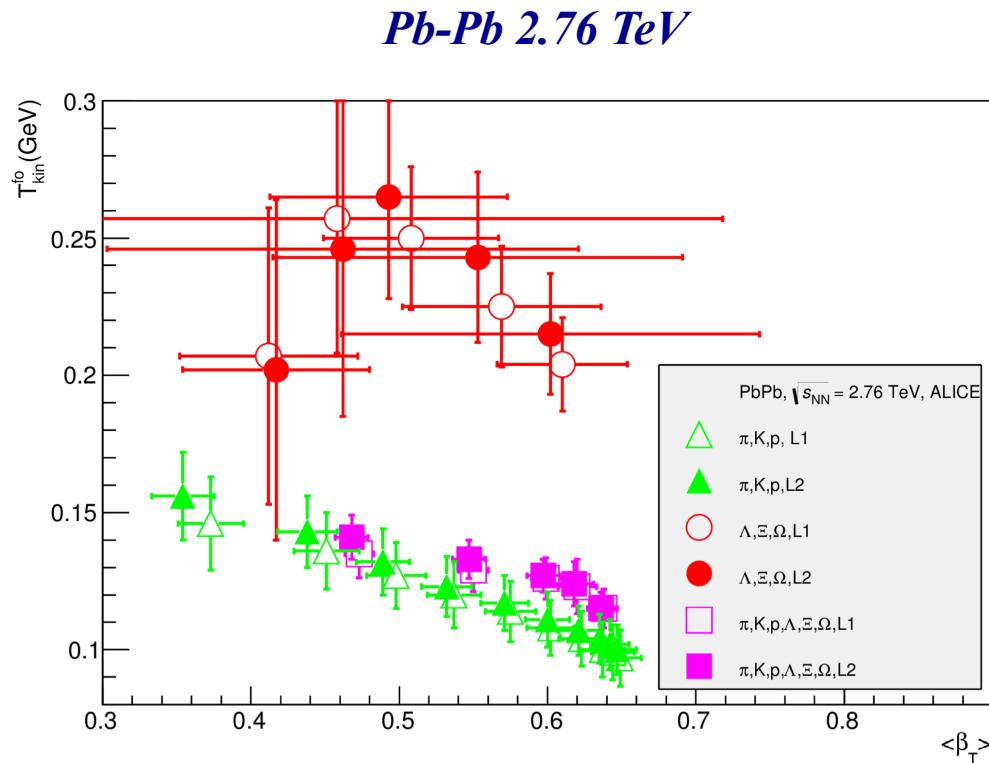
$\Lambda, \bar{\Lambda}, \Xi^\pm, \Omega^-, J/\psi$

	Au + Au
	TBW
T [MeV]	198.0 ± 7.6
β	0.32 ± 0.012
q	1.0247

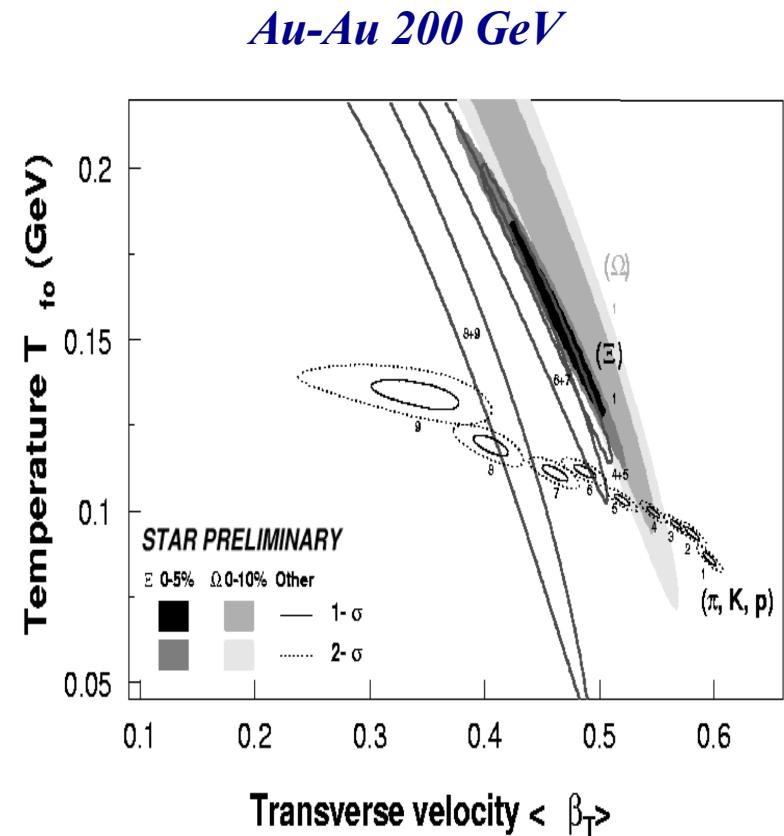
	Au + Au	Au + Au
	BGBW	TBW
T [MeV]	215.5 ± 89.2	200.5 ± 0.1
β	0.37 ± 0.12	0.36
q	1.0	1.021

A few considerations

A-A BGBW - fits

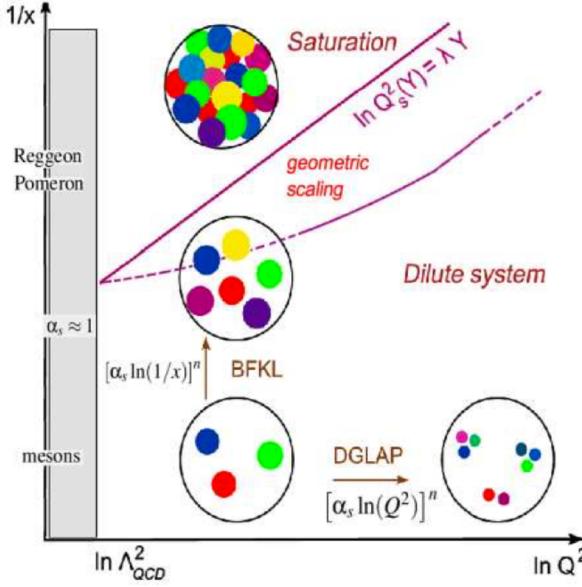


M.Petrovici et al. AIP Conf.Proc. 1852, 050003-1 (2017)



M.Etienne, STAR Coll. arXiv:nucl-ex/0411034

What is really new at LHC ?



- for higher μ_B more baryons are excited

Chiral transition:

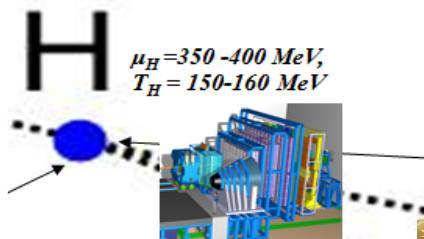
$\mu_B > \mu_E$ - first order
 $\mu_B < \mu_E$ - crossover
 realistic u,d,s masses

Liquid-gas phase transition:

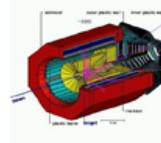
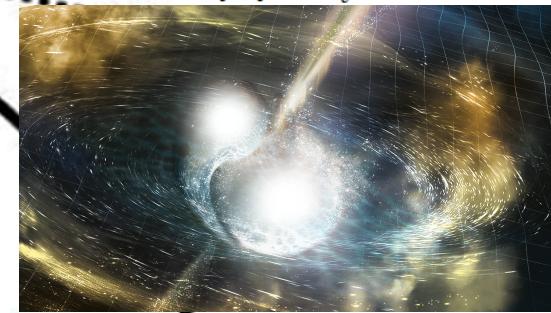
$\mu_{NM} \cong 924 \text{ MeV}$
 $n_0 = 0.17 \text{ fm}^{-3}$

Expectations based on QCD

QCD Critical Points



Their meeting point
 Triple point
 H - remnant for finite N_c



G



Superfluid nuclear matter

- large N_c QCD phase diagram:
 - three regions, i.e.:
 - confined
 - deconfined
 - quarkionic phase separated by phase transition
- ...
- limit of QCD suppressed by $1/N_c$ contribution to the $N_c = \infty$ world for quarkyonic matter

Quark-Hadron continuity:

μ_B

Superconducting quark matter



Theoretical approaches - short list of references

Macroscopic (Statistical and Hydrodynamical) Models

L.D. Landau, E.M. Lifshitz, Fluid Mechanics (Pergamon, Oxford, 1959)
H. Stöcker, W. Greiner, Phys. Rep. 137(1986)277
R.B. Clare, D. Strottman, Phys. Rep. 141(1986)177
E. Schnedermann, J. Sollfrank, U. Heinz, Phys. Rev. C48(1993)2462
J. Brachmann et al., Nucl. Phys. A619(1997)391

Microscopic (string-, transport-, cascade-, etc.) Models

FRITIOF

B. Anderson et al., Phys. Rep. 97(1983)31

VENUS

K. Werner, Phys. Rep. 232(1993)87

QGSM

N.S. Amelin et al., Sov. J. Nucl. Phys. 51, 327 (1990)

RQMD

H. Sorge, H. Stöcker, W. Greiner, Ann. Phys. (N.Y.) 192, 266 (1989)

Theoretical approaches - short list of references

HJING (Heavy-Ion Jet Interaction Generator) Monte Carlo Model

- two-component geometrical model of minijet production and soft interaction
- incorporated nuclear effects: nuclear modification of parton distribution functions and jet quenching via final state jet medium interaction

X.N.Wang et al., Phys.Rev. D44(1991)34501

M. Gyulassy et al., Comp.Phys.Comm. 83(1994)301

W.T.Deng et al., Phys.Rev. C83(2011)014915

- UrQMD** - describes the phenomenology of hadronic interactions at low and intermediate energies ($\sqrt{s} < 5 \text{ GeV}$) in terms of interactions between known hadrons and their resonances
- at energies $\sqrt{s} > 5 \text{ GeV}$, the excitation of color strings and their subsequent fragmentation in to hadrons is considered

M.Bleicher et al., J.Phys. G25(1999)1859

Theoretical approaches - short list of references

NeXSPheRIO - a combination of two codes:

- *SPheRIO* - describes the hydrodynamic evolution
- *NeXus* - computes the initial conditions $T_{\mu\nu}$, j^μ and u^μ on a proper time hypersurface

*R.Andrade et al., Acta Phys. Hung. A19(2004)1
arXiv:[nucl-th]0511021*

AMPT - a combination of four models:

- *HIJING* - for generating initial conditions
- *ZPC* - Zhang's parton cascade for partonic scatterings
- Lund string fragmentation model
 - or
 - quark coalescence model*
for hadronization
- *ART* - relativistic transport model for hadronic scatterings

*Z.W.Lin et al., Phys.Rev. C72(2005)064901
J.Xu et al., arXiv:[nucl-th]1103.5187*

PHSD - Parton-Hadron-String-Dynamics transport approach, based on dynamical quasiparticle model for partons (DQPM) matched to reproduce lattice-QCD results including partonic equation of state - in thermodynamic equilibrium. The transition from partonic to hadronic degrees of freedom is described by covariant transition rates for the fusion of quark-antiquark pairs or three quarks (antiquarks) obeying flavor current conservation, color neutrality and energy-momentum conservation

*W.Cassing et al., arXiv:[nucl-th]0907.5331
V.P.Konchakovski et al., arXiv:[nucl-th]1201.3220*

Theoretical approaches - short list of references

MUSIC - MUSCL-type (*Monotonic Upstream-centered Schemes for Conservation Laws*)
a combination
- implementation of **MUSCl** for heavy Ion Collisions

B.Schenke et al., *Phys.Rev. C*82(2010)014903

superSONIC - a combination of pre-equilibrium flow, viscous hydrodynamic evolution and late stage
hadronic rescatterings

R.D. Weller et al., *arXiv:[nucl-th]1701.07145*